

# Interaction tactile et multi-points

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*ressources:* <http://malacria.com/teachings/>

Diapositives adaptées de Géry Casiez et Gilles Bailly

# CS Education Week

Recognizing the Transformative Role of Computing

Certified Software

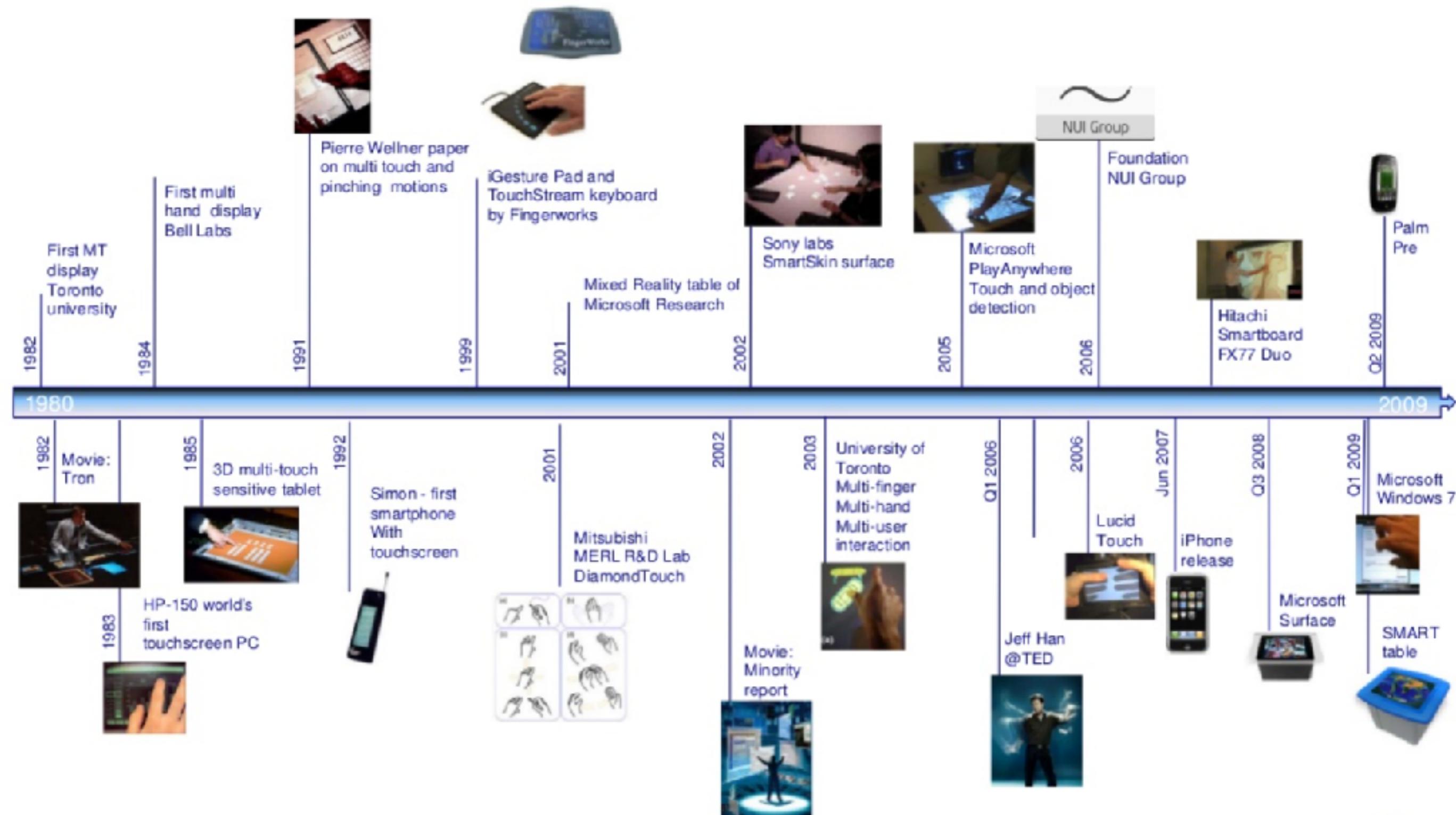
A Conversation with Pixar's Ed Catmull

Bayesian Networks

The Theft of Business Innovation

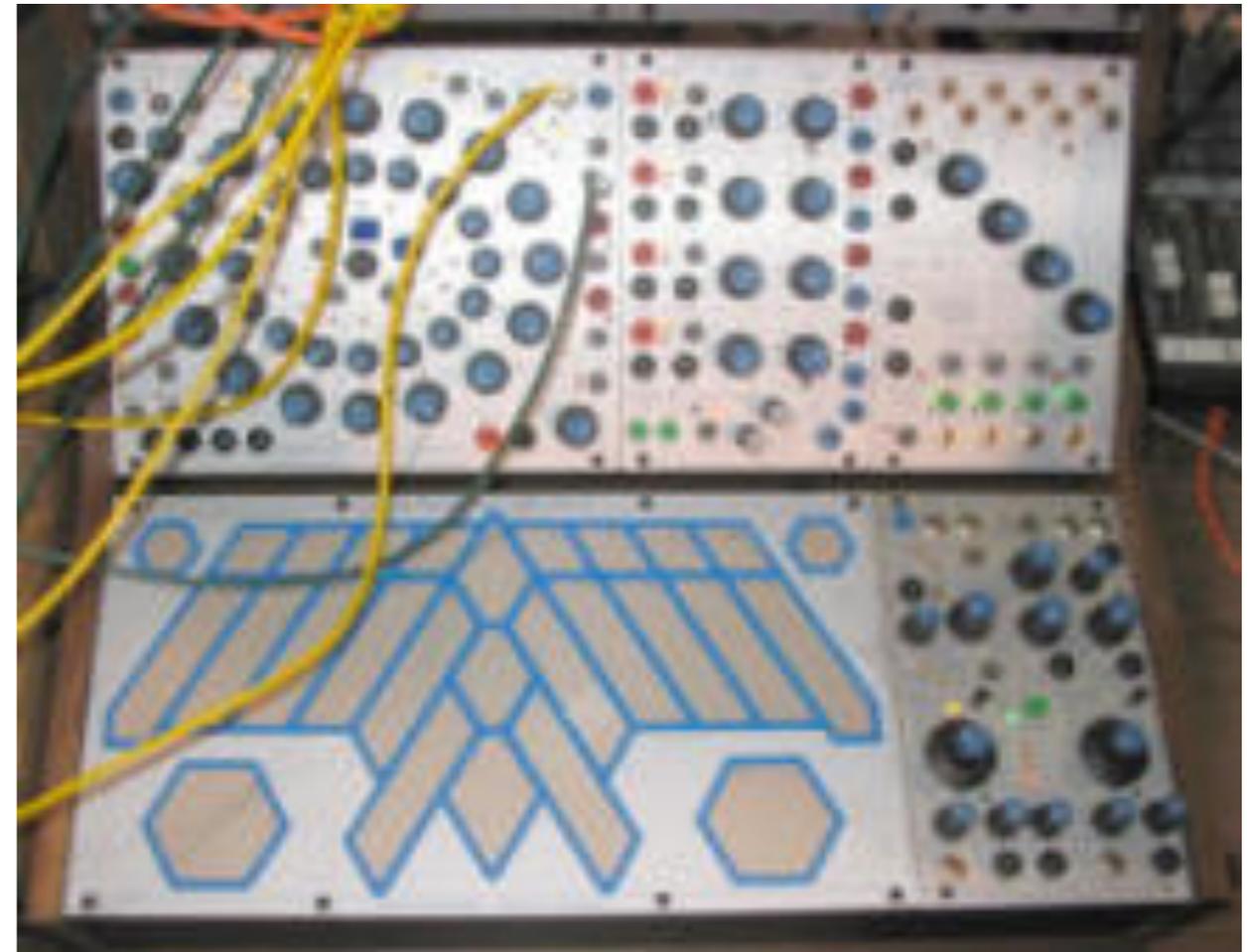


# History of Multi-touch interaction





Keyboard



Electronic Touch Sensor

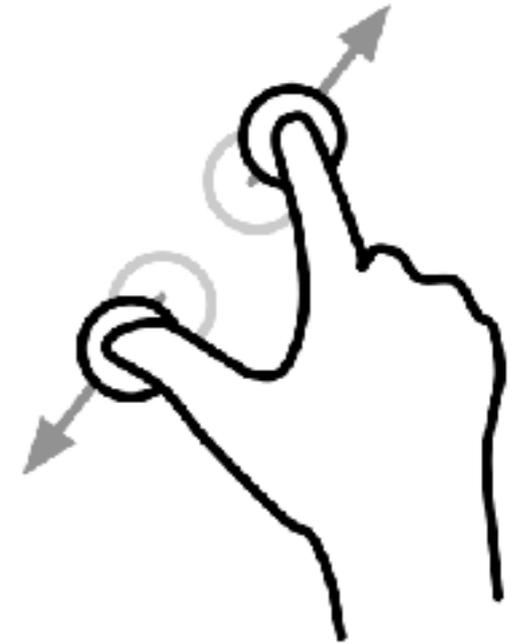
**1983**

*VideoPlace*



**1985**

*RST [Krueger et al.]*



**1985**

*Multitouch Tablet*



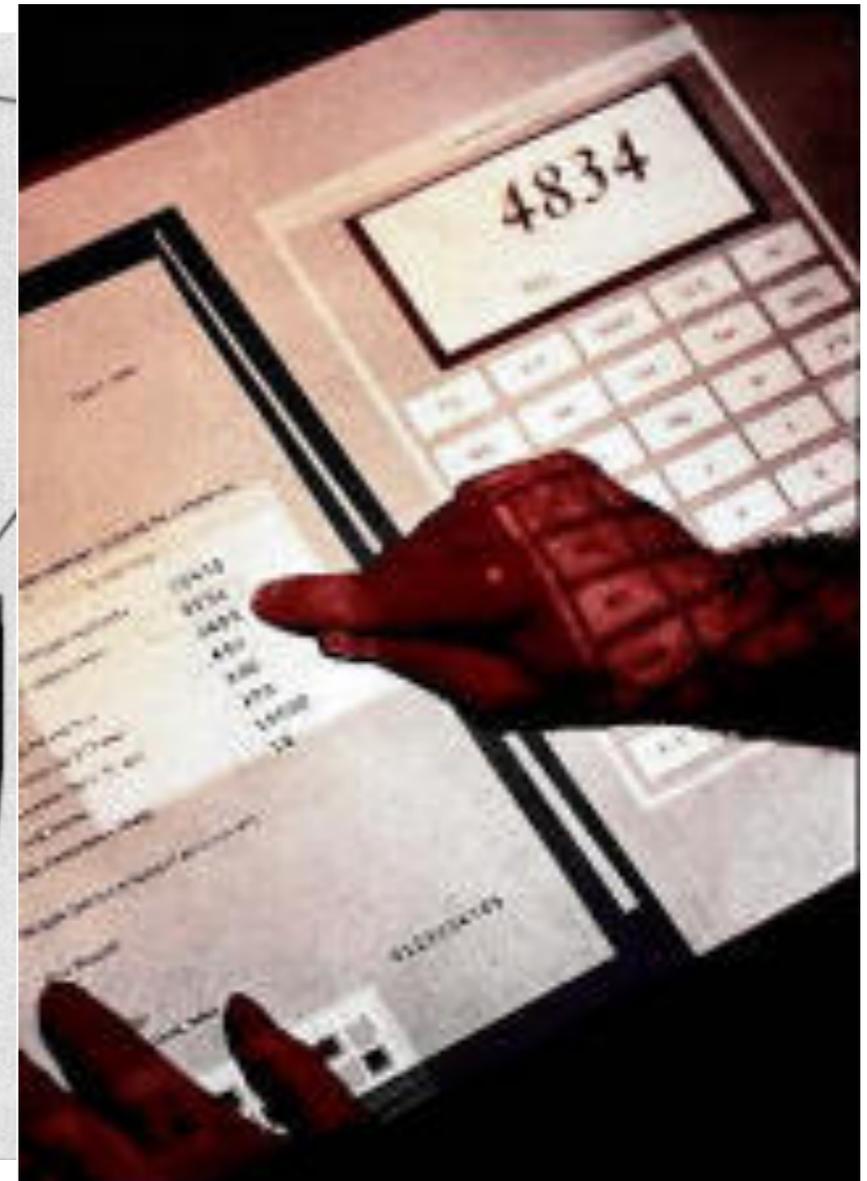
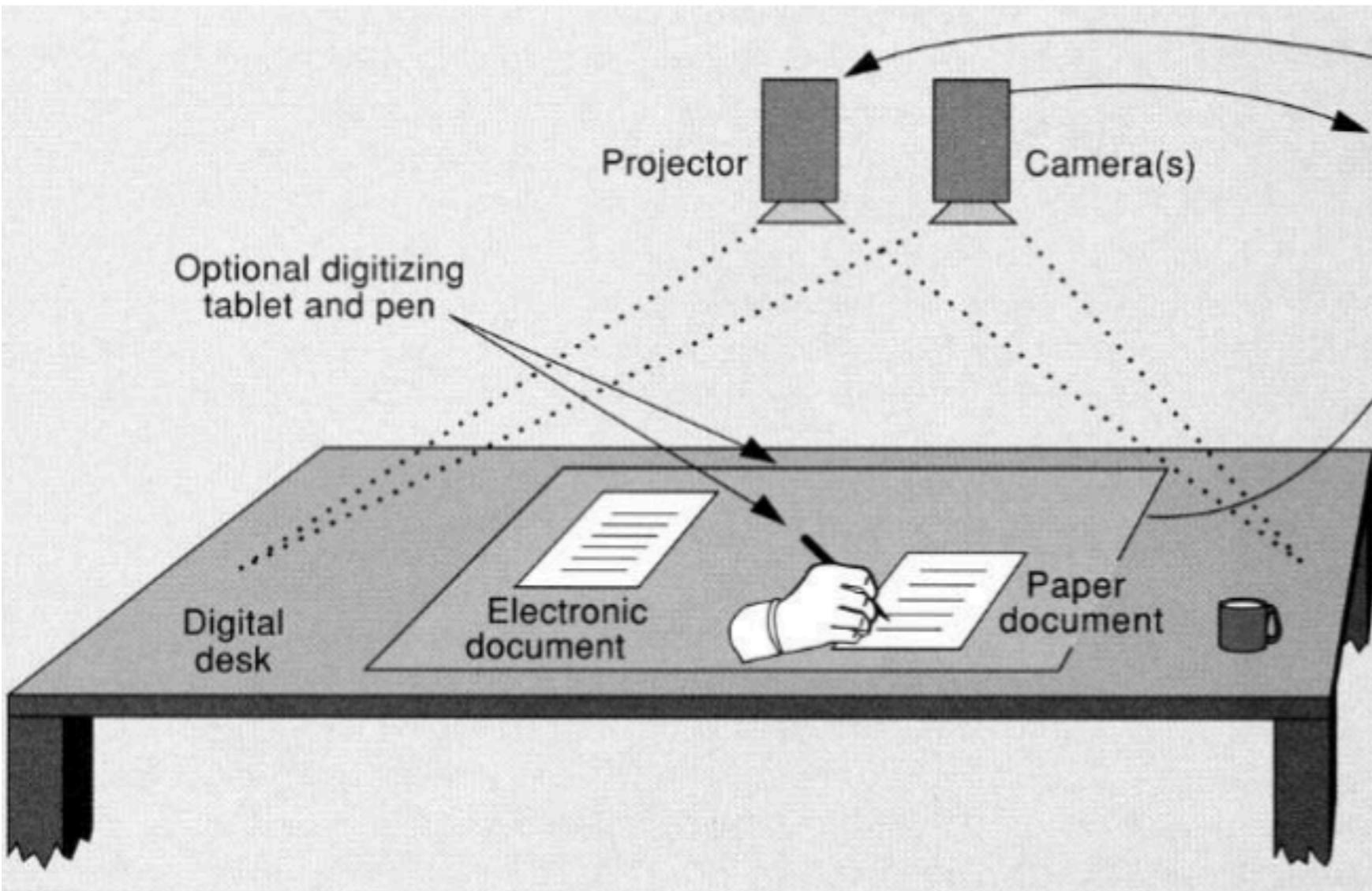
**1985**

*Multitouch Tablet*



1991

*DigitalDesk*



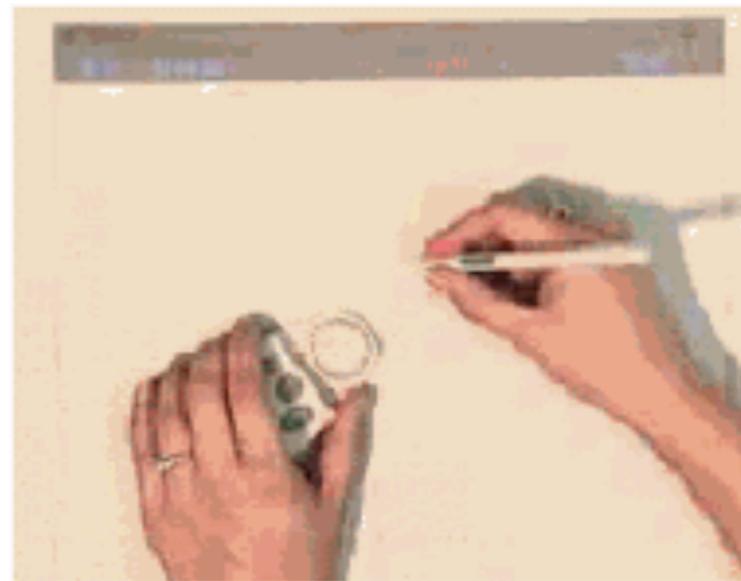




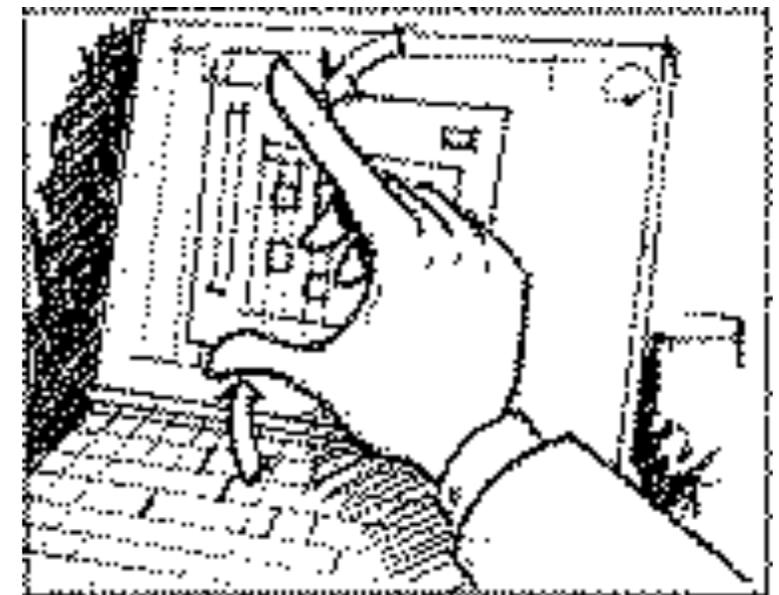
1991



Flip Keyboard



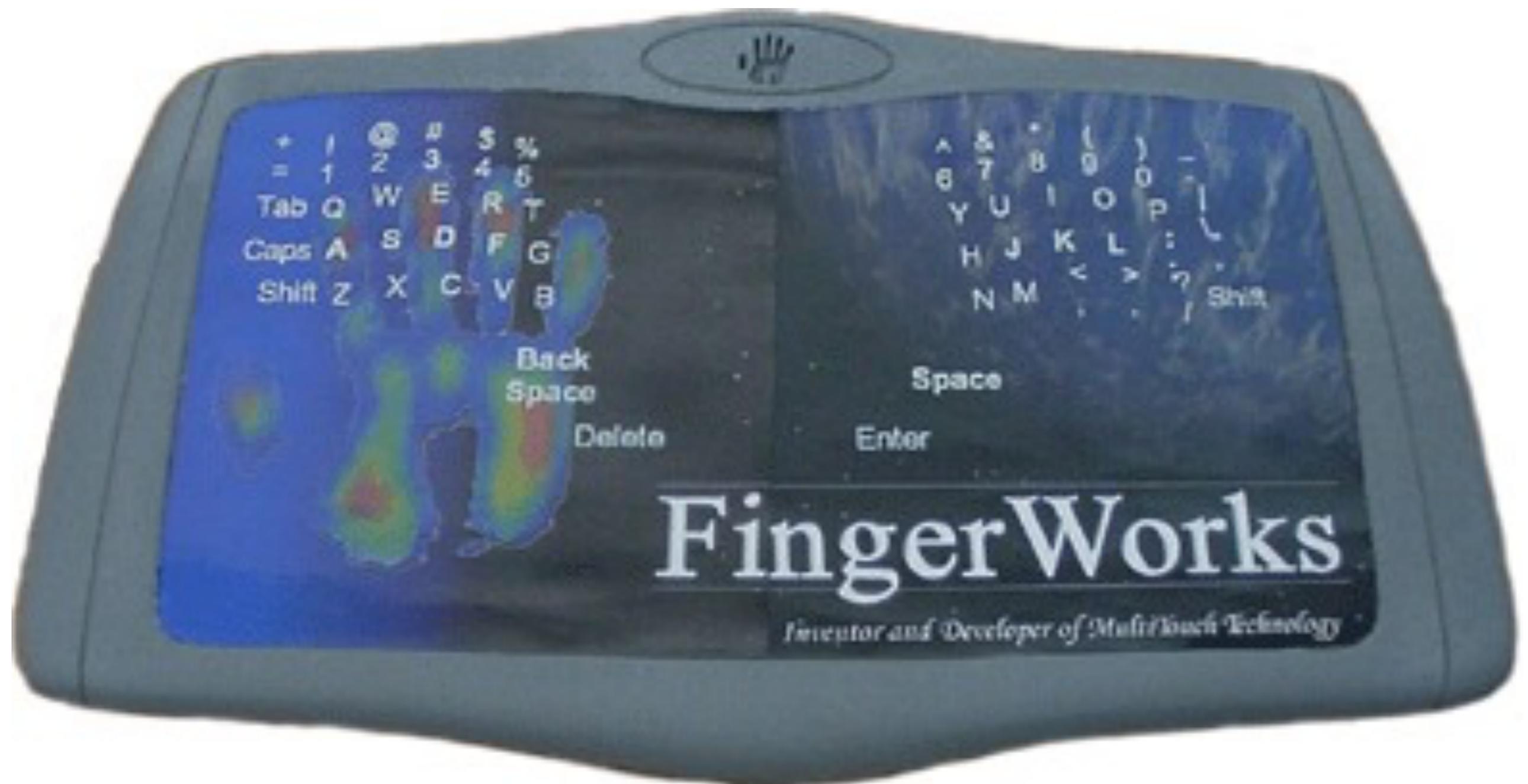
Wacom



Starfire

**2001**

*FingerWorks*



# 2001

## *Diamond Touch*



**2002**

*Smartskin*

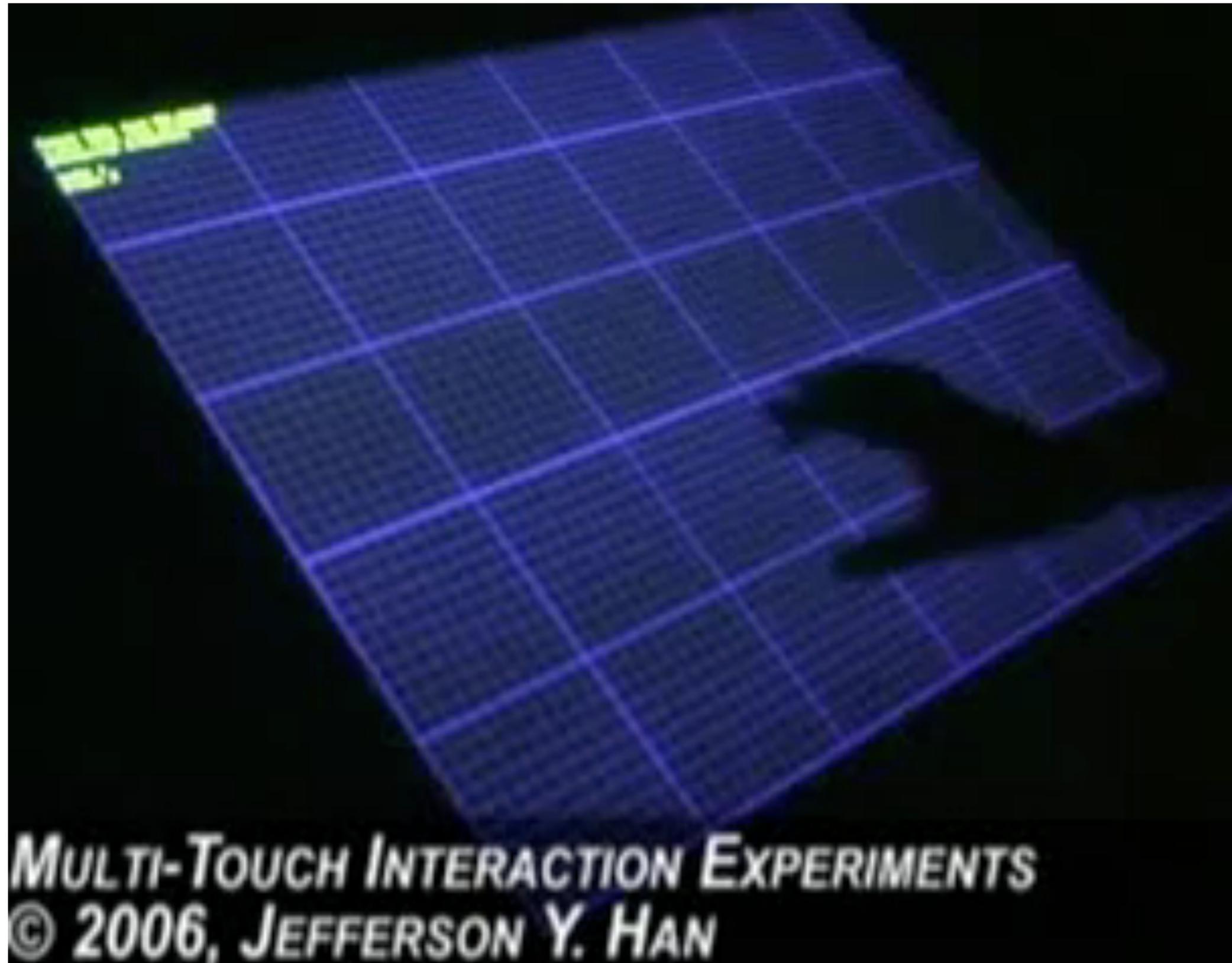


**2003**

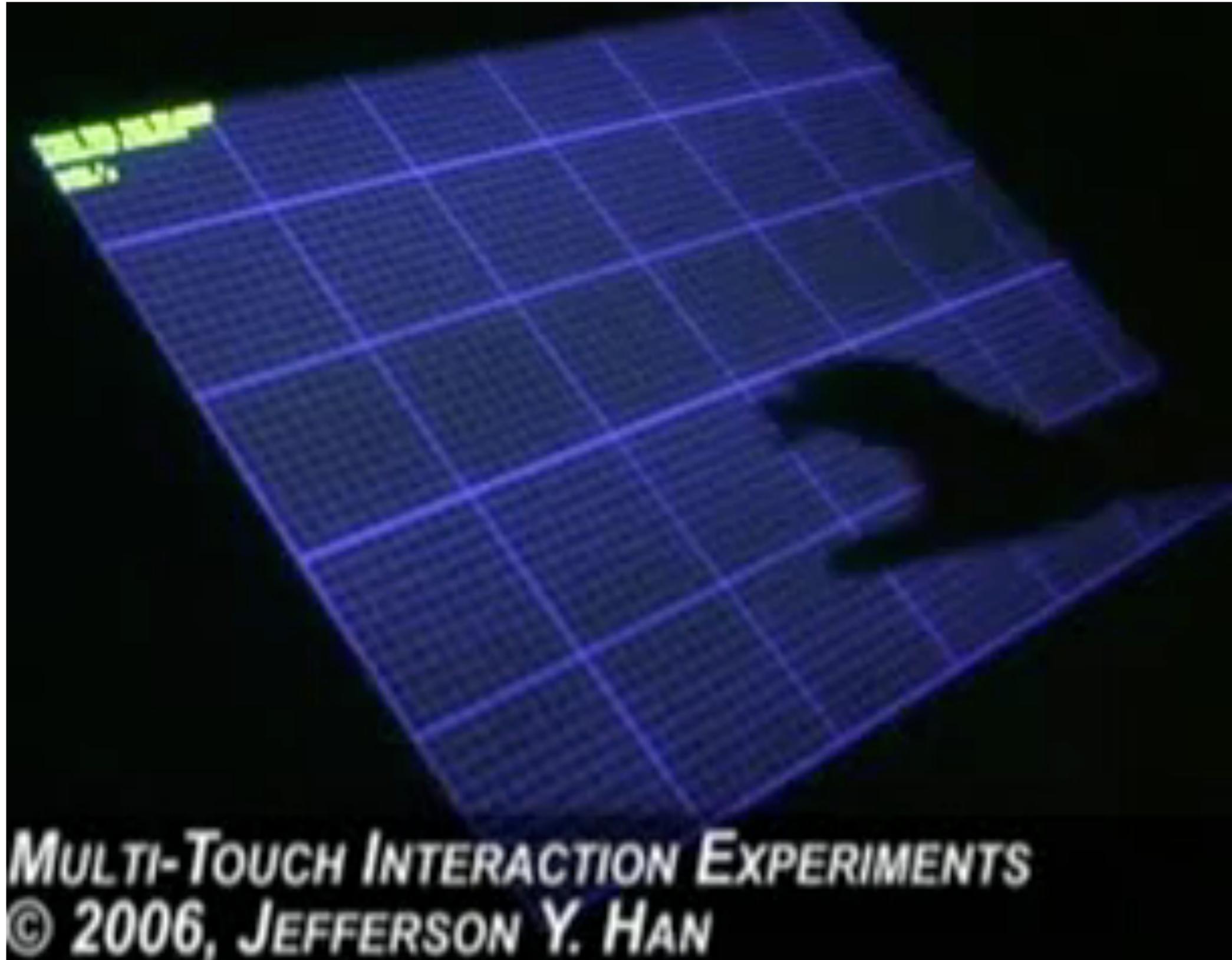
*Lemur/Jazz Mutant*



2006



2006



# 2007 *iPhone*



**2007**

*Microsoft Surface*



# 2007

*ThinSight*



**2011**

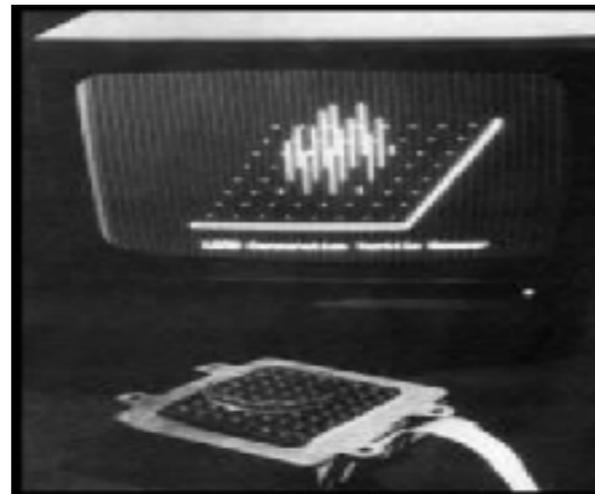
*Microsoft Surface 2.0*



# Technologie



1972  
Plato IV



1981



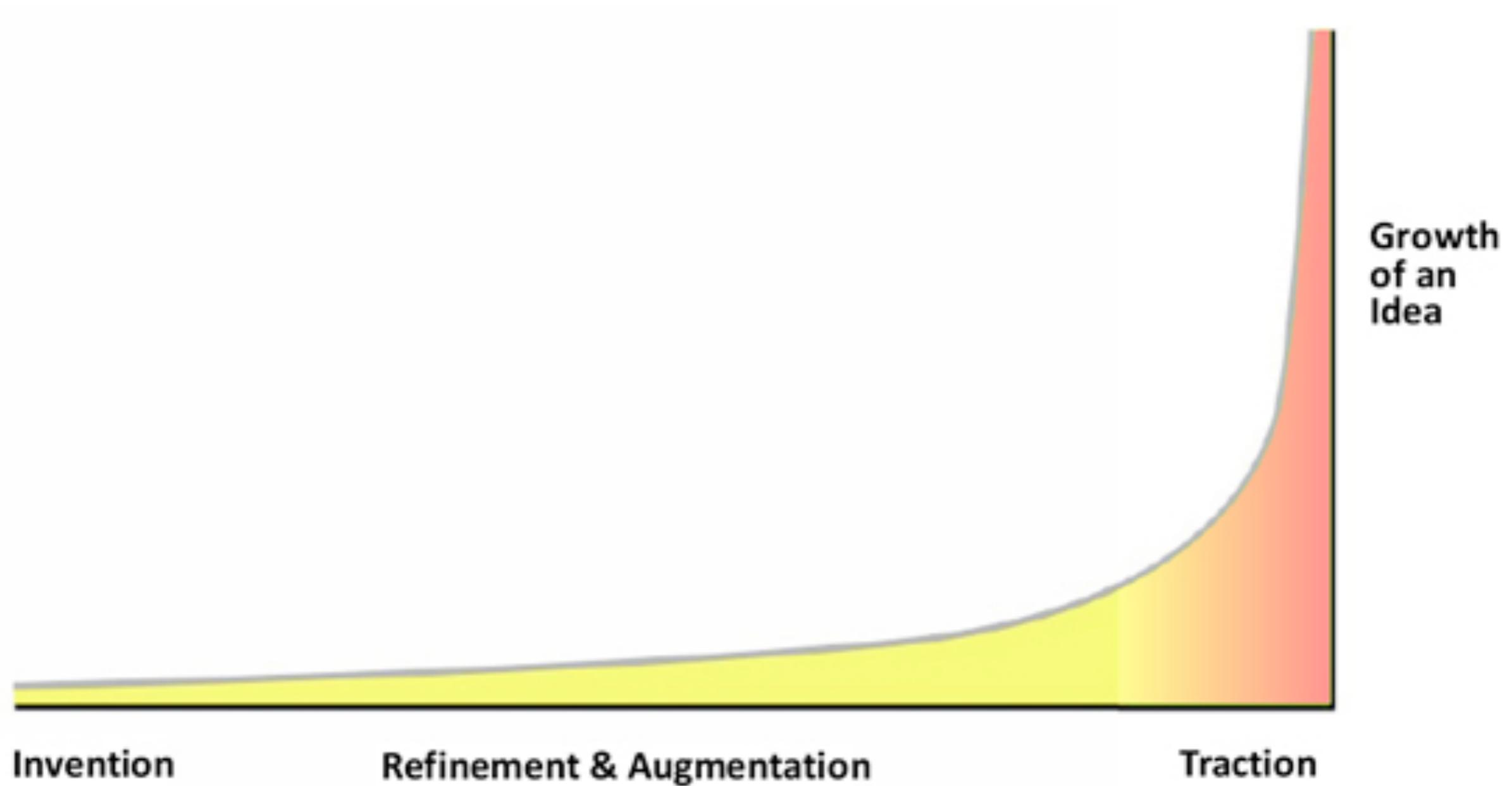
2007  
iPhone



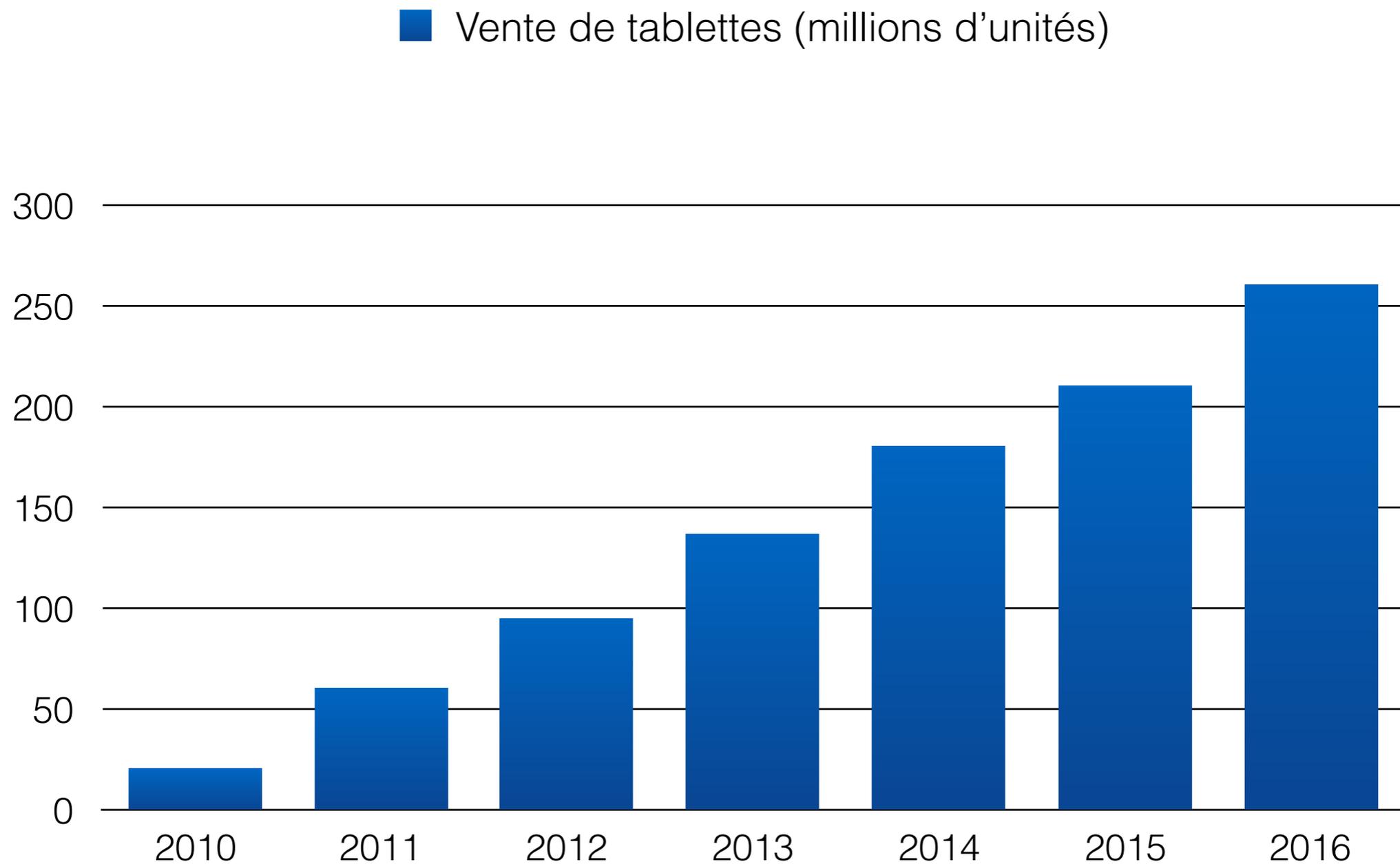
2010  
iPad

# The long nose of innovation

Bill Buxton

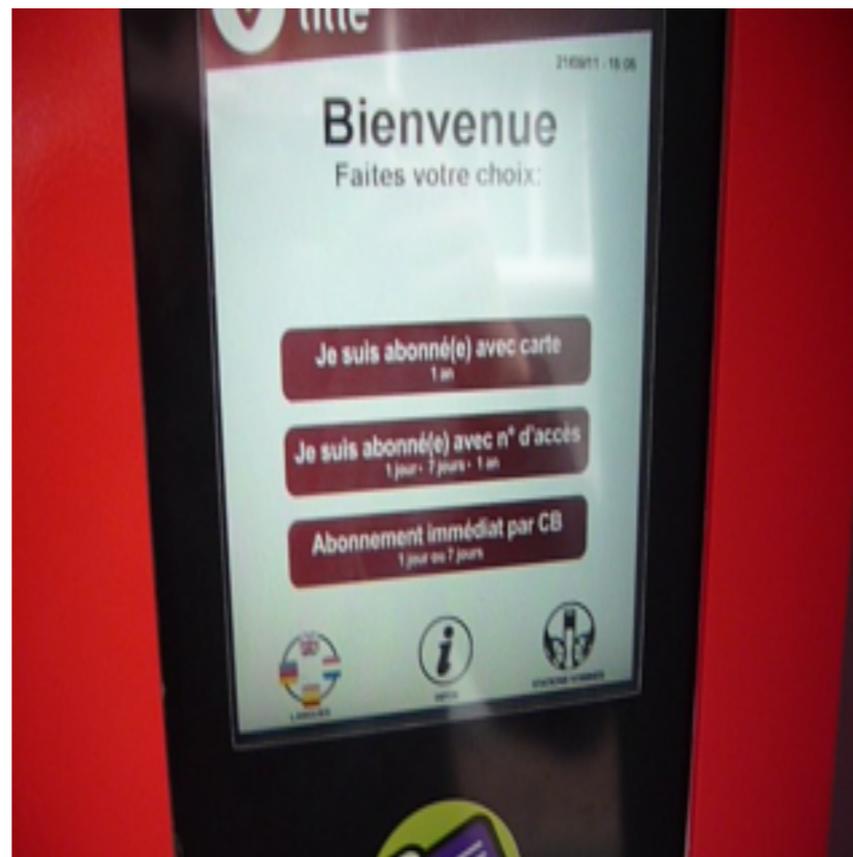


# Technologie



# Technologie tactile

- Nombre de périphériques tactiles dans les espaces publics



2007

2008

2009

2010

2011

2012<sub>23</sub>

« Everything is best for something and worst for something else. The trick is knowing what is what, for what, when, for whom, where, and most importantly, why. »

–Bill Buxton

# Avantages



Barrière d'entrée



Robuste



Plaisir



Sans fil

# Multipoint vs souris



# Multipoint vs souris



# Multipoint vs souris

(2) Degrés de Liberté (DDL) intégrés



# Multipoint vs souris

(2) Degrés de Liberté (DDL) intégrés

(1) pointeur



# Multipoint vs souris

(2) Degrés de Liberté (DDL) intégrés

(1) pointeur

interaction *indirecte*



# Multipoint vs souris

(2) Degrés de Liberté (DDL) intégrés

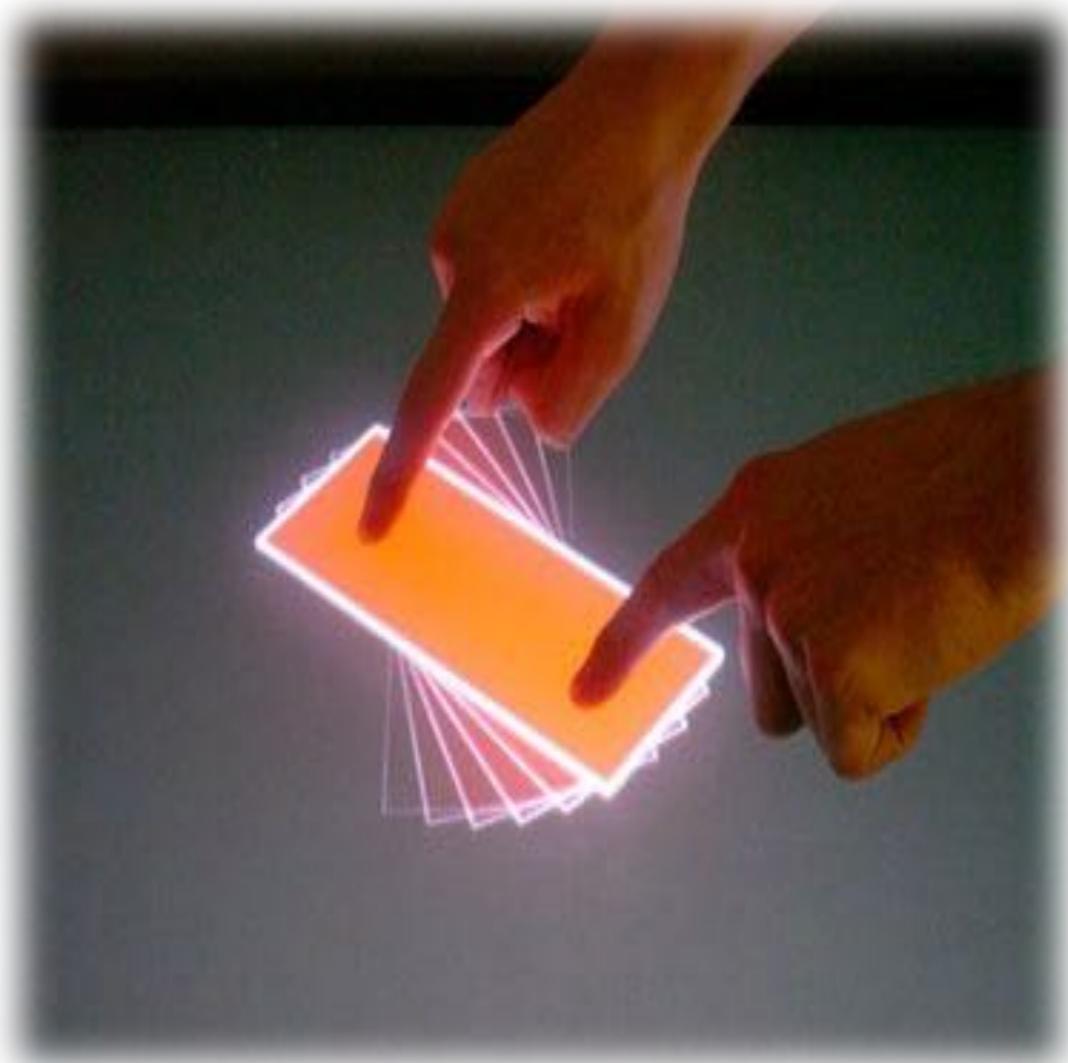
(1) pointeur

interaction *indirecte*

+1 DDL séparé



# Directivité



Direct



Indirect

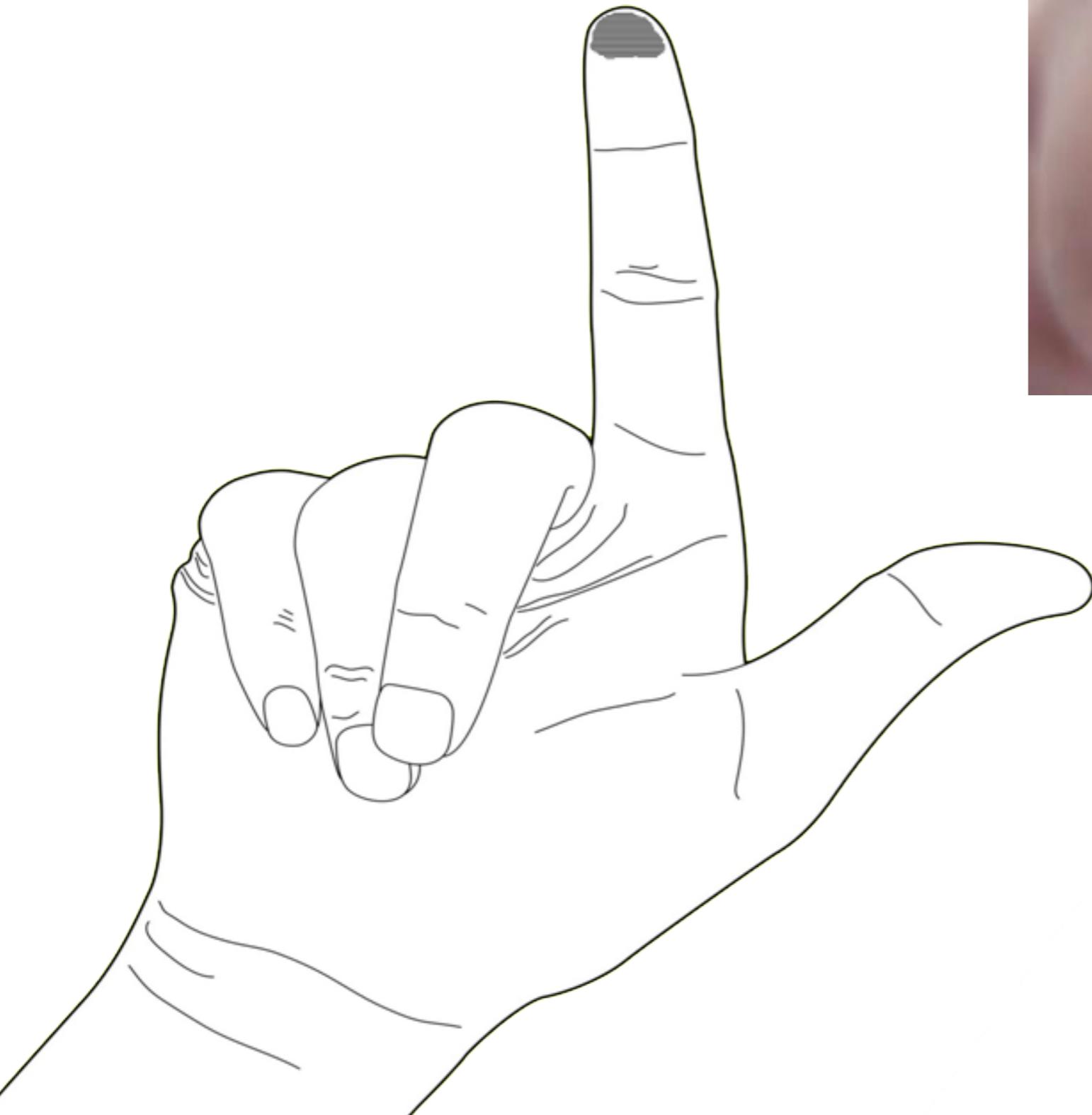
# Problems

## *Fat Finger*



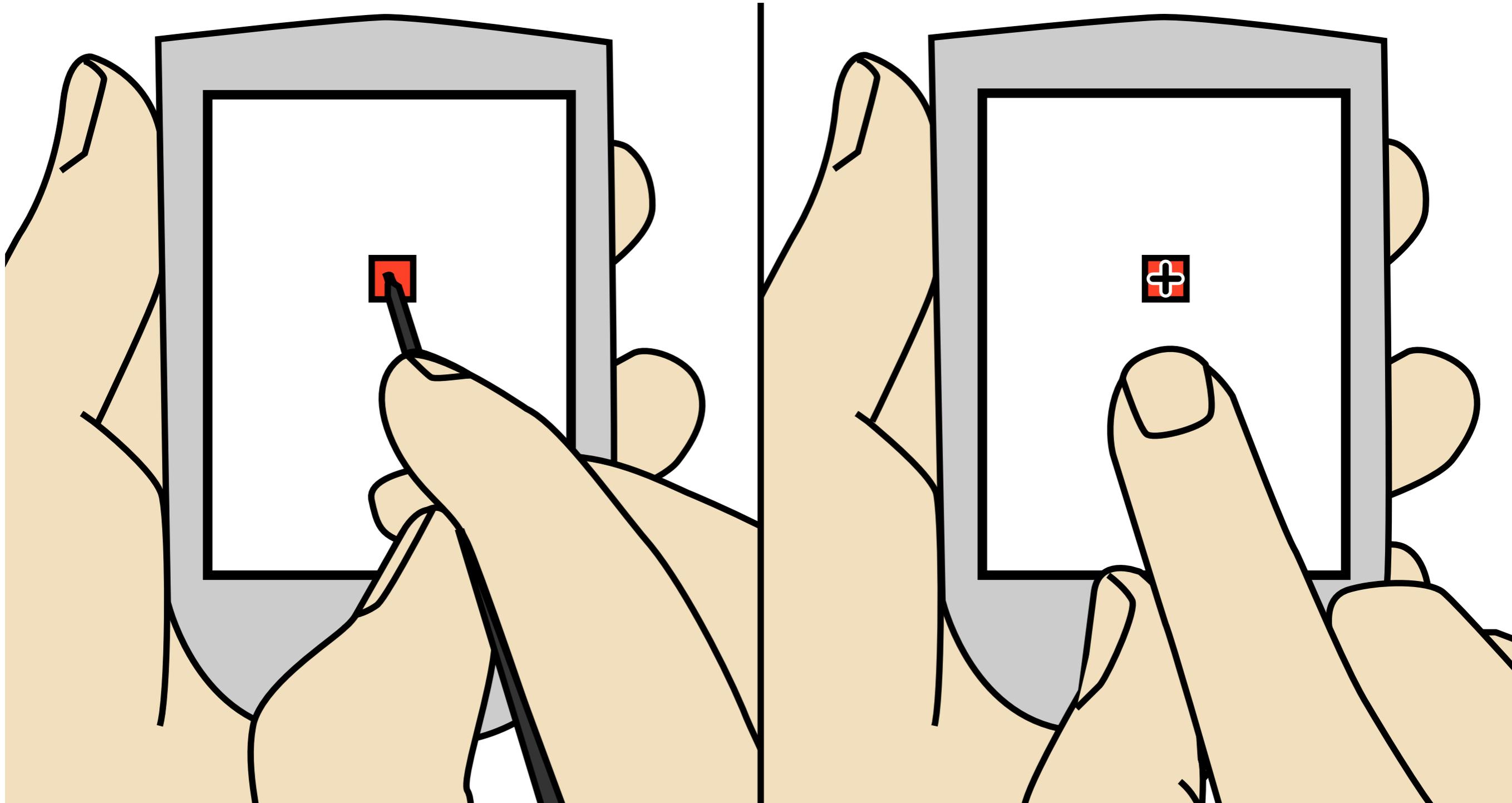
# Problems

*Fat Finger*



# Problems

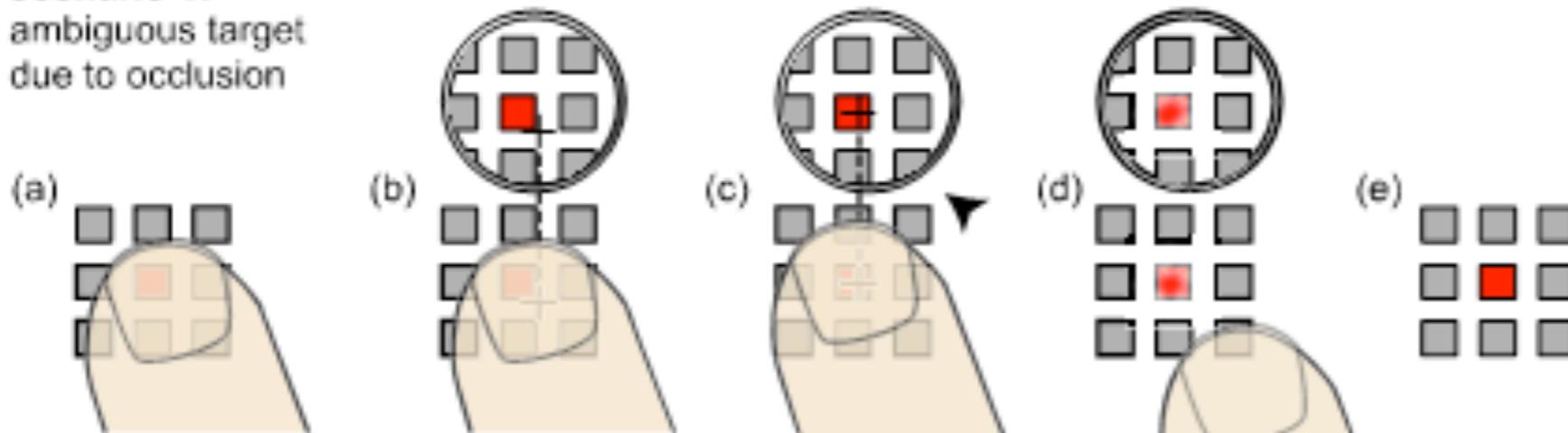
## *Precision*



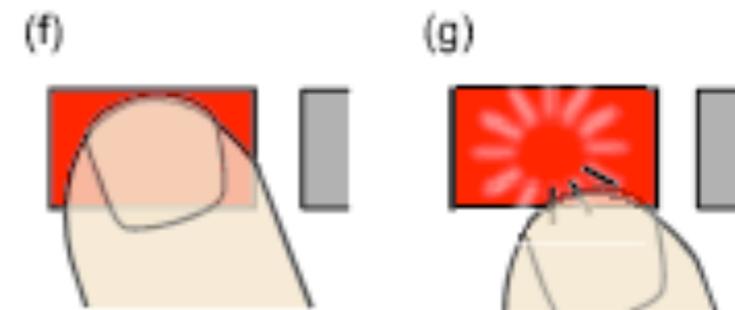
# Shift

*[Vogel et al. 2007]*

**scenario 1:**  
ambiguous target  
due to occlusion



**scenario 2:**  
occlusion not a  
problem



# Shift

*[Vogel et al. 2007]*



# Shift

*[Vogel et al. 2007]*



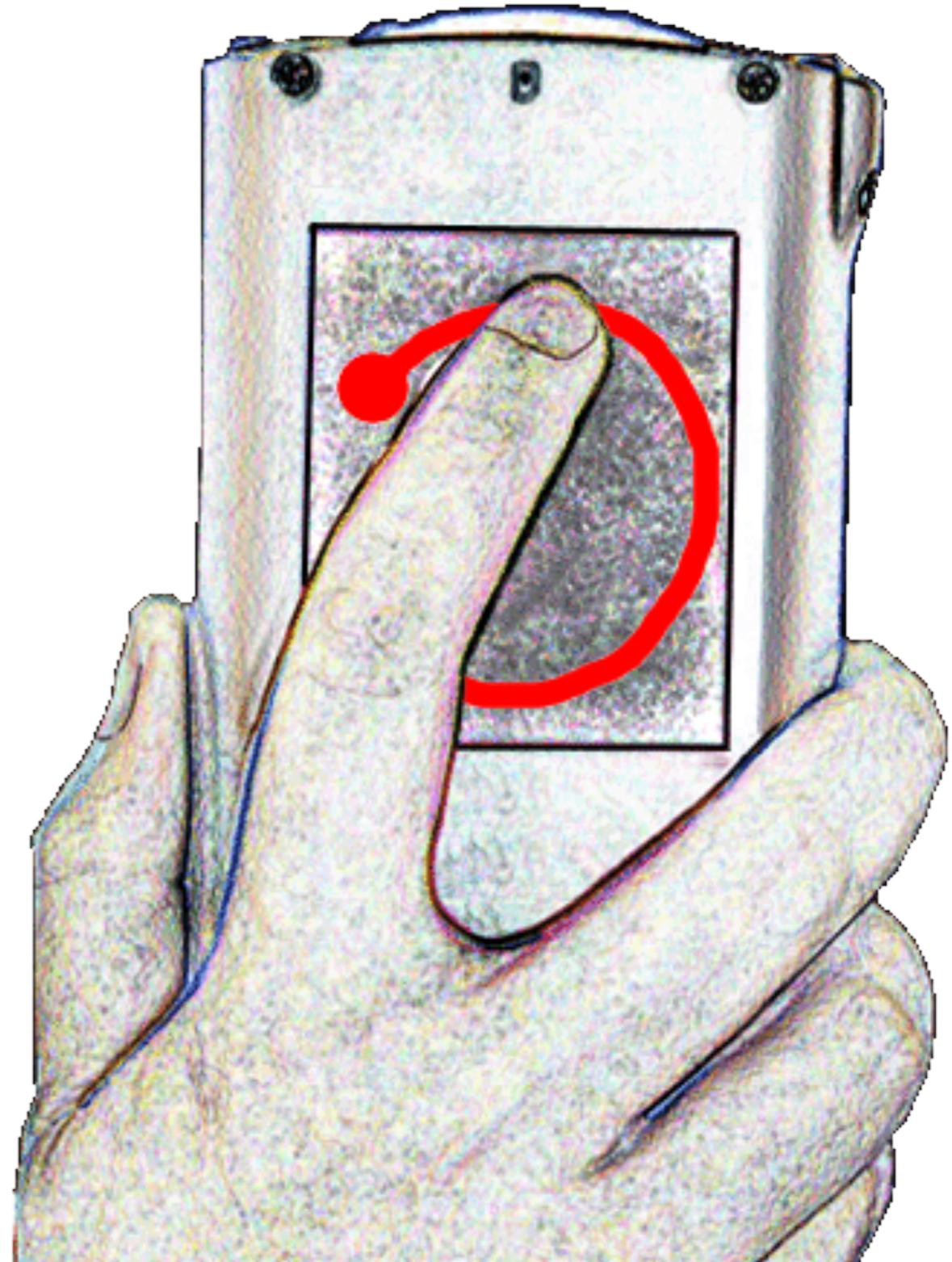
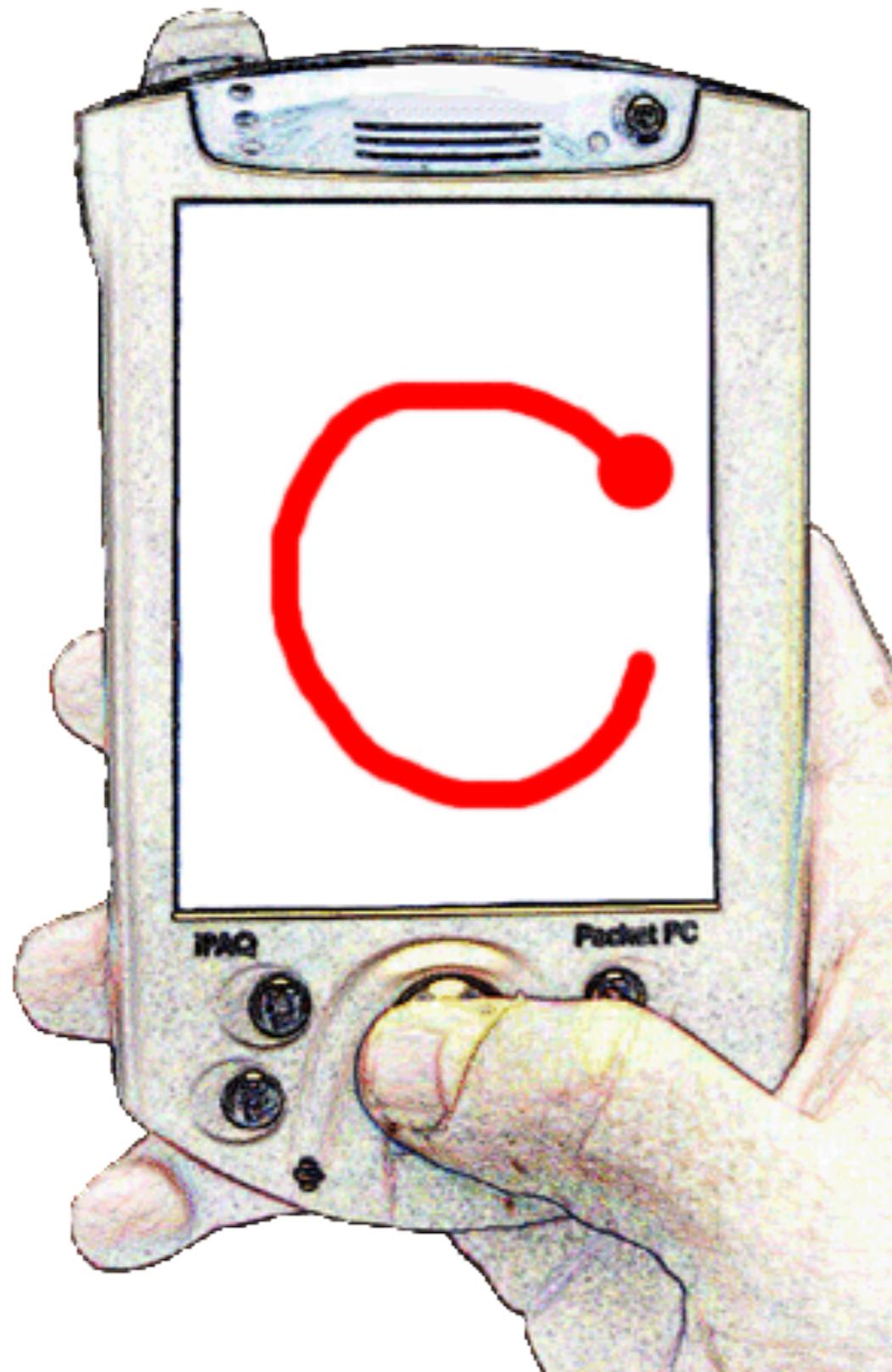
# Behind touch

[Hiraoka et al. 2003]



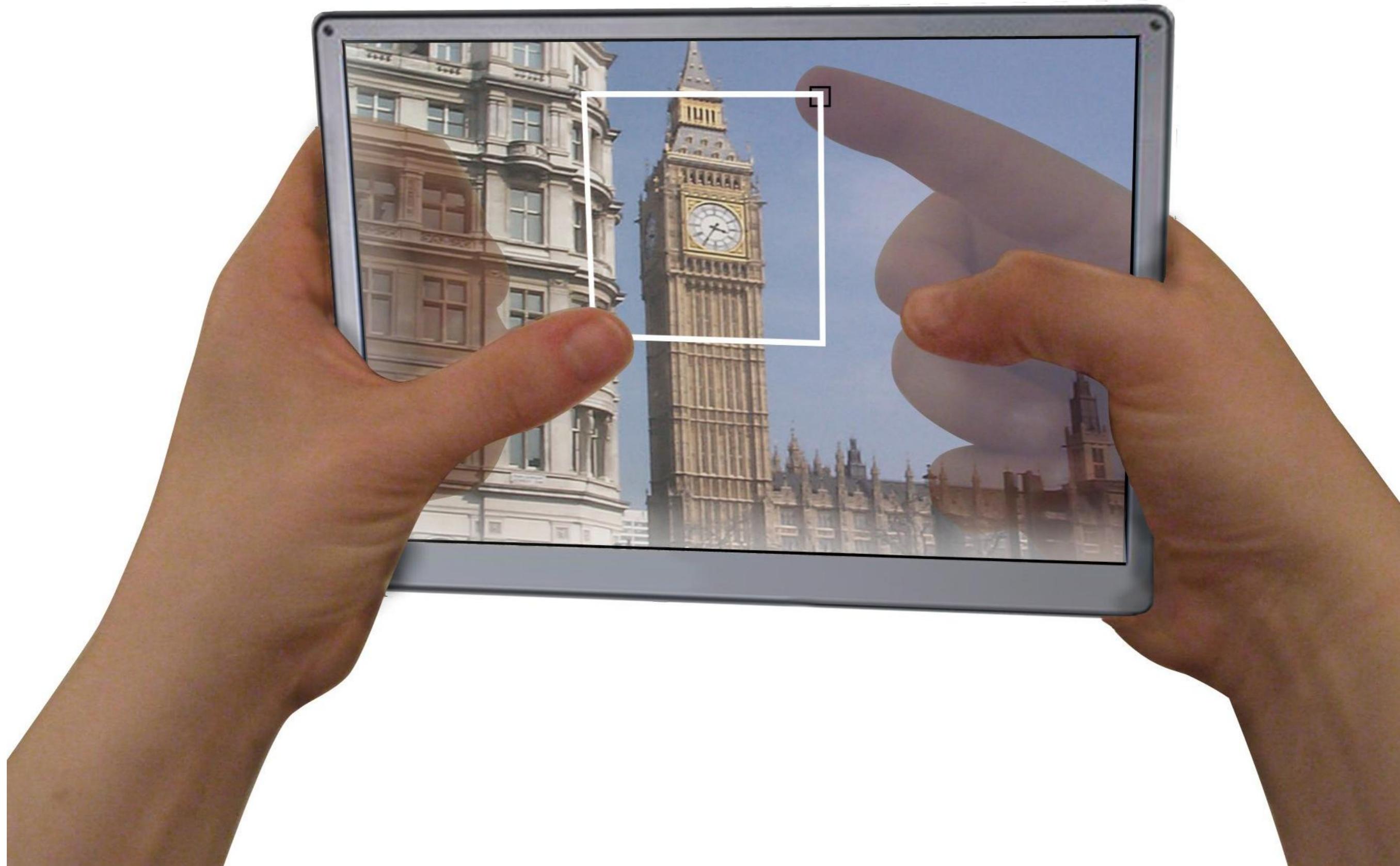
# Behind touch

*[Wigdor et al.]*



# Behind touch

*[Wigdor et al.]*



# Lucid touch

*[Wobbrock et al.]*



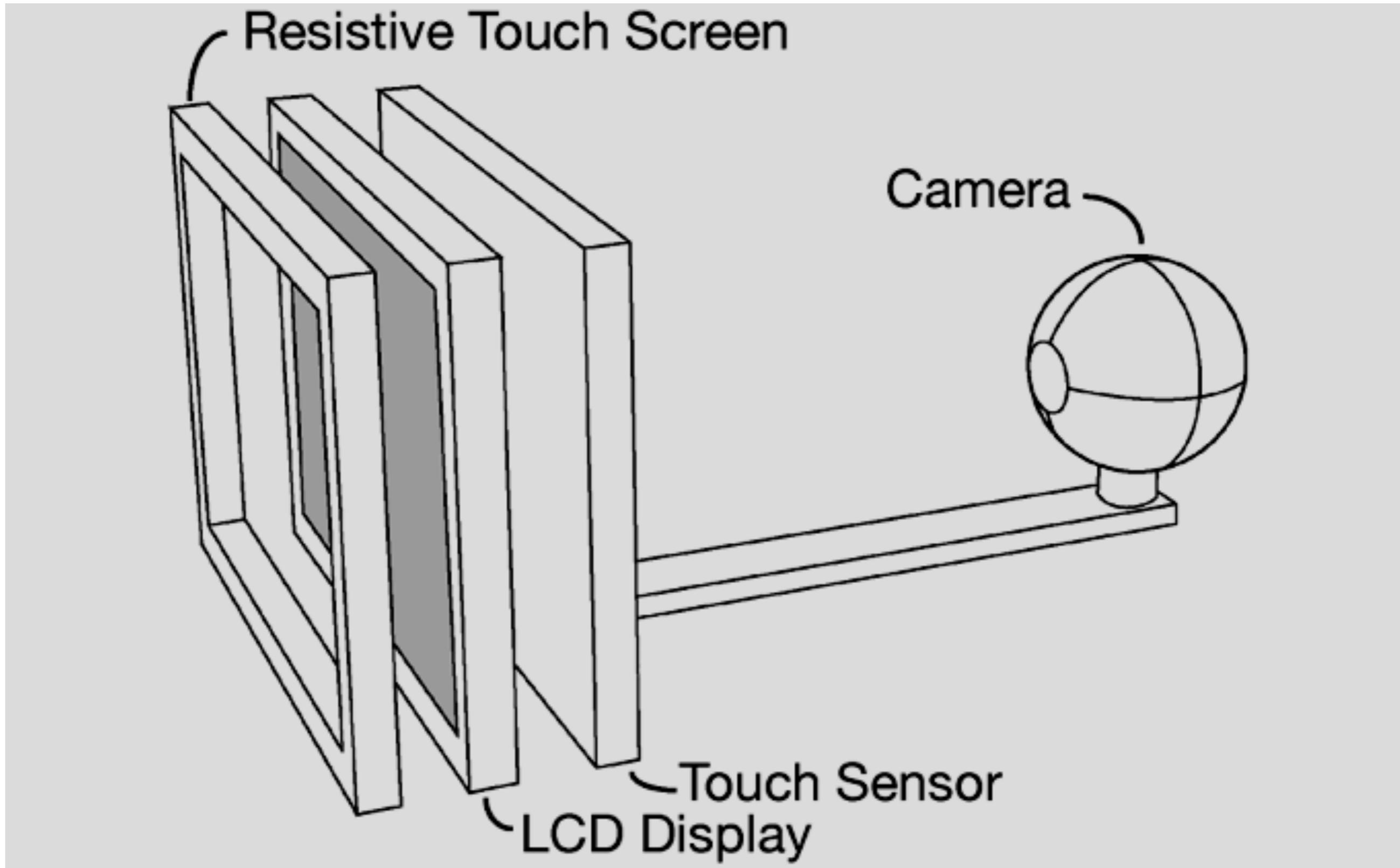
# Lucid touch

*[Wobbrock et al.]*



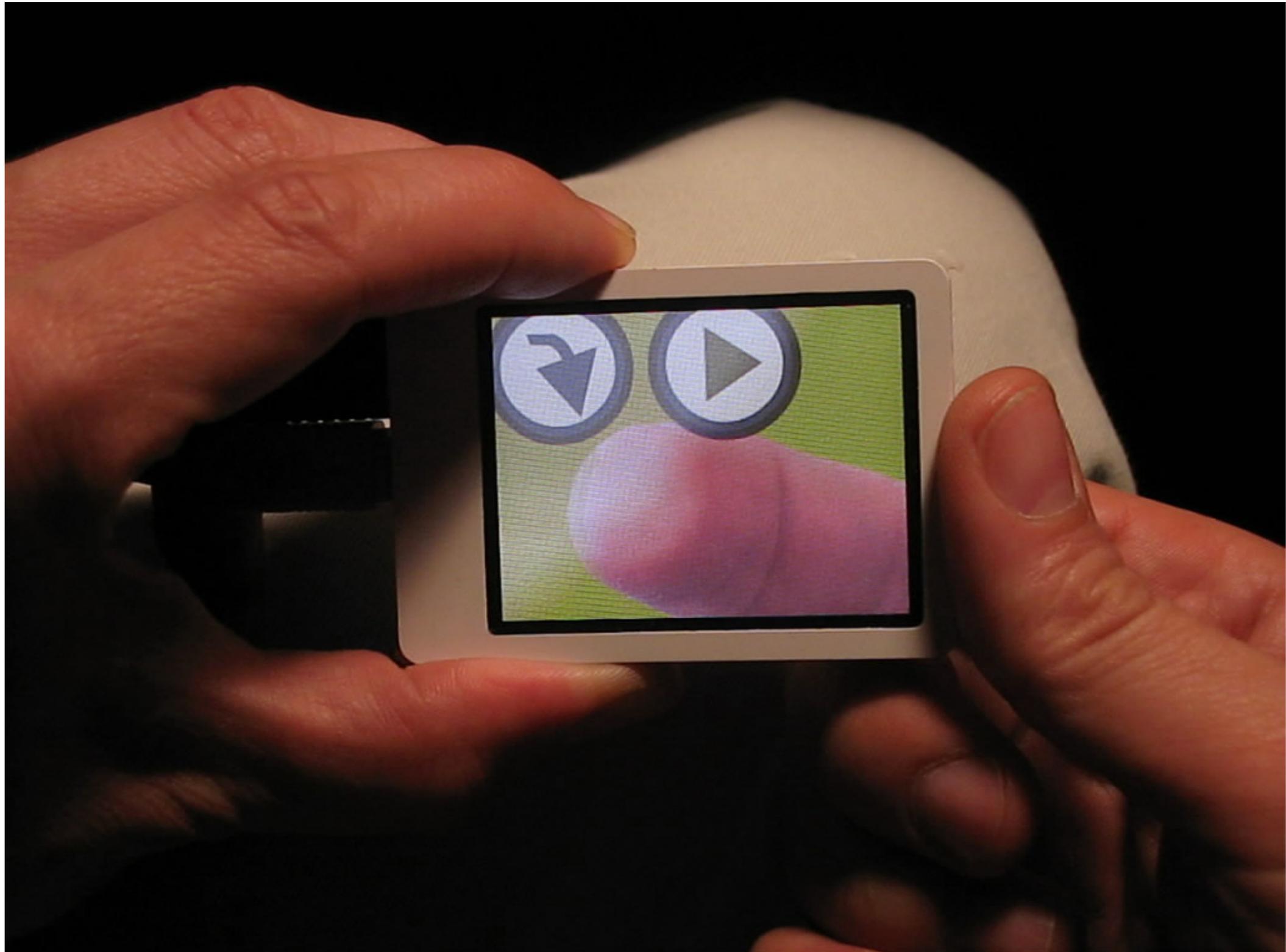
# Lucid touch

*[Wobbrock et al.]*



# Lucid touch 2

*[Baudisch and Chu]*



# Lucid touch 2

*[Baudisch and Chu]*



# Problem

## *Occlusion*

# Occlusion-Aware Interfaces

Daniel Vogel<sup>1,2</sup> and Ravin Balakrishnan<sup>1</sup>

<sup>1</sup>Dept. of Computer Science  
University of Toronto, CANADA

<sup>2</sup>Dept. of Math & Computer Science  
Mount Allison University, CANADA

# Problem

## *Occlusion*

# Occlusion-Aware Interfaces

Daniel Vogel<sup>1,2</sup> and Ravin Balakrishnan<sup>1</sup>

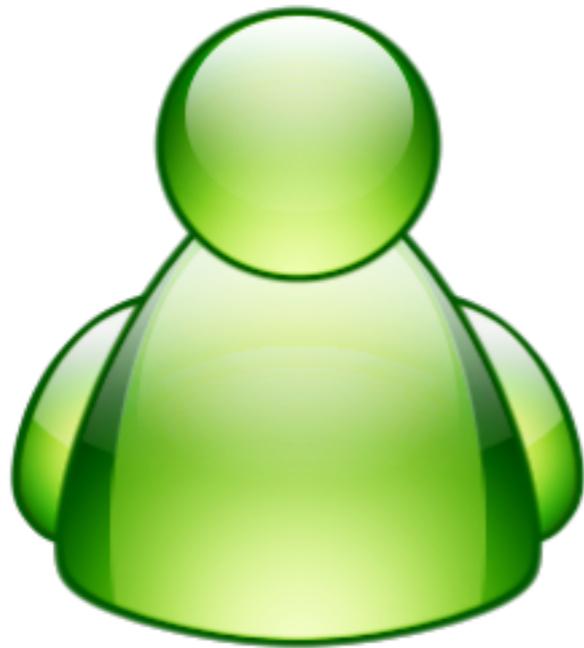
<sup>1</sup>Dept. of Computer Science  
University of Toronto, CANADA

<sup>2</sup>Dept. of Math & Computer Science  
Mount Allison University, CANADA

# Contexts / usages



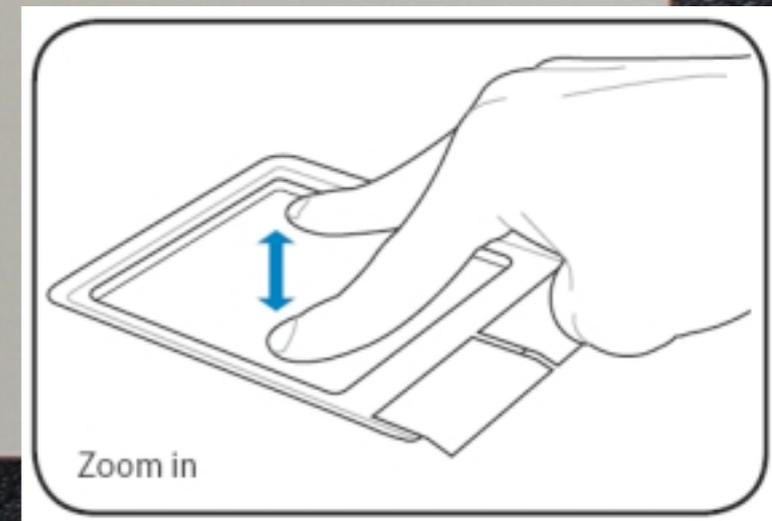
**1 user**



# Smartphone, Tablets



TouchPad:  
multitouch + pressure + Tactile feedback



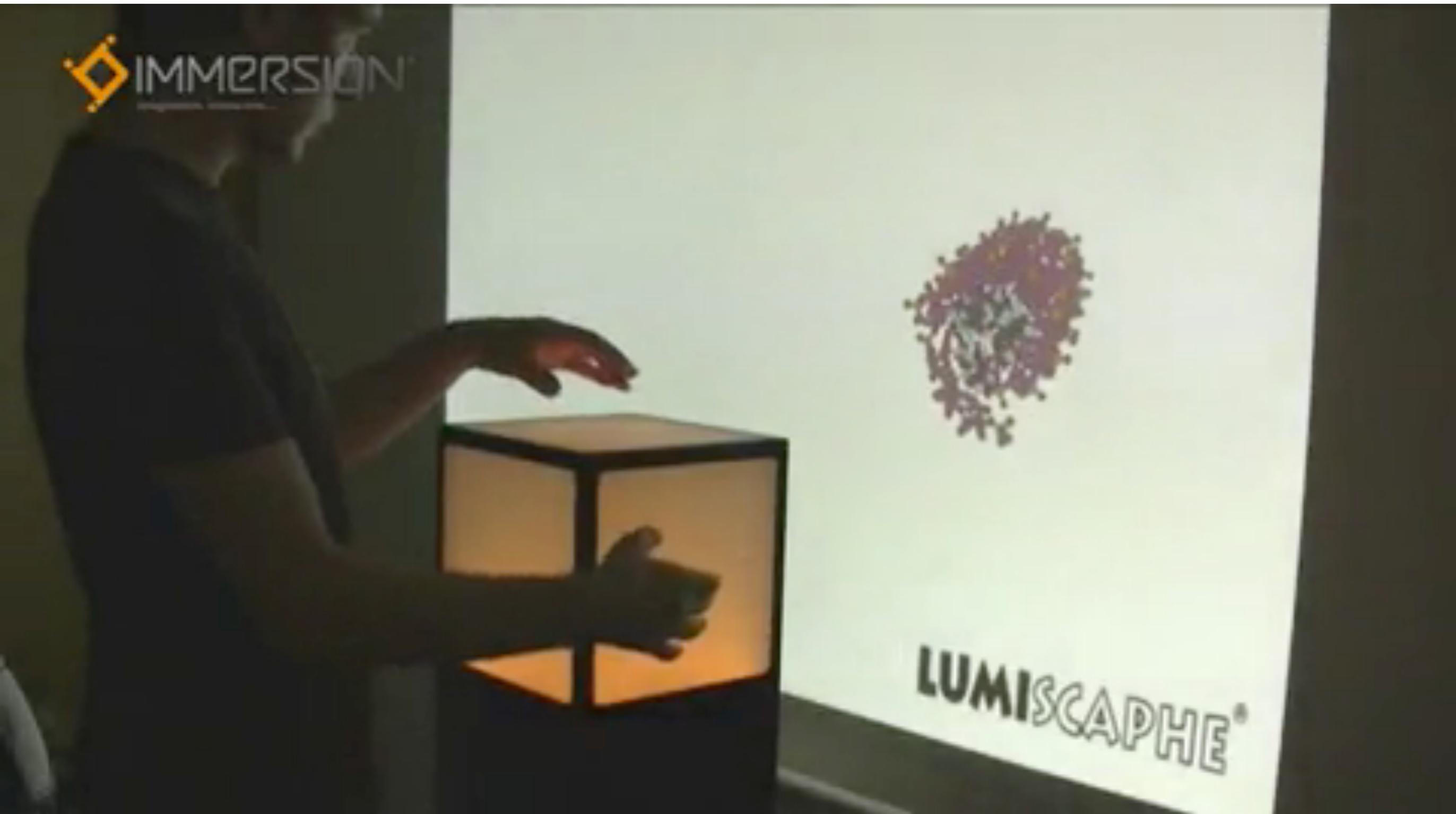
# Touchscreen



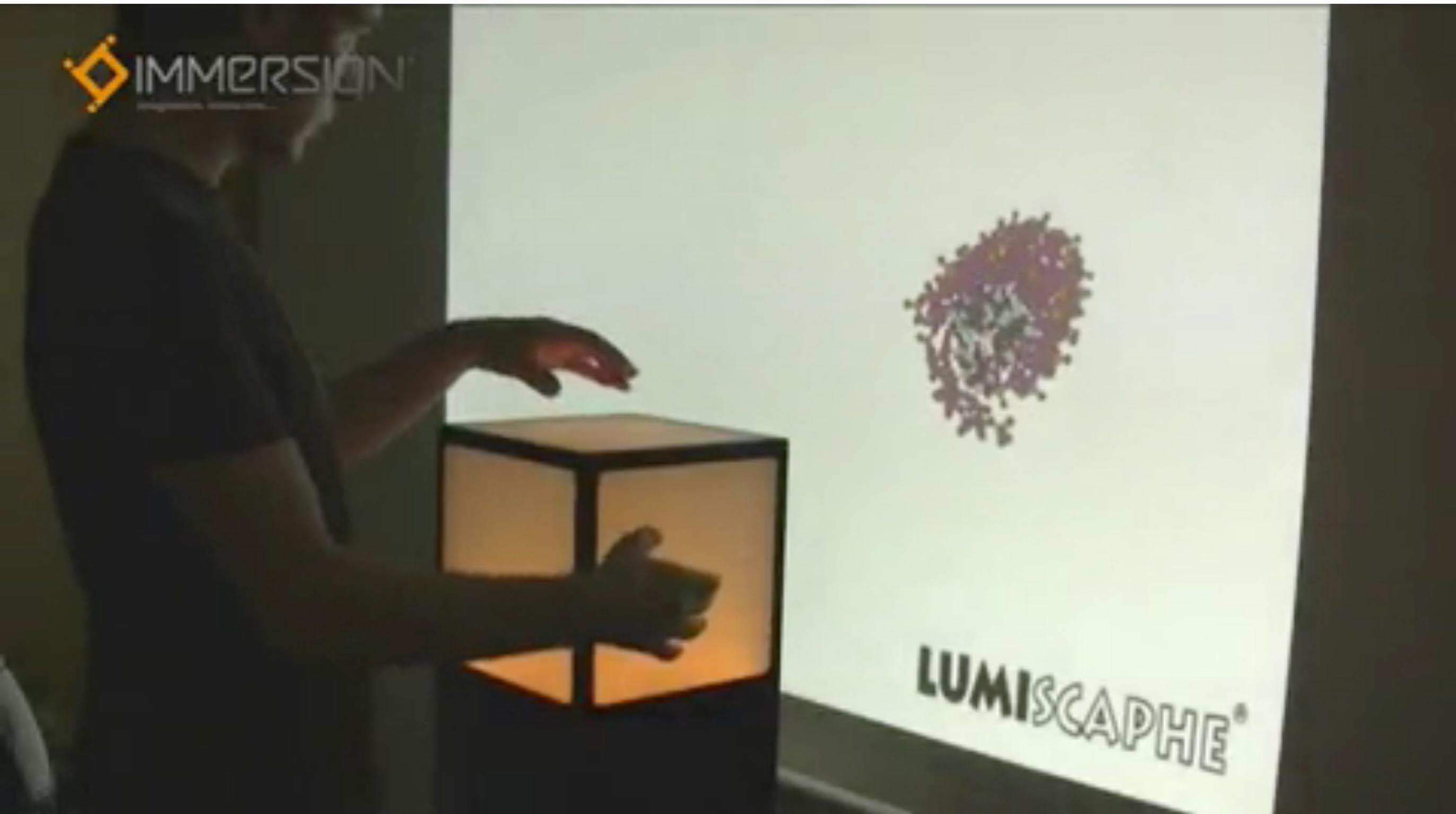
# Mouse



# CubeTile [Immersion]



# CubeTile [Immersion]



Sphere



Microsoft Sphere

# Surfaceless



CAMERA

COLOR MARKERS

PROJECTOR

MIRROR

SixthSense [Mistry and Maes]

GENERAL CENTER  
Times: Morning edition published at 6 a.m., 8:30 a.m., 11 a.m., 2 p.m., 5 p.m., 8 p.m.  
Home: 630 a.m. - 5:30 p.m.  
Business: 7:30 a.m. - 4 p.m.  
Phone: 617-725-1000

## In the news

President-elect Barack Obama will call for about \$100 billion in tax cuts in his inaugural plan, countering Republican worries that he would rely too heavily on new spending. **AZ.**

A suicide attack on Shi'ite Muslim pilgrims killed up to 30 people and wounded 72 in Baghdad in January. **AZ.**

Drama should be abundant this year in the Boston City Council, which must deal with a political campaign, a fiscal crunch, and a member under criminal indictment. **BL.**

A Beth Israel Deaconess urologist helps challenge a long-standing prohibition against giving testosterone to men who have had prostate cancer. **AS.**

Early in Massachusetts golf season, a city initiative to help low-income families get their children into school. **BL.**

Virginia Governor Dean Kuznetsov's Democratic Party campaign strategy. **AZ.**

A company's technology revolutionizes the way it handles drug prescriptions. **BL.**

Parents could have greater control over their children's education if they could change that the state constitution. **AS.**

Medicines that help with depression and anxiety. **AS.**

More to be learned about the impact of the recession on the economy. **AS.**

As rich rivals cut back, small colleges sell stability. **AS.**

Rely on tuition, not endowment. **AS.**



FOR THE PROJECT PURPOSE ONLY  
Smoke rose as Israeli infantry soldiers walked into Gaza yesterday. The battles so far have been outside urban areas.

## Israelis split Gaza in two amid calls for a cease-fire

By Ethan Bronner  
NEW YORK TIMES

ON THE ISRAELI-GAZA BORDER — Israeli soldiers split the Gaza Strip into two parts yesterday, a move that drew criticism from both sides.

ground combat appeared to have been comparatively restrained. Hamas, the Islamist rulers of Gaza, had warned that Israeli soldiers would be killed if they entered the territory.

Israeli soldiers said they were not sure if the move would bring a cease-fire. Hamas leaders said they would not accept the move unless it was part of a broader agreement.



Jumbo

## Obama Cabinet nominee pulls out

Contract in... bogs down R...

First bump in process for president-elect

Richardson Lammie, Obama's pick for commerce secretary, has withdrawn from consideration. The move represented the first public snag in Obama's attempt to assemble his Cabinet.

Richardson denied wrongdoing but said the investigation would probably remain unresolved until well after Obama's inauguration and he didn't want to disrupt the new administration.

"I am not sure that I and my staff have acted properly in all matters and that this investigation will bear out that fact," Richardson said in a statement released by Obama's transition team. "But I have concluded that the investigation also would have served an important purpose in the construction process."

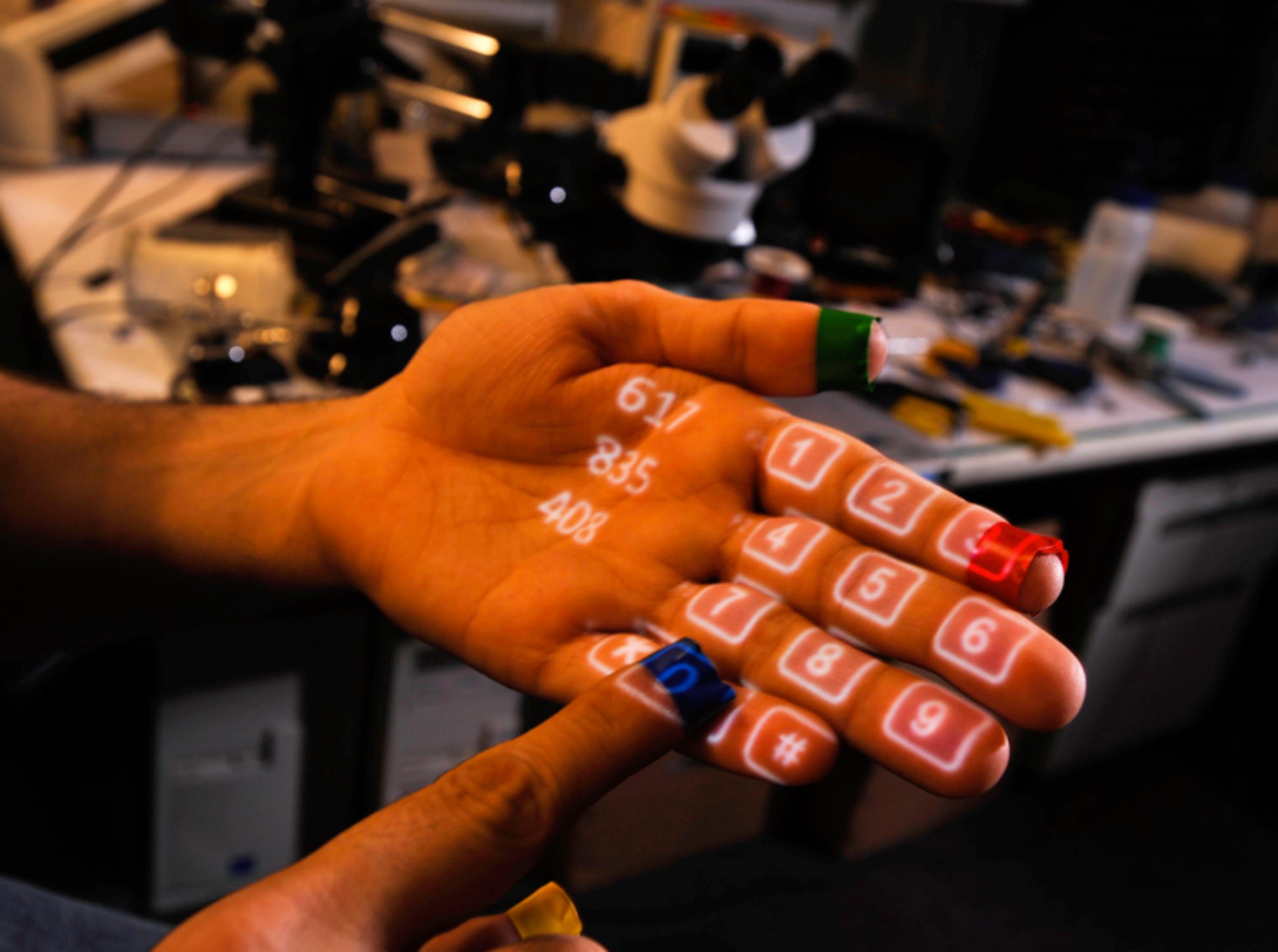
Obama had tapped Richardson for the position. **Page A12**

## Church struggles to keep its voice

Christ...



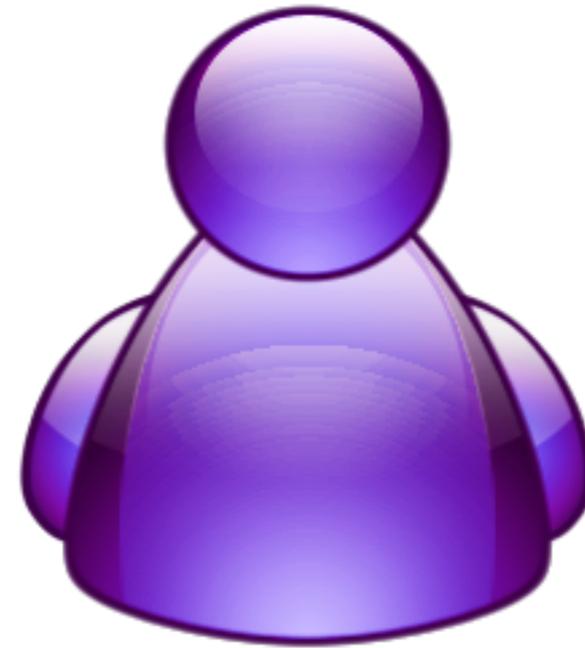
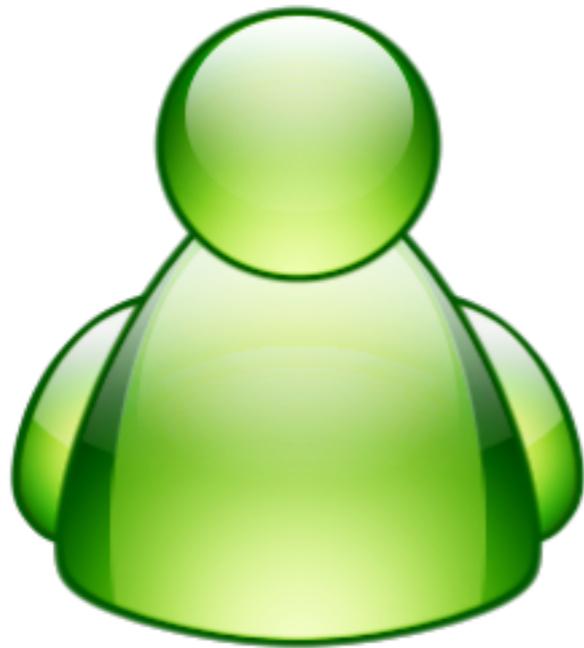




617  
835  
408

1 2 3  
4 5 6  
7 8 9  
\* 0 #

**2 users**





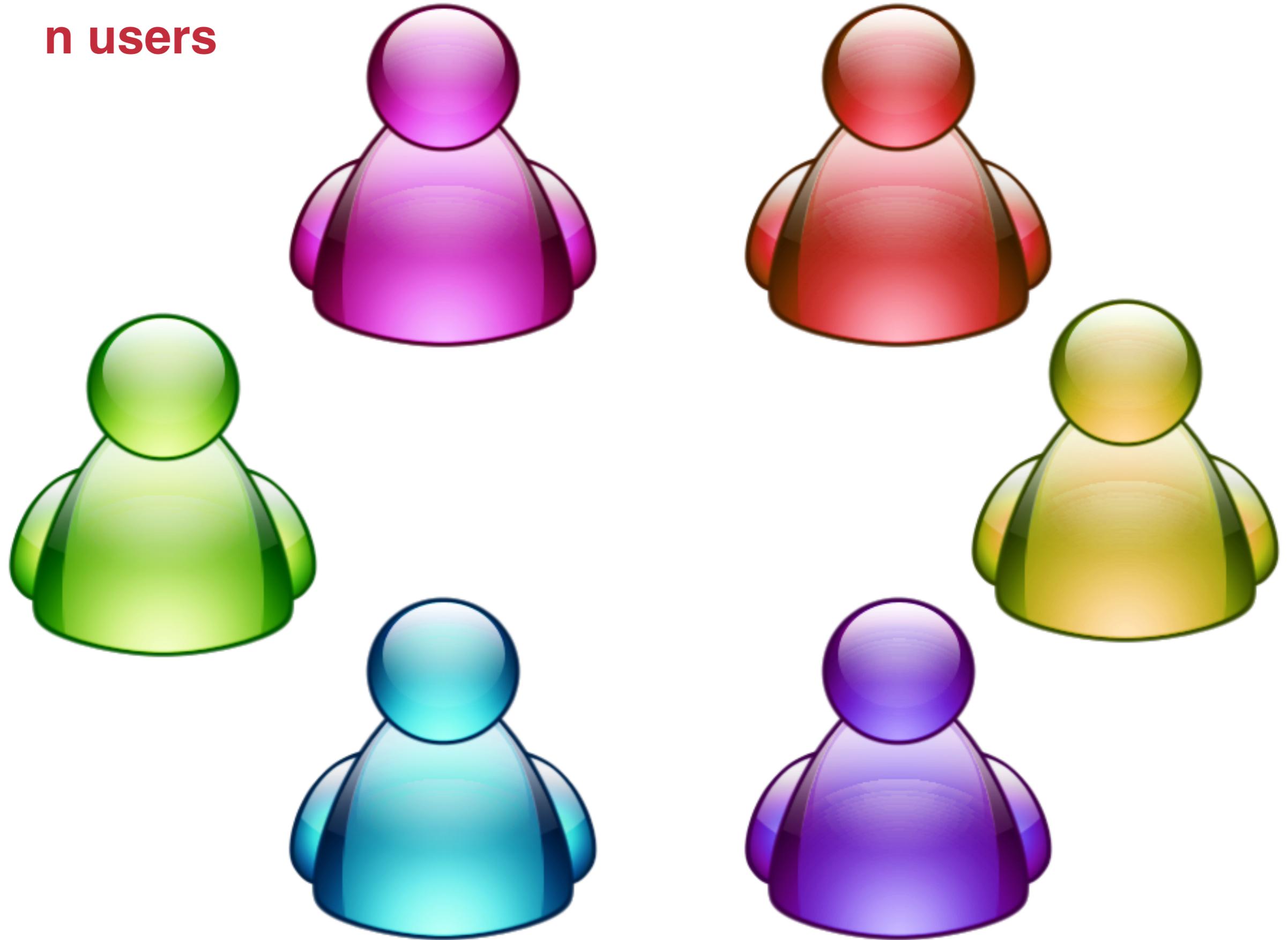


# Coffee Table



Microsoft Surface

**n users**



# Tabletop





# TableTop

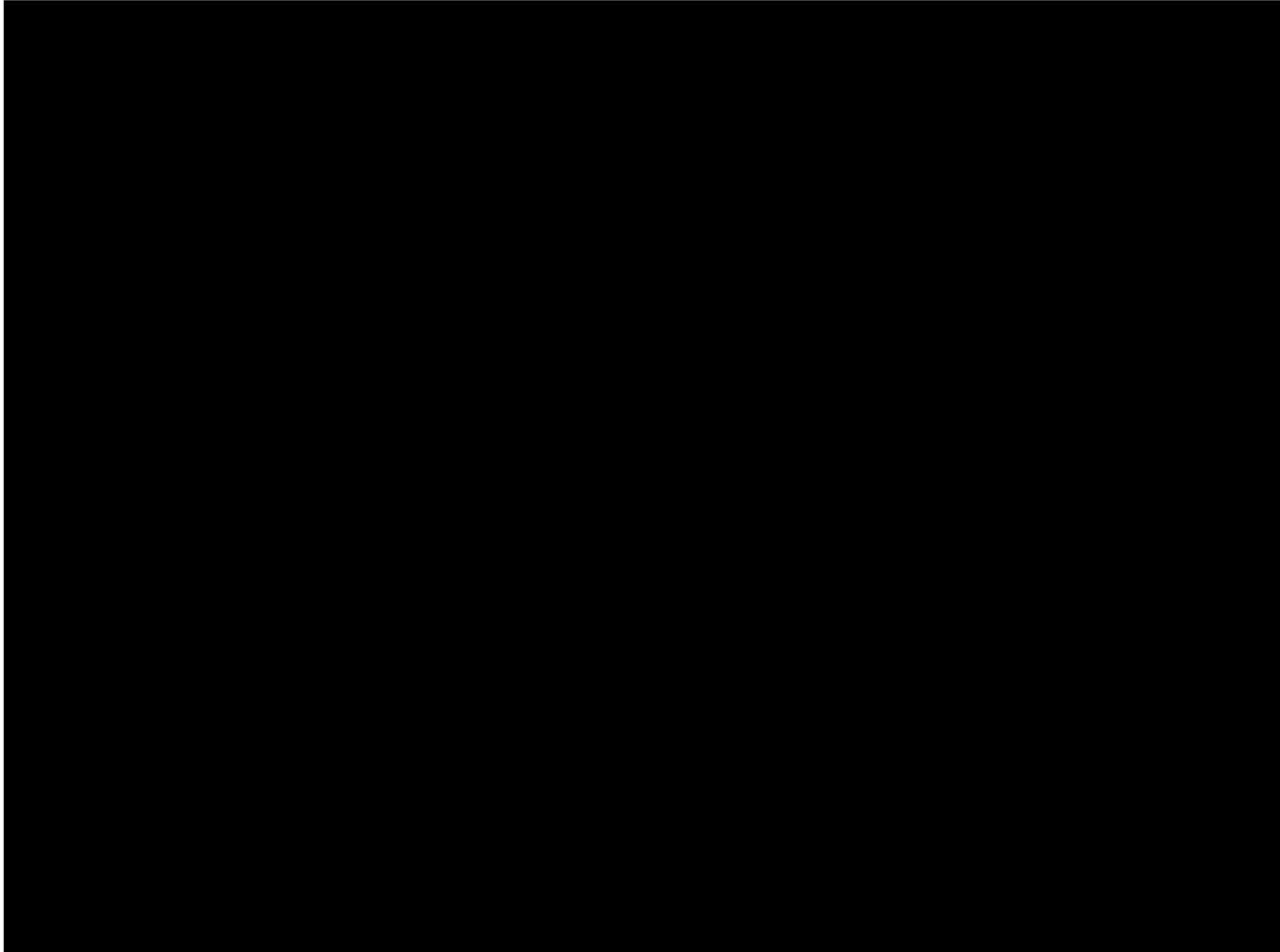
*Reactable*



<http://reactable.com/>

# TableTop

*Reactable*



<http://reactable.com/>

# Interactive wall displays



# Interactive wall displays

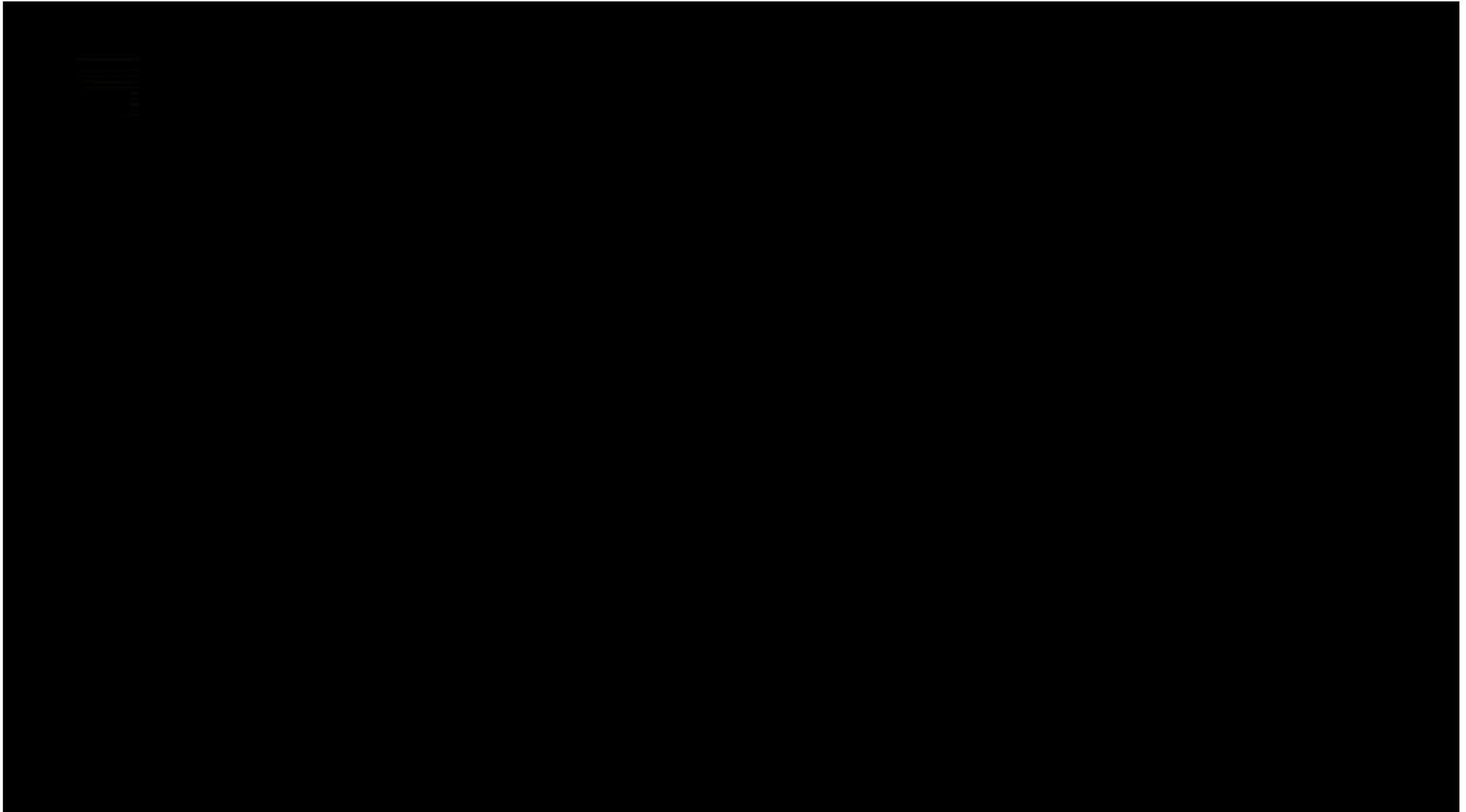


# Interactive floor



# Interactive Floor

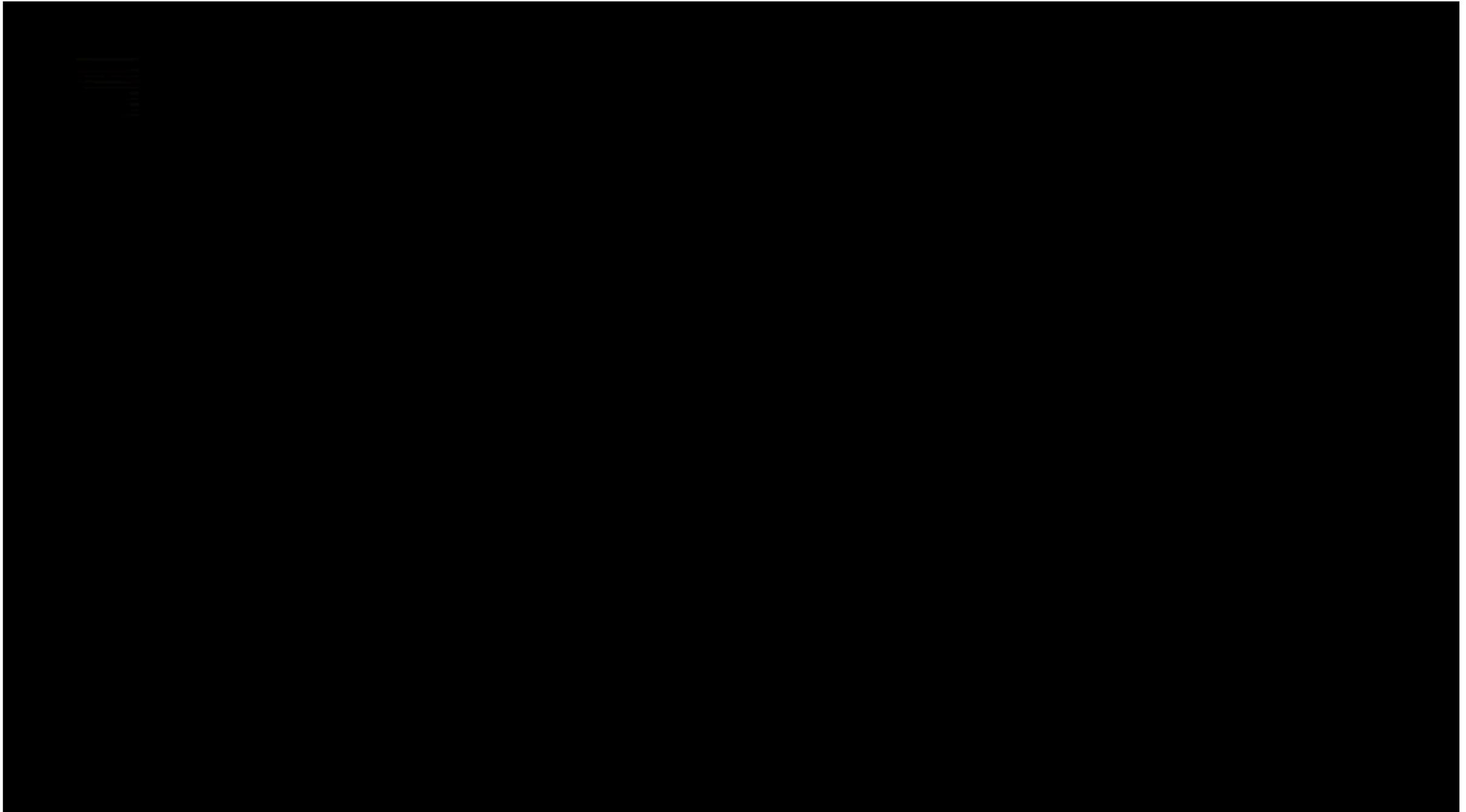
*Multitoe [Fetzer et al.]*



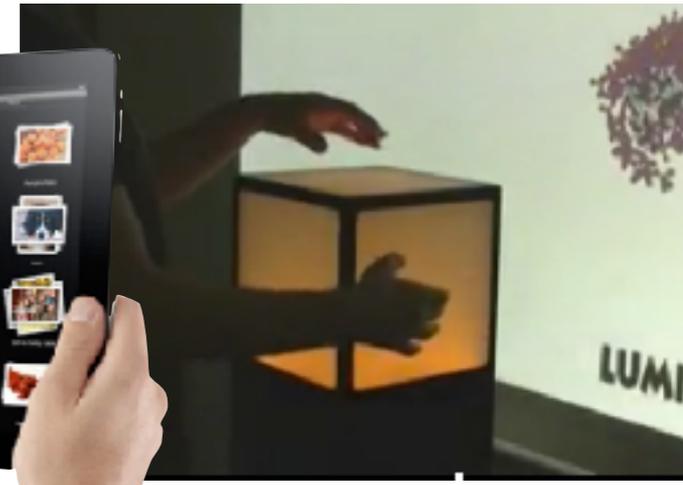
<https://hpi.de/baudisch/projects/multitoe.html>

# Interactive Floor

*Multitoe [Fetzer et al.]*



<https://hpi.de/baudisch/projects/multitoe.html>



# Applications

# Smart Home

*CRISTAL*



## Living Room

TV

Speakers

Lights

Vacuum Cleaner

Digital

Picture Frame

# Smart Home

*CRISTAL*



## Living Room

TV

Speakers

Lights

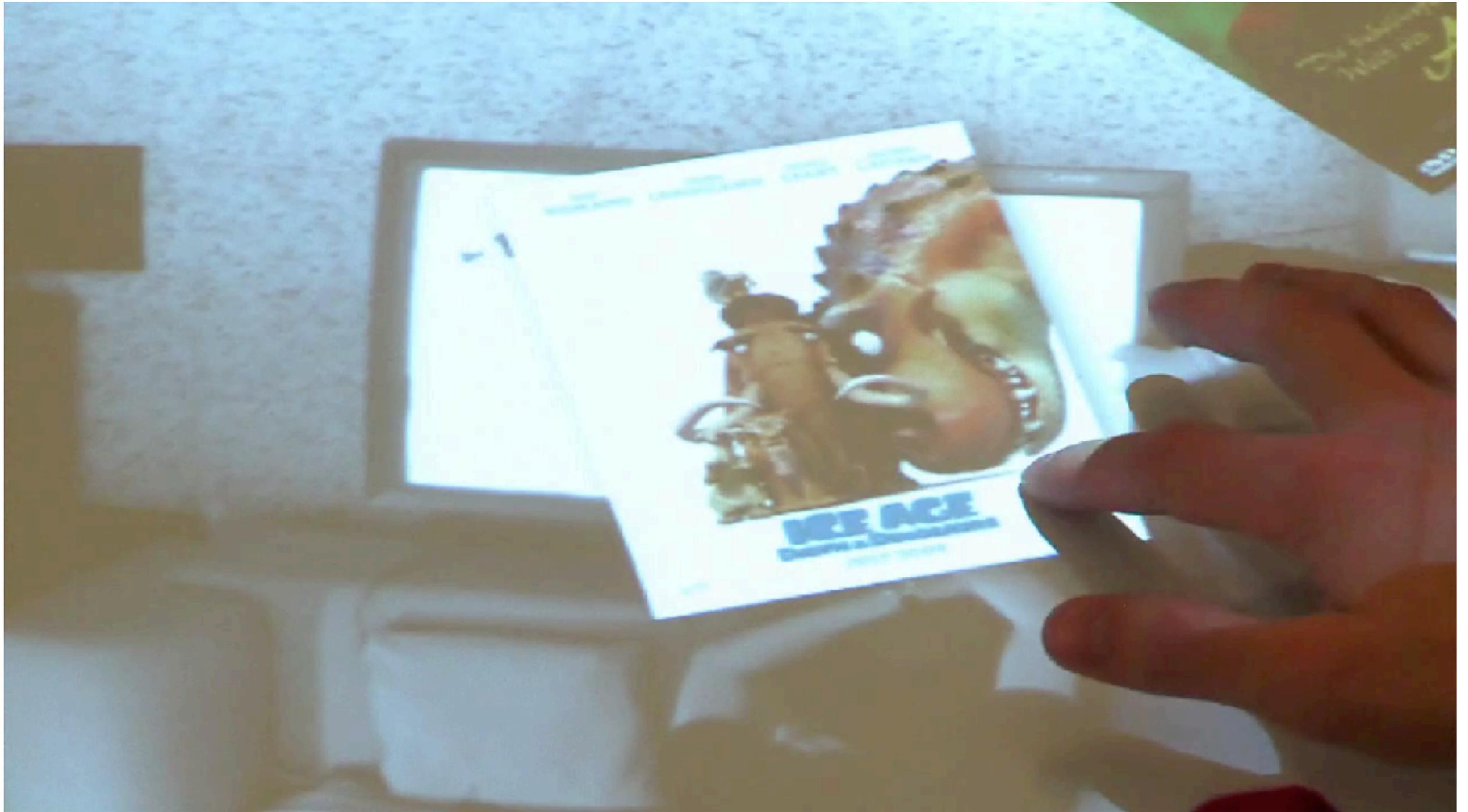
Vacuum Cleaner

Digital

Picture Frame

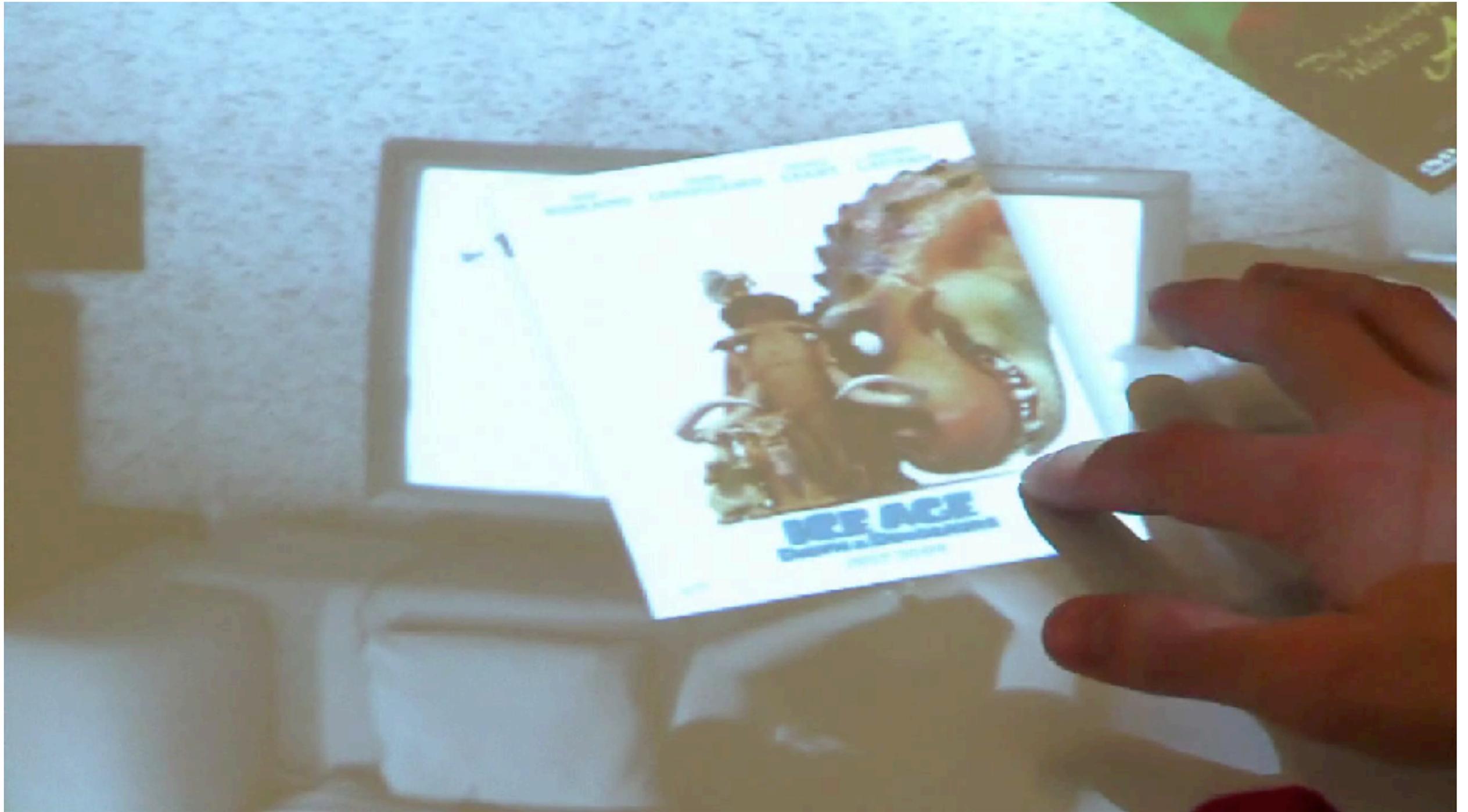
# Smart Home

*CRISTAL*



# Smart Home

*CRISTAL*



# Museums / Expositions



Fiction



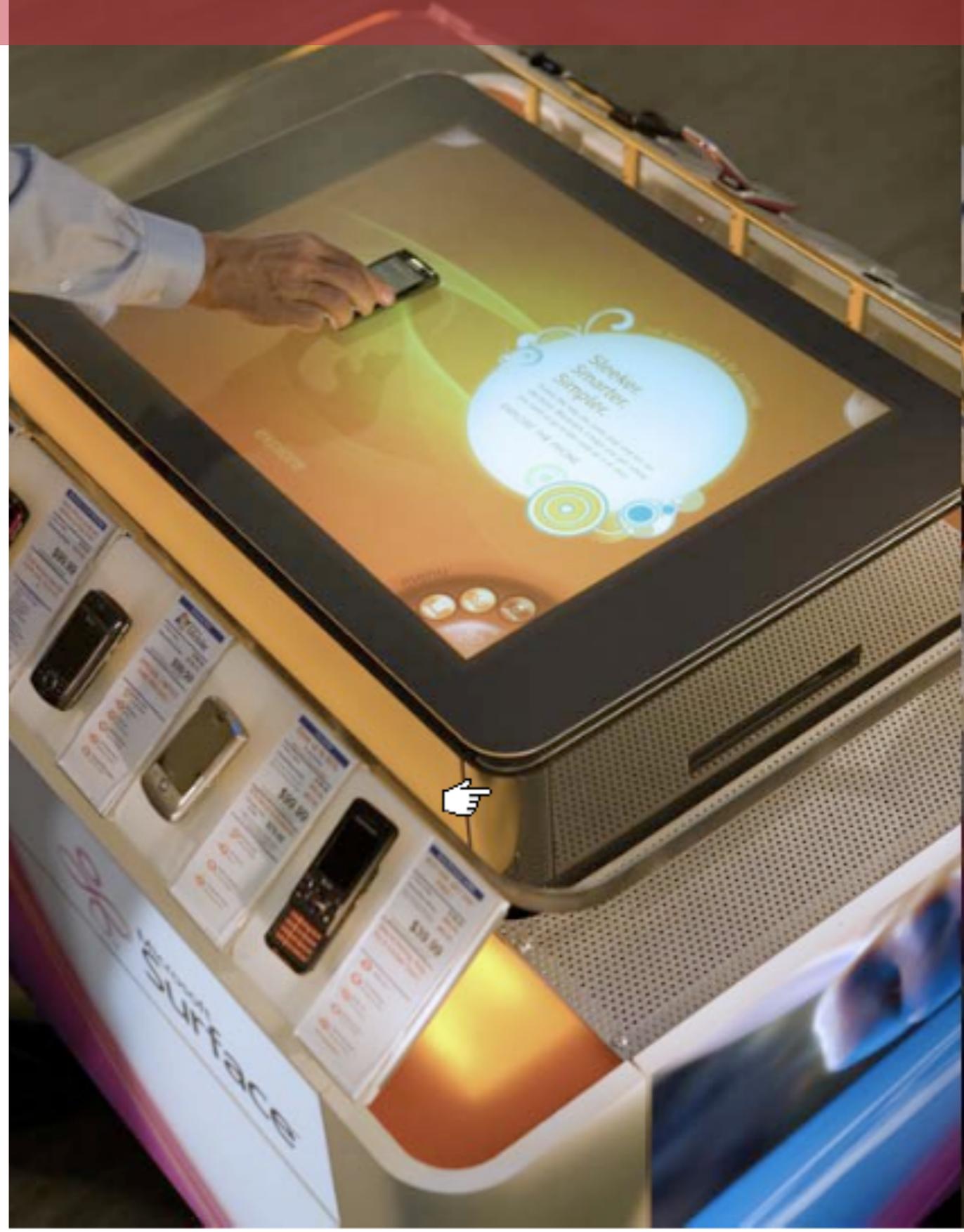
# Gaming



# Bars



# Shops







# Situation room



Music



*Le Monde Numérique*

# Music



# Digital art



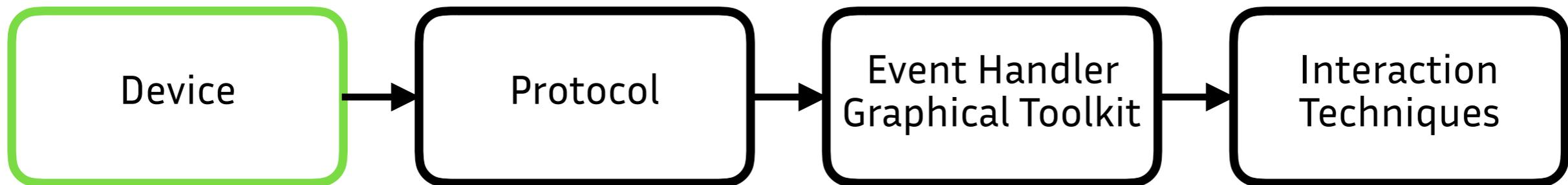
SandCanvas - <https://www.youtube.com/watch?v=NQ9FERXWWsQ>

# Digital art



SandCanvas - <https://www.youtube.com/watch?v=NQ9FERXWWsQ>

# Multitouch pipeline



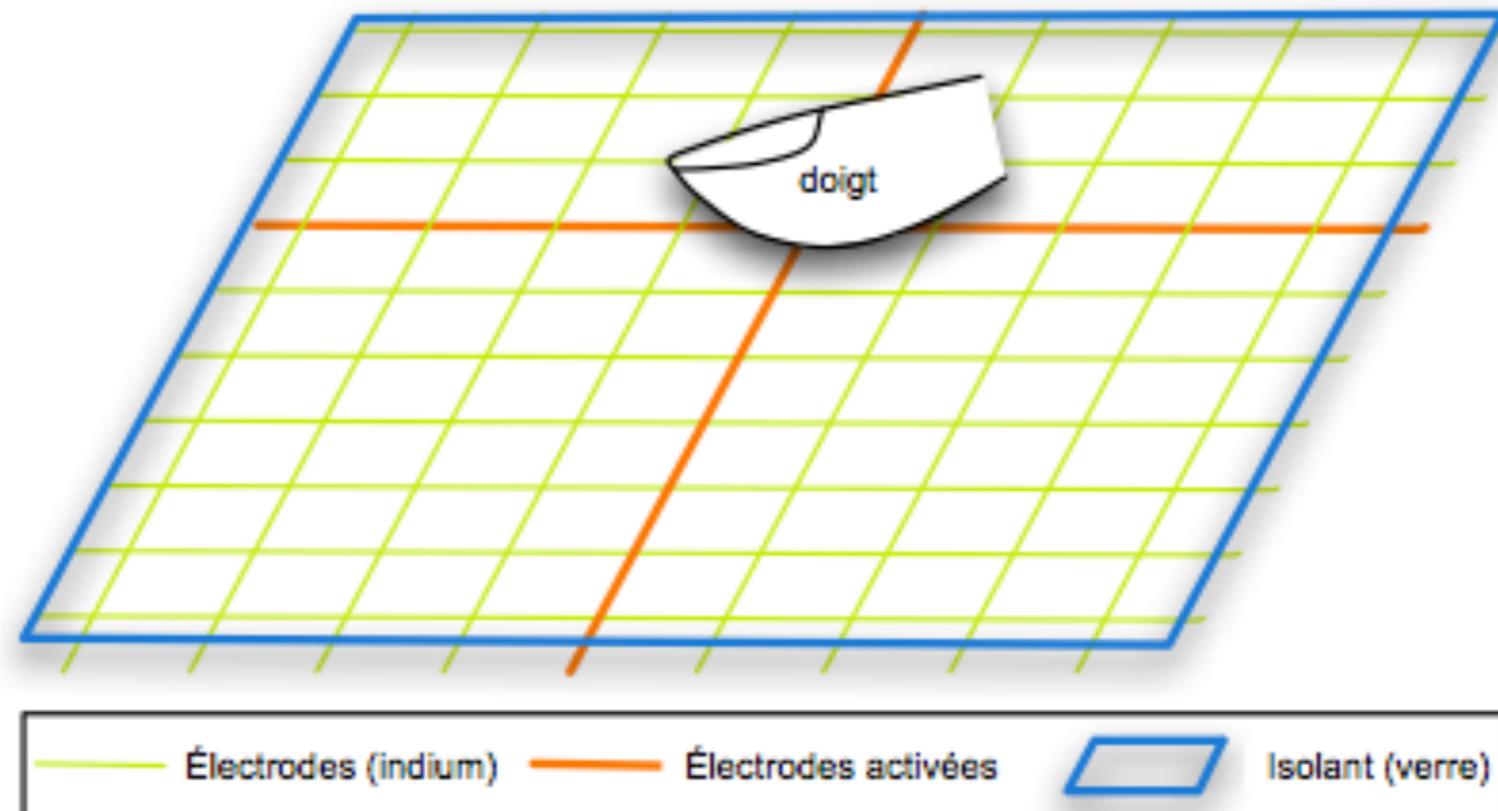
# Technologies

Acoustique

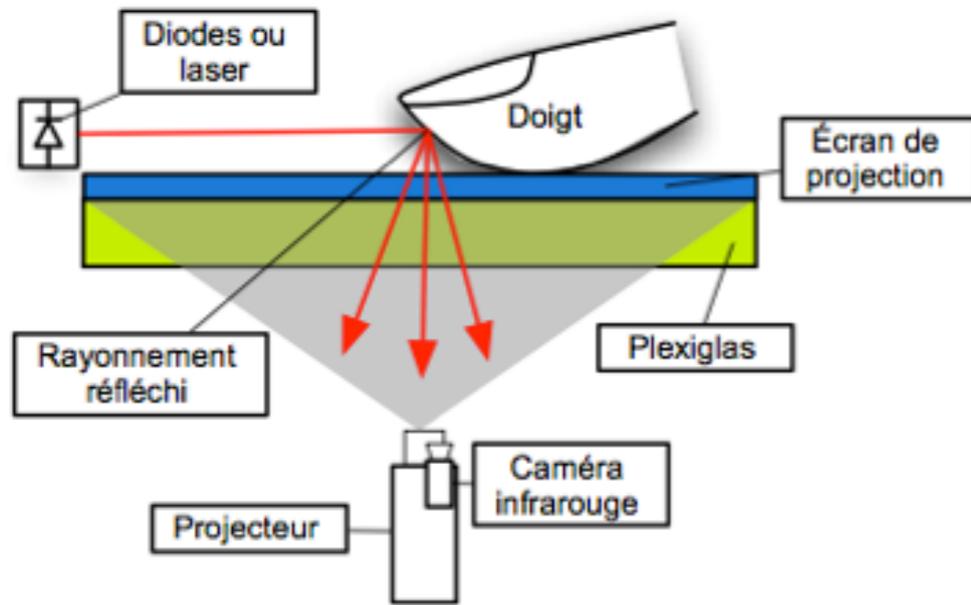
Résistive

Capacitive

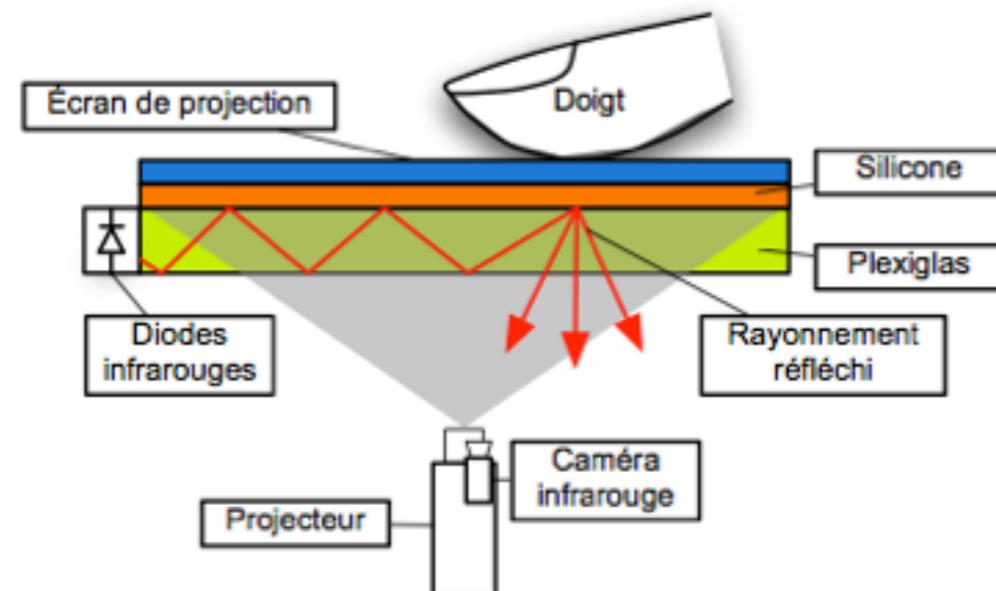
Optique



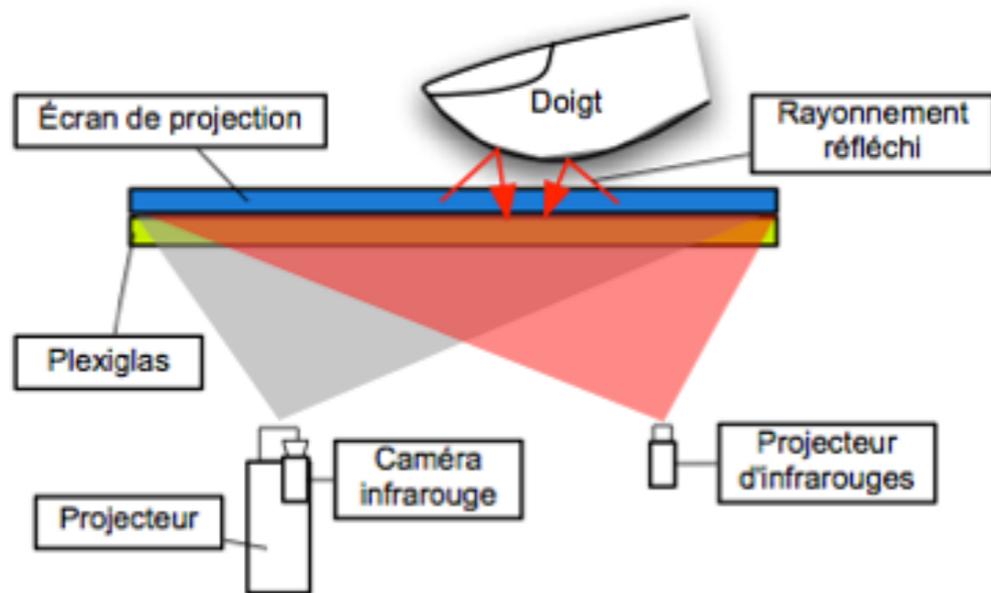
# Technologie optique



(a) *Occlusion Sensing.*



(b) *FTIR.*

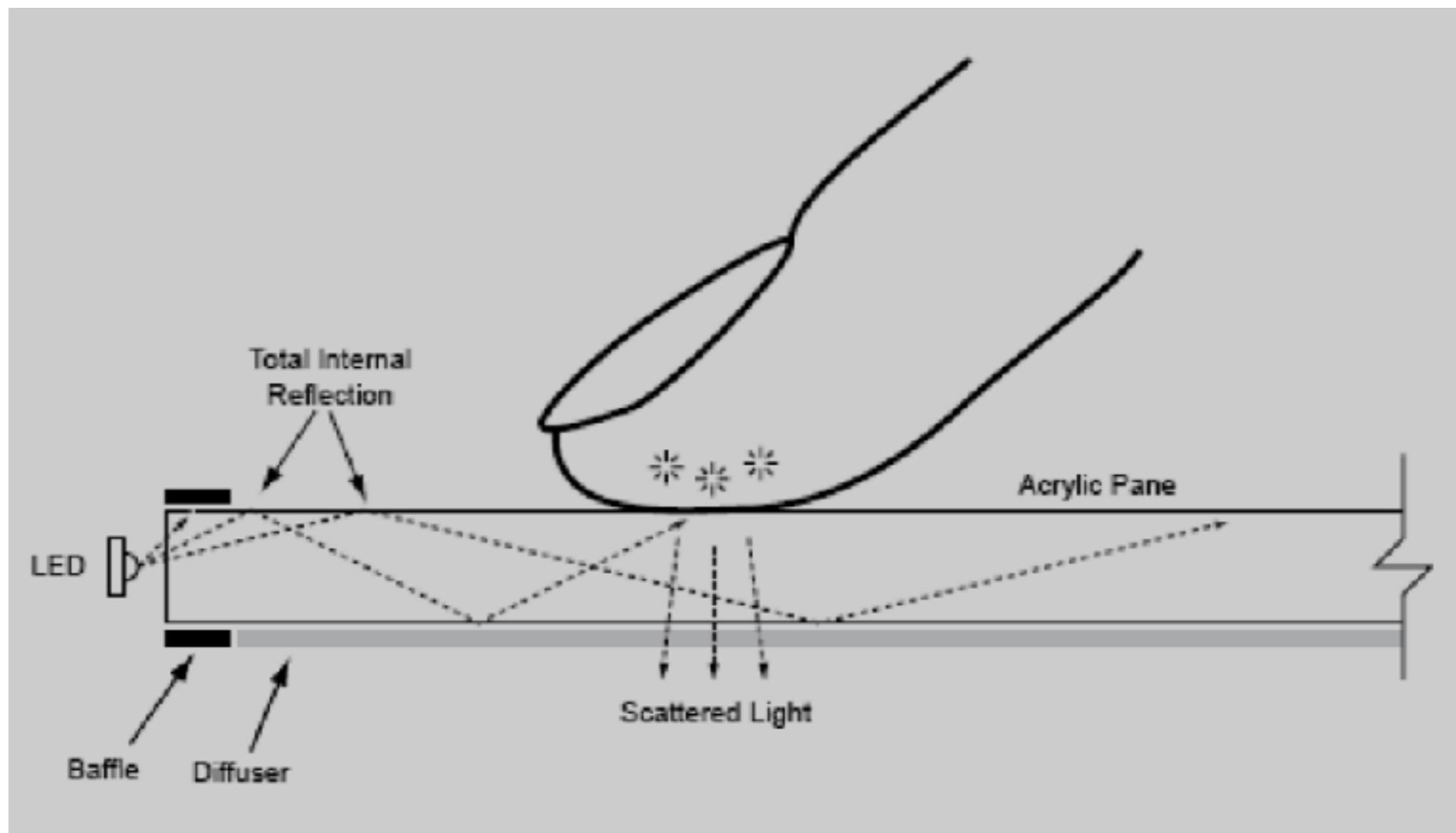


(c) *DI.*



(d) *ThinSight.*

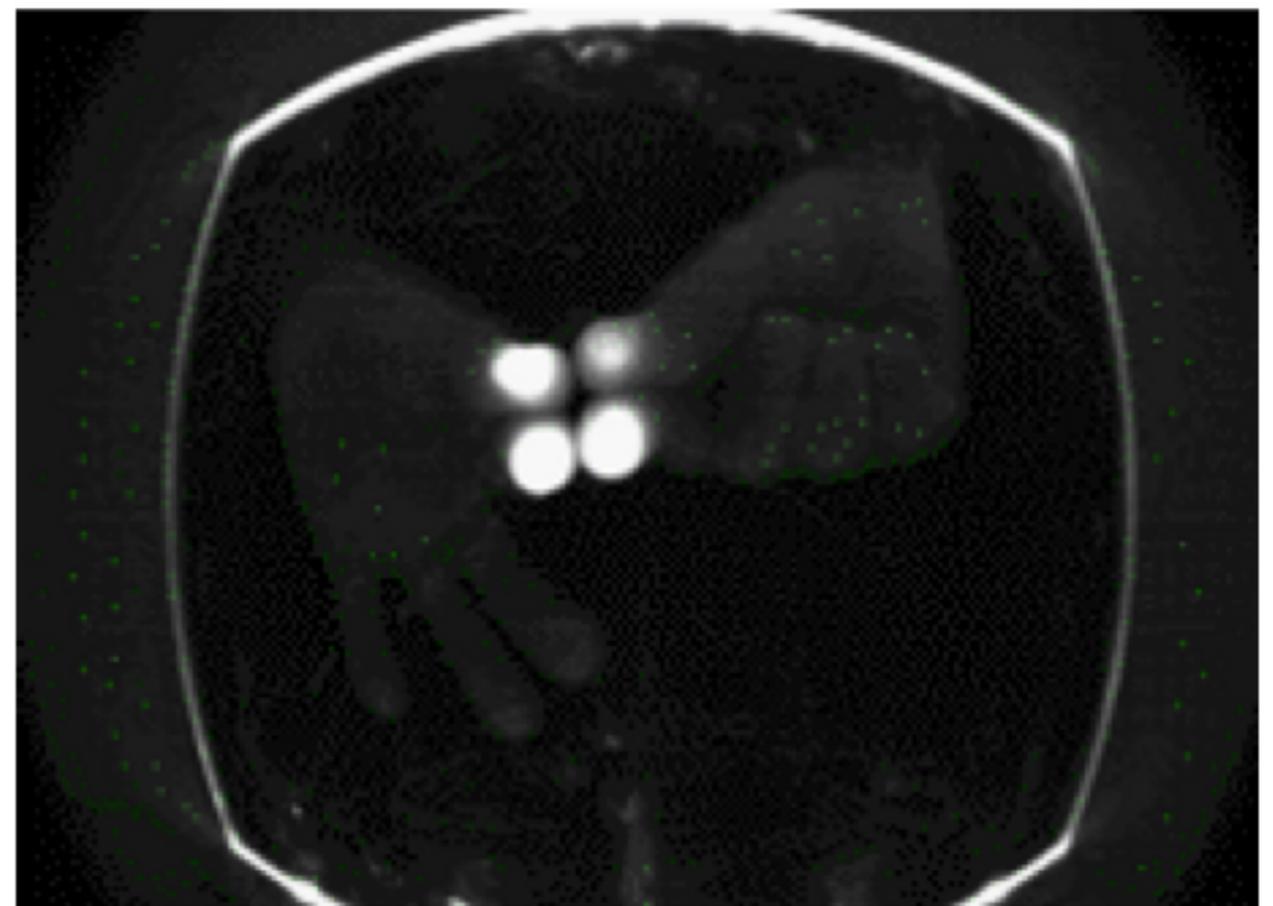
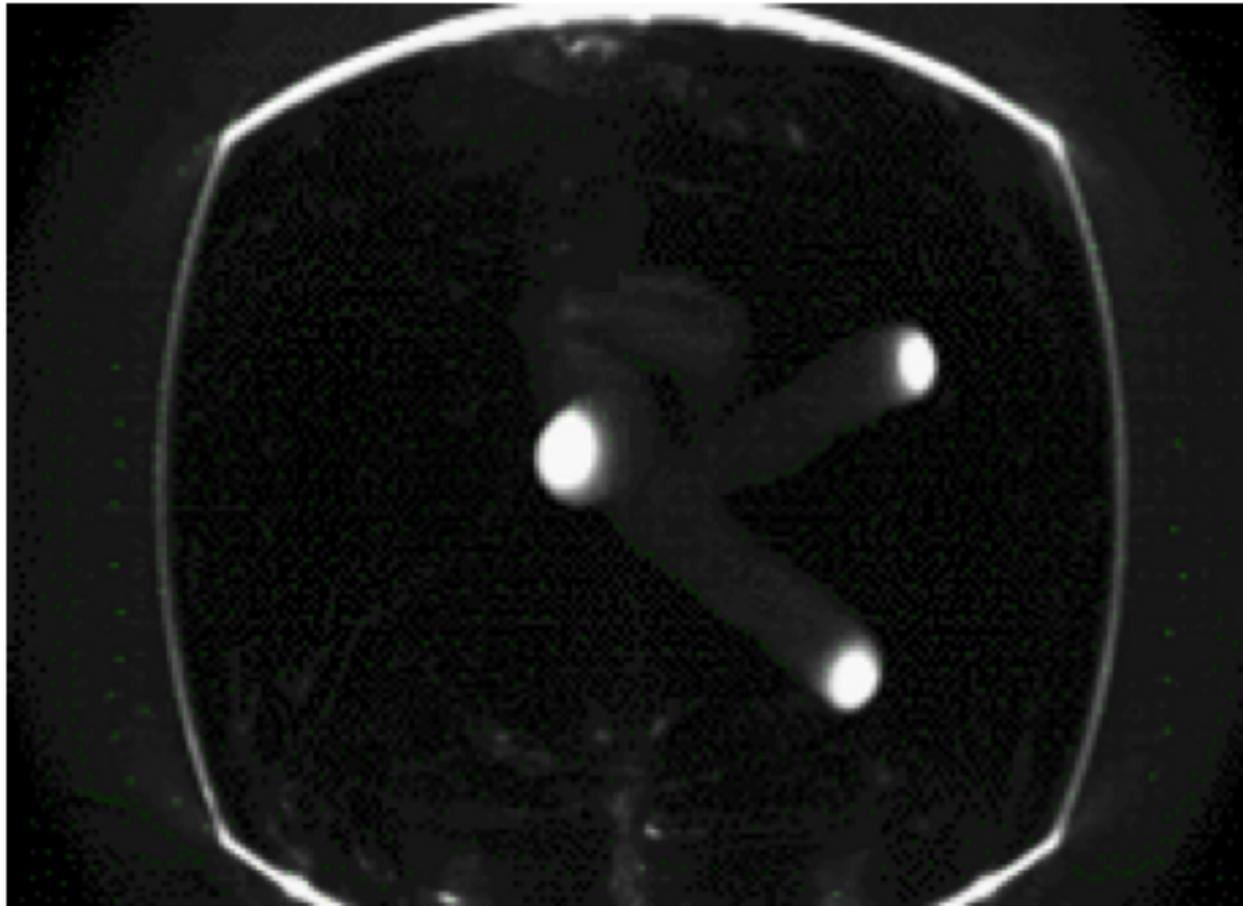
# FTIR



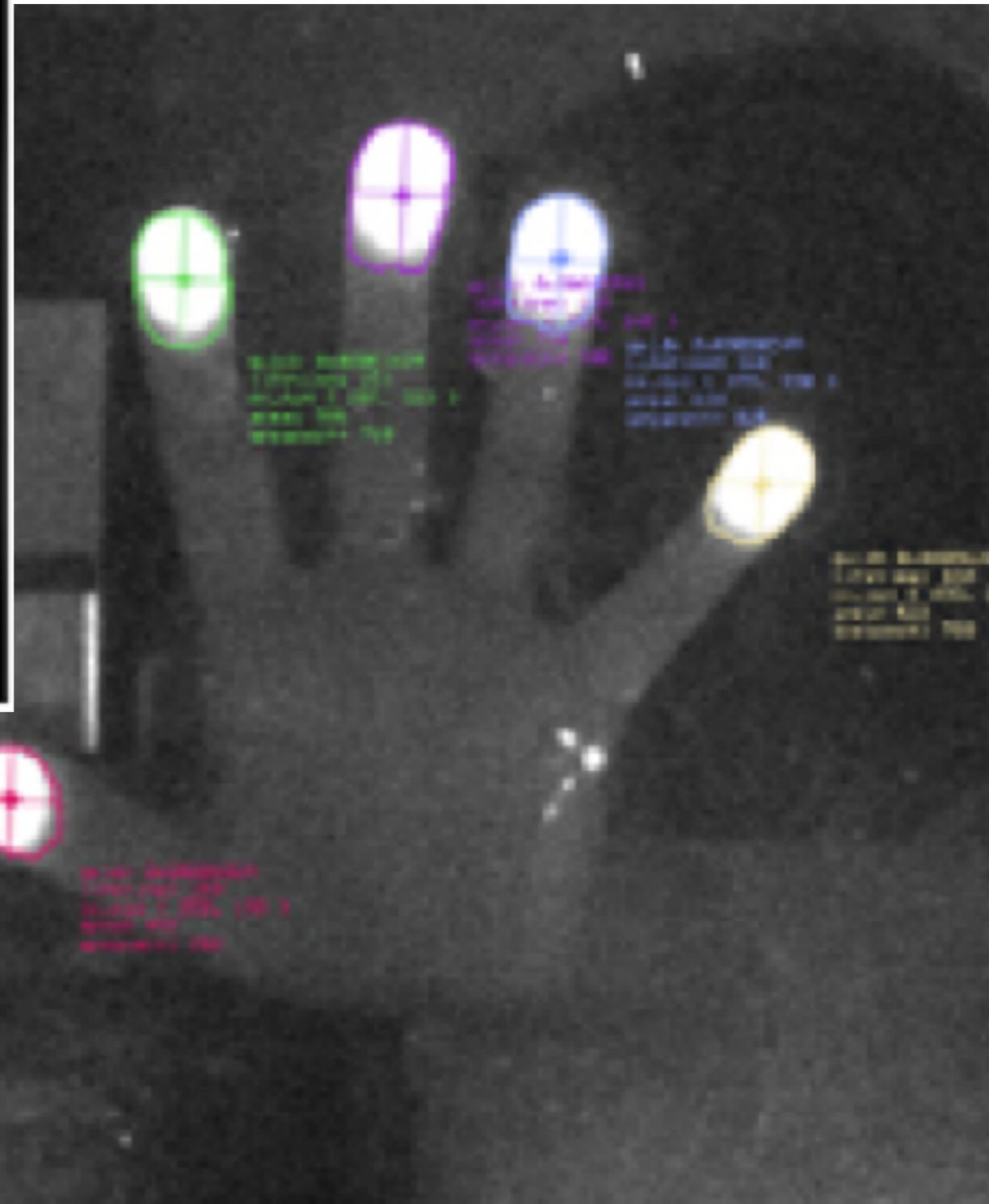
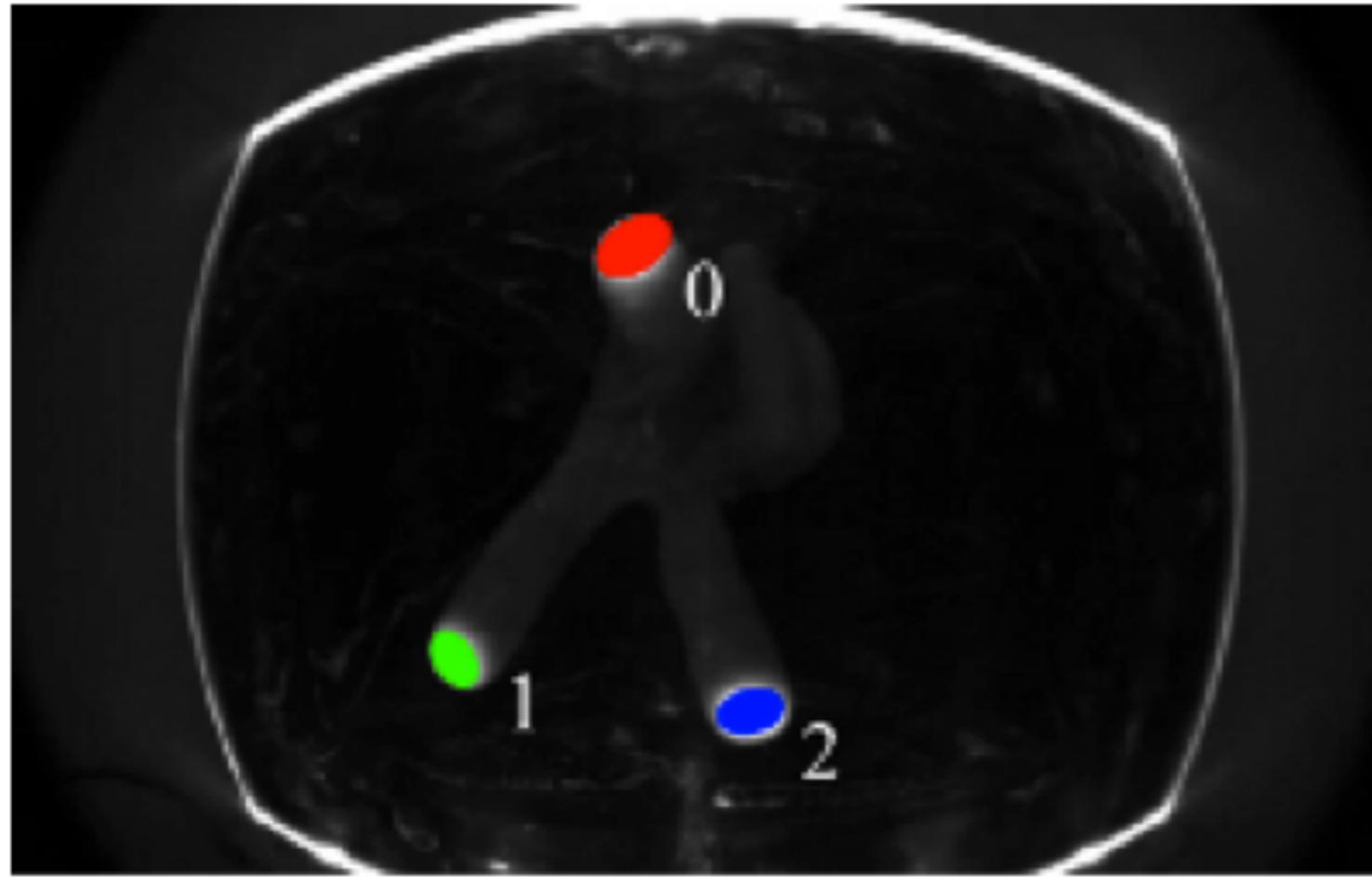
FTIR



# FTIR

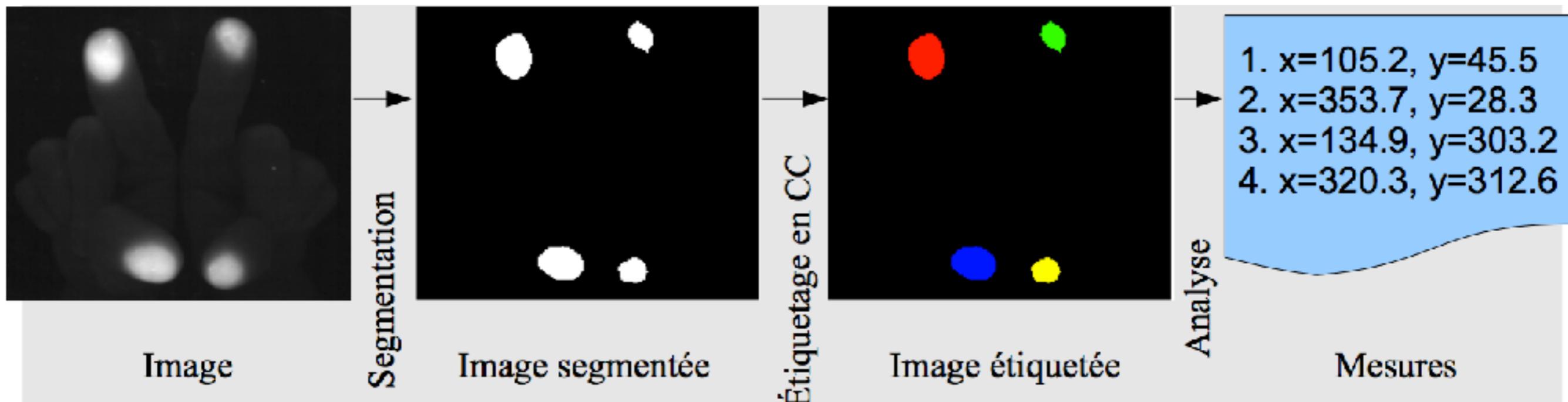


# FTIR



# Segmentation

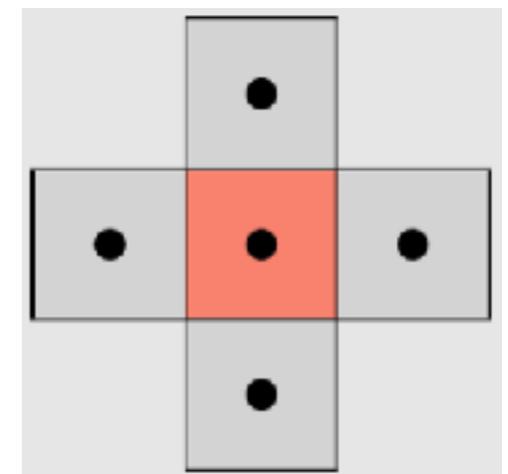
Binarisation



# Détection des régions connexes

0	0	0	0	0	0	0	0	0
0	1	1	0	0	0	1	1	1
0	1	1	0	0	1	0	1	1
0	1	1	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0
0	0	0	1	1	0	0	0	0
0	0	0	1	0	0	0	0	0
0	0	0	0	0	0	0	0	0

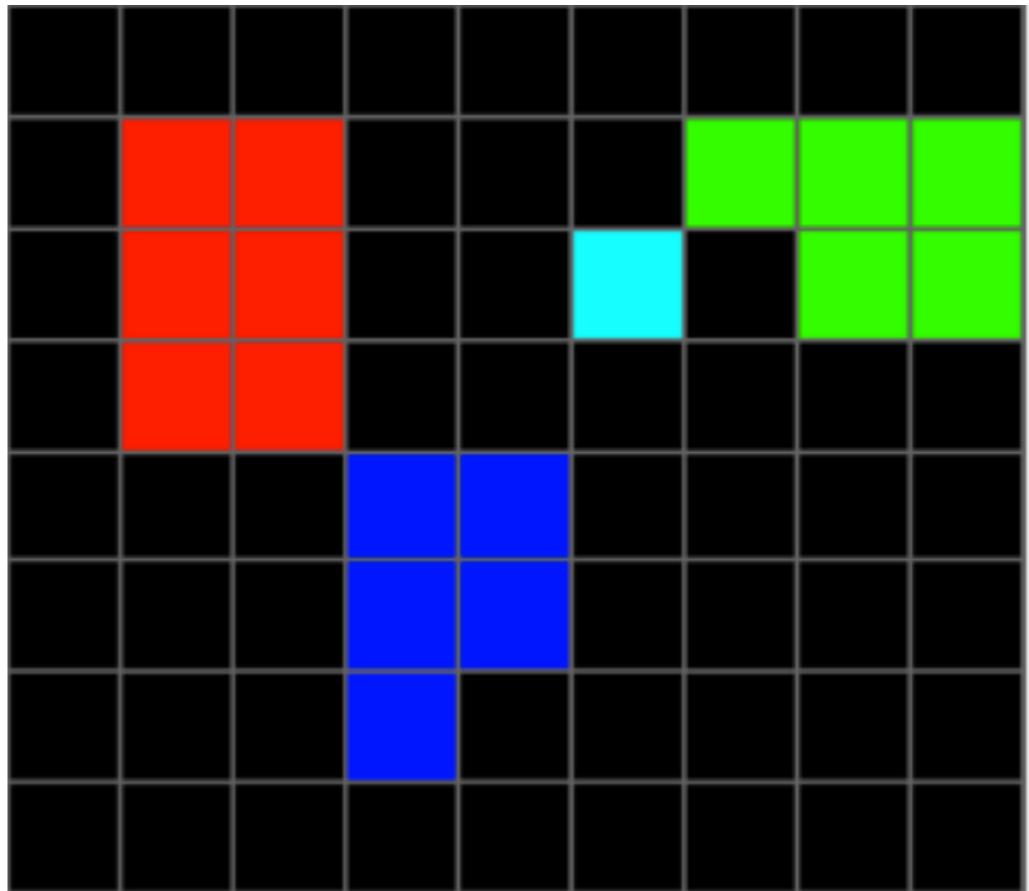
0	0	0	0	0	0	0	0	0
0	1	1	0	0	0	1	1	1
0	1	1	0	0	1	0	1	1
0	1	1	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0
0	0	0	1	1	0	0	0	0
0	0	0	1	0	0	0	0	0
0	0	0	0	0	0	0	0	0



# Etiquetage

0	0	0	0	0	0	0	0	0
0	1	1	0	0	0	1	1	1
0	1	1	0	0	1	0	1	1
0	1	1	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0
0	0	0	1	1	0	0	0	0
0	0	0	1	0	0	0	0	0
0	0	0	0	0	0	0	0	0

0	0	0	0	0	0	0	0	0
0	1	1	0	0	0	2	2	2
0	1	1	0	0	3	0	2	2
0	1	1	0	0	0	0	0	0
0	0	0	4	4	0	0	0	0
0	0	0	4	4	0	0	0	0
0	0	0	4	0	0	0	0	0
0	0	0	0	0	0	0	0	0



# Double parcours

- **E/S**
  - Paramètre d'entrée : image binaire  $B$
  - Résultat de sortie : matrice (ou *carte*) d'étiquettes  $L$
- **Algorithme**
  - Premier parcours de l'image, dans le sens classique (*raster-scan order*) :  
À chaque pixel à 1 dans  $B$ , on affecte
    - la plus petite étiquette parmi celles de ses voisins **haut** et **gauche**  
*ou*
    - une nouvelle étiquette si aucun de ces 2 voisins n'est encore étiqueté
  - Second parcours de l'image, dans le sens inverse :  
À chaque pixel précédemment étiqueté, on affecte la plus petite étiquette parmi la sienne et celles de ses voisins **bas** et **droite**.

# Double parcours (1er parcours)

## Exemple-1<sup>er</sup> parcours (1/3)

- Initialisation  
 $nbLabels=0$
- Étape 1  
les voisins haut et gauche du premier pixel à 1 dans  $B$  ne sont pas encore étiquetés  
 $\Rightarrow$  nouvelle étiquette ( $nbLabels=1$ )
- Étape 2  
le voisin gauche du pixel suivant à 1 dans  $B$  est déjà étiqueté à 1  $\Rightarrow$  affecter cette même étiquette au pixel
- Étape 3  
nouvelle étiquette ( $nbLabels=2$ )

**B**

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

**L**

0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	1	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	1	1	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

# Double parcours (1er parcours)

## Exemple-1<sup>er</sup> parcours (2/3)

- Étape 4  
affecter au pixel l'étiquette de son voisin gauche
- Étape 5  
nouvelle étiquette ( $nbLabels=3$ )
- Étape 6  
les voisins haut et gauche du pixel suivant à 1 dans  $B$  sont étiquetés différemment  $\Rightarrow$  affecter au pixel l'étiquette minimale
- Étape 7  
affecter au pixel l'étiquette de son voisin haut

**B**

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

**L**

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	0	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	0	0	0	0	0	0
0	0	0	0	0	0	0

# Double parcours (1er parcours)

## Exemple-1<sup>er</sup> parcours (3/3)

- Étape 8  
affecter au pixel l'étiquette de son voisin haut
- Étape 9  
nouvelle étiquette ( $nbLabels=4$ )
- Étape 10  
affecter au pixel l'étiquette de son voisin gauche
- Étape 11  
les voisins haut et gauche du pixel suivant à 1 dans  $B$  sont étiquetés différemment  $\Rightarrow$  affecter au pixel l'étiquette minimale

$B$

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

$L$

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	0	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	4	0	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	4	4	0
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	4	4	2
0	0	0	0	0	0	0

# Double parcours (2e parcours)

## Exemple-2<sup>ème</sup> parcours (1/2)

- Image et carte initiales

**B**

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

**L**

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	4	4	2
0	0	0	0	0	0	0

- 1<sup>ère</sup> étiquette modifiée  
Affecter au pixel l'étiquette de son voisin droit car elle est inférieure à la sienne

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	4	2	2
0	0	0	0	0	0	0

- 2<sup>ème</sup> étiquette modifiée  
Affecter au pixel l'étiquette de son voisin droit car elle est inférieure à la sienne

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	2	2	2
0	0	0	0	0	0	0

- (étiquette non modifiée)

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	2	2	2
0	0	0	0	0	0	0

# Double parcours (2e parcours)

## Exemple-2<sup>ème</sup> parcours (2/2)

- (étiquette non modifiée)

**B**

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

**L**

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	3	1	0	0	0	2
0	3	0	0	2	2	2
0	0	0	0	0	0	0

- 3<sup>ème</sup> étiquette modifiée

Affecter au pixel l'étiquette de son voisin droit car elle est inférieure à la sienne et à celle de son voisin bas

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	1	1	0	0	0	2
0	3	0	0	2	2	2
0	0	0	0	0	0	0

- Carte à l'issue du 2<sup>ème</sup> parcours  
Aucune autre étiquette n'est plus modifiée

0	0	0	0	0	0	0
0	0	1	1	0	1	1
0	1	1	0	0	0	1
0	1	0	0	1	1	1
0	0	0	0	0	0	0

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	1	1	0	0	0	2
0	3	0	0	2	2	2
0	0	0	0	0	0	0

- **Problème (collisions)** : d'autres parcours (jusqu'à ce qu'il n'y ait plus de changement) sont nécessaires pour obtenir la carte finale. Ex. après 3<sup>ème</sup> parcours en sens classique :

0	0	0	0	0	0	0
0	0	1	1	0	2	2
0	1	1	0	0	0	2
0	1	0	0	2	2	2
0	0	0	0	0	0	0

# Suivi des blobs

1

2

3

instant t

1

2

3

instant t+1

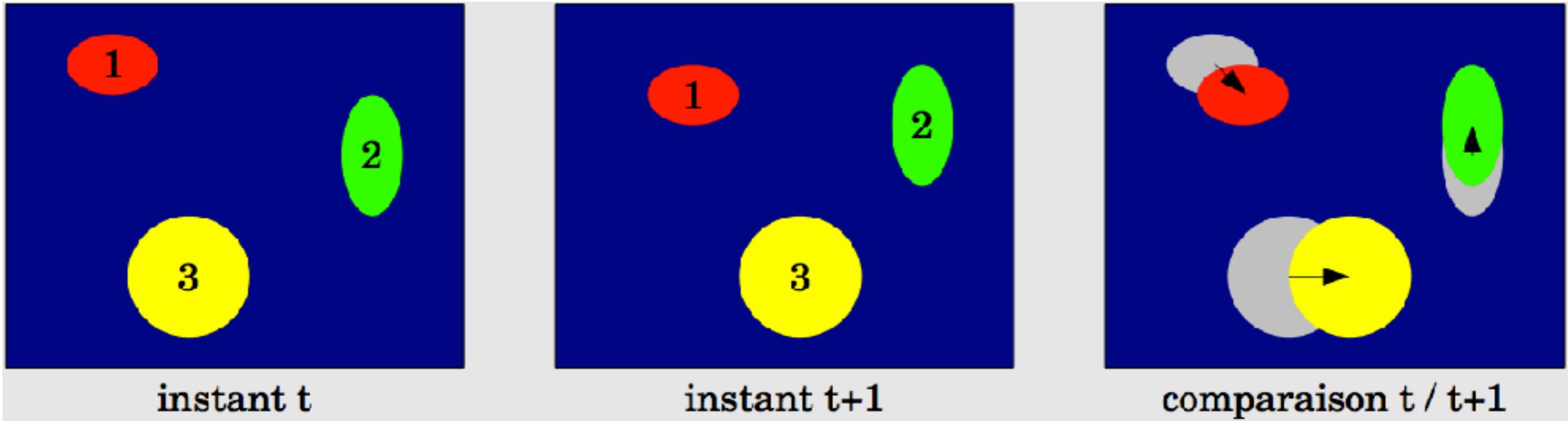
2

1

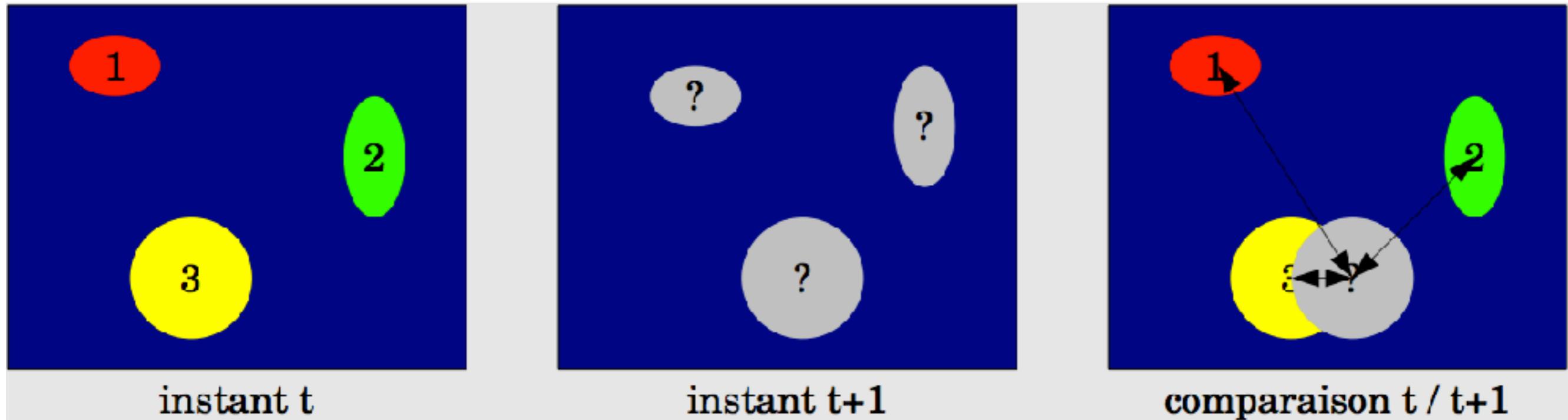
3

instant t+2

# Distances inter-blobs



# Distances inter-blobs



# Distances inter-blobs

		t+1		
t		?	?	?
1	25.3	1.9	40.3	
2	3.2	27	36.4	
3	41.6	33.2	4.2	

		t+1		
t		?	?	?
1			1.9	
2		3.2		
3				4.2

		t+1		
t		2	1	3
1			1.9	
2		3.2		
3				4.2

# Disparition d'un objet

		t+1	
t		?	?
1	25.3	1.9	
2	3.2	27	
3	41.6	33.2	

		t+1	
t		?	?
1		1.9	
2	3.2		
3			

		t+1	
t		2	1
1			1.9
2	3.2		
3			

# Apparition d'un objet

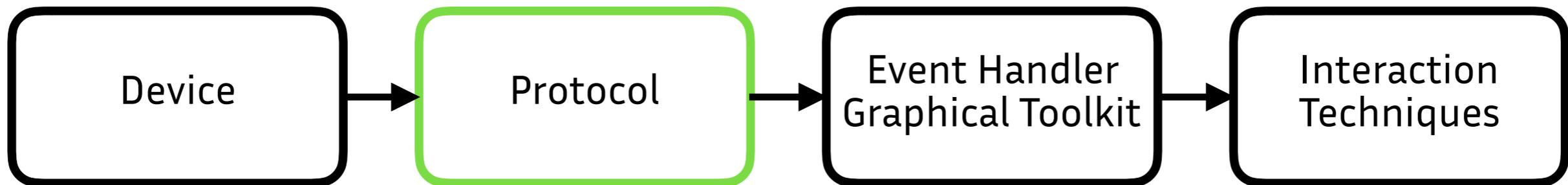
		t+1		
		?	?	?
t	1	25.3	1.9	40.3
t	2	3.2	27	36.4

		t+1		
		?	?	?
t	1		1.9	
t	2	3.2		

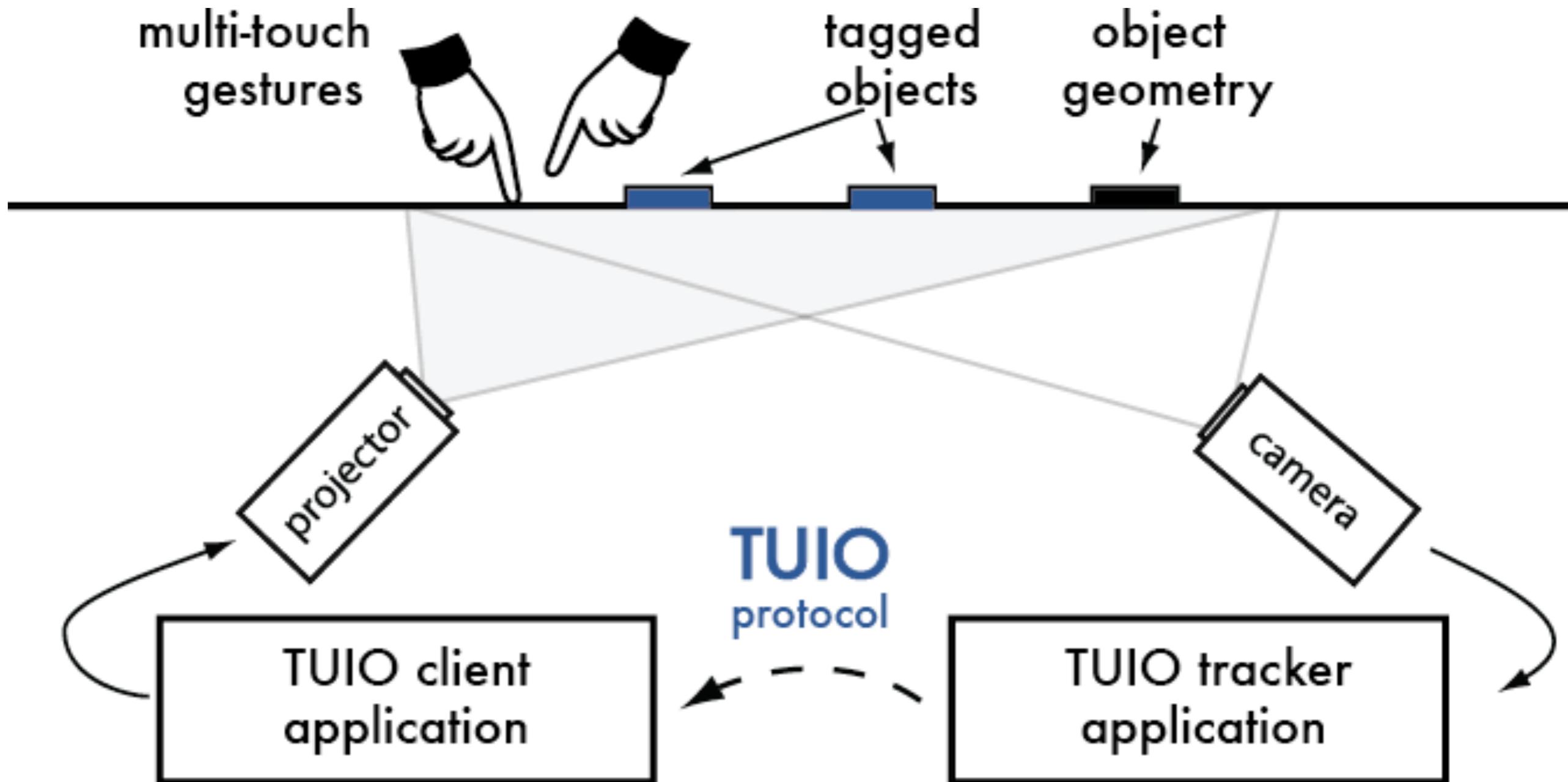
		t+1		
		2	1	?
t	1		1.9	
t	2	3.2		

		t+1		
		2	1	3
t	1		1.9	
t	2	3.2		

# Multitouch pipeline



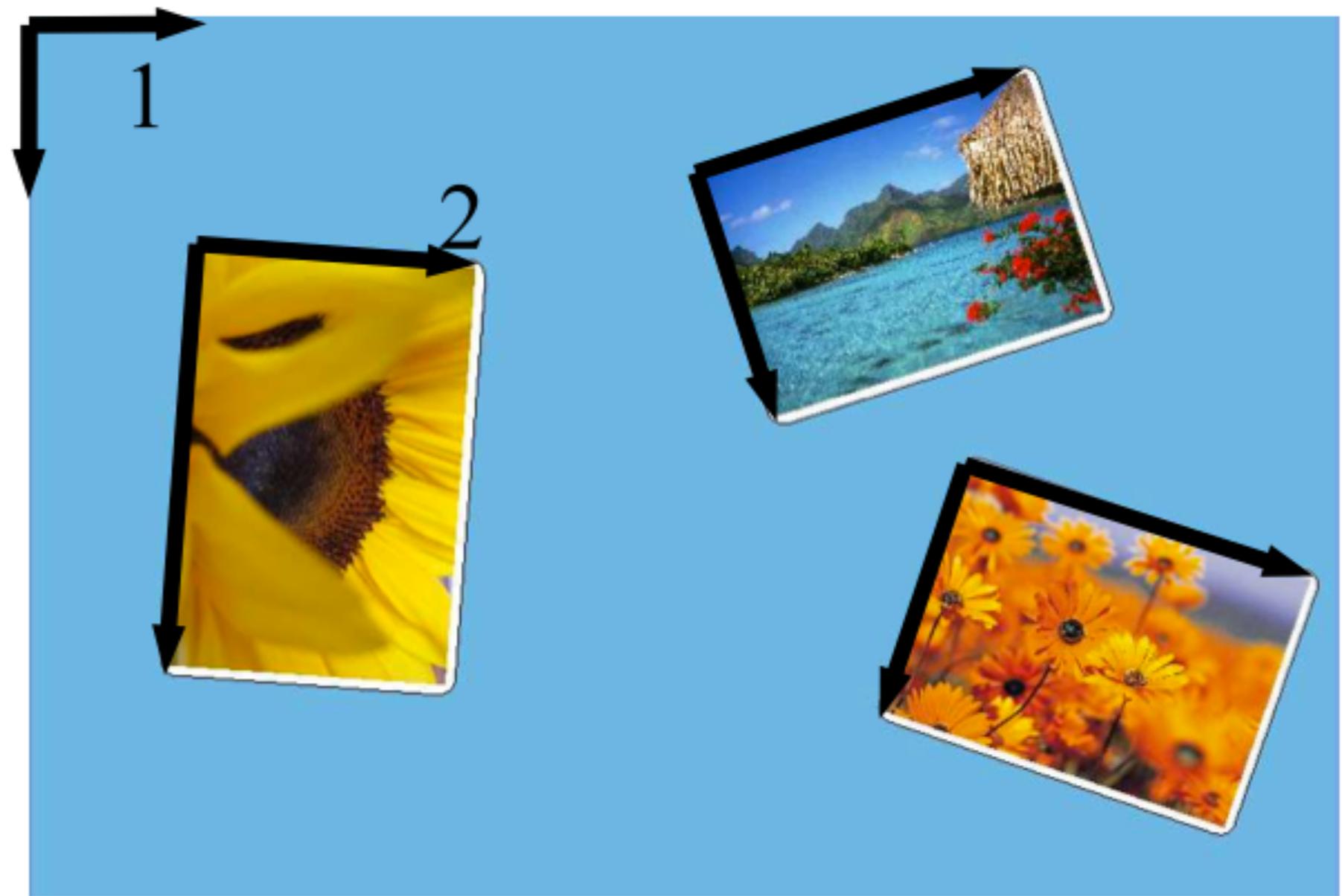
# TUIO



# Interaction



# OBB



Le repère 2 est placé dans le repère 1 en déplaçant 1 vers 2 (on dit qu'on passe du repère 1 au repère 2, et sera noté  $M_{1 \rightarrow 2}$ ) :

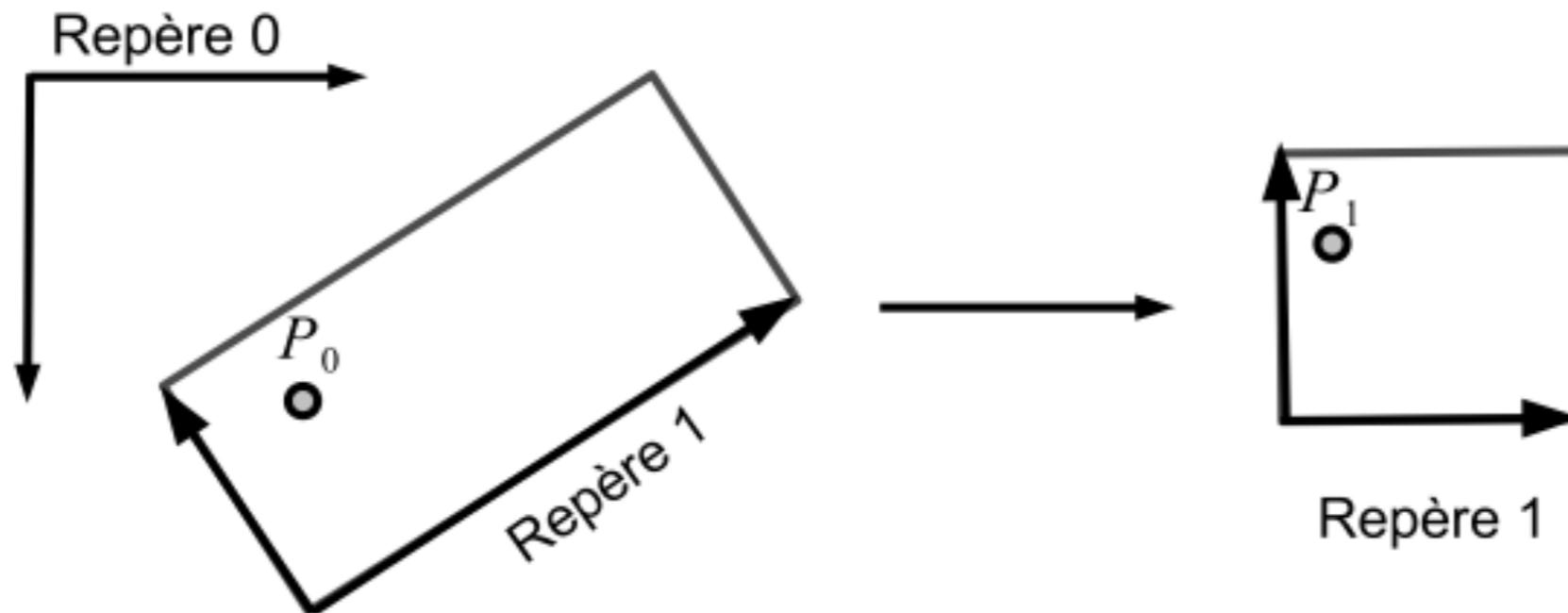
- 1 En faisant une translation (donnée par le champs `position`) notée  $T$
- 2 **Puis** une rotation autour de l'origine **actuelle** (l'angle est donné par `angle`) notée  $R$
- 3 **Puis** un changement d'échelle (l'axe `x` actuel est multiplié par `width`, l'axe actuel `y` par `height`) notée  $S$ .
- 4  $\Rightarrow$  on note ainsi le passage de 1 vers 2 :  $M_{1 \rightarrow 2} = TRS$ .

## Expression d'un point dans des repères différents

- ▶ Soit un point  $P$  connu dans un repère 2 (noté  $P_2$ ). Soit un repère 1 dont on connaît le passage  $M_{1 \rightarrow 2}$ .
- ▶ Alors les coordonnées de  $P$  dans 1 sont donnés par la relation  $P_1 = M_{1 \rightarrow 2} P_2$ .
- ▶ Exemple :  $M_{1 \rightarrow 2} = TRS$ , et  $P_2(x_2, y_2)$ , alors  $P_1(x_1, y_1) = TRSP_2(x_2, y_2)$  :
  - $S(k_x, k_y) : x' = k_x \times x_2$  et  $y' = k_y \times y_2$ .
  - puis  $R(\theta) : x'' = x' \cos \theta - y' \sin \theta$  et  $y'' = x' \sin \theta + y' \cos \theta$
  - et finalement  $T(t_x, t_y) : x_1 = x'' + t_x$  et  $y_1 = y'' + t_y$ .

## Localiser un point dans une OBB

- ▶ Sélection d'un composant = lors d'un "addCursor(x,y)" on détermine à quel composant correspond  $(x, y)$ .
- ▶ Donnée : un point  $P(x, y)$  dans le repère initial 0 (curseur en coordonnée pixel).
- ▶ Problème : à quel composant appartient  $P$  ?

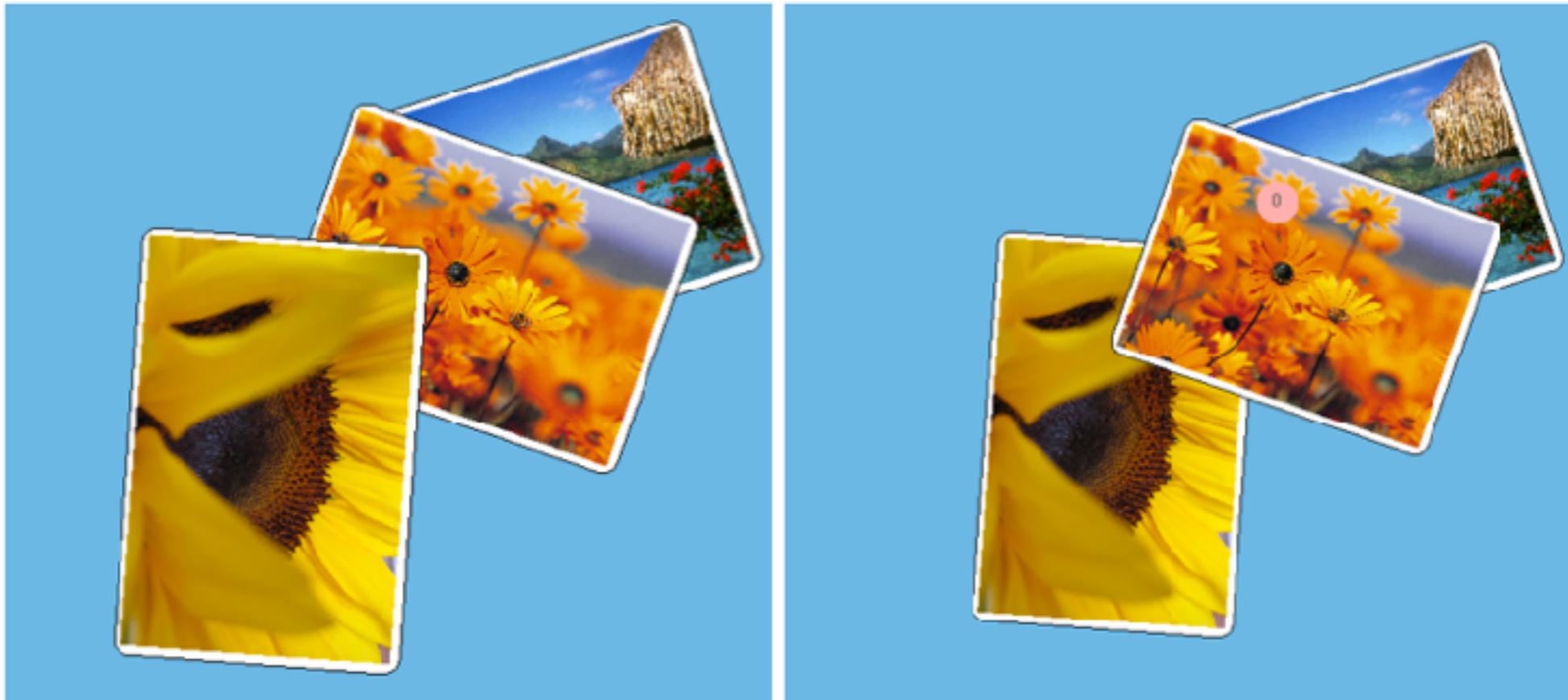


## Localiser un point dans une OBB

- ▶ une OBB est un carré défini dans un repère local 1 dont on a fait subir  $M_{0 \rightarrow 1} = TRS$  pour le placer par rapport au repère 0 ( $T = origin$ ,  $R = angle$ ,  $S = (width, height)$ ).
- ▶ il est plus aisé de tester l'appartenance du point  $P$  dans le carré  $\Rightarrow$  exprimer  $P$  dans 1 par  $P_1 = M_{1 \rightarrow 0} P_0$ .
- ▶ Cas général : il faut inverser  $M_{p \rightarrow q}$  pour obtenir  $M_{q \rightarrow p}$ .
- ▶ Cas d'une Composition : l'inverse de  $M_{p \rightarrow q} M_{q \rightarrow r}$  est  $M_{r \rightarrow q} M_{q \rightarrow p}$
- ▶ Par ailleurs  $T^{-1} = -T$ ,  $R^{-1}(\theta) = R(-\theta)$  et  $S^{-1}(k_x, k_y) = S(\frac{1}{k_x}, \frac{1}{k_y})$ .

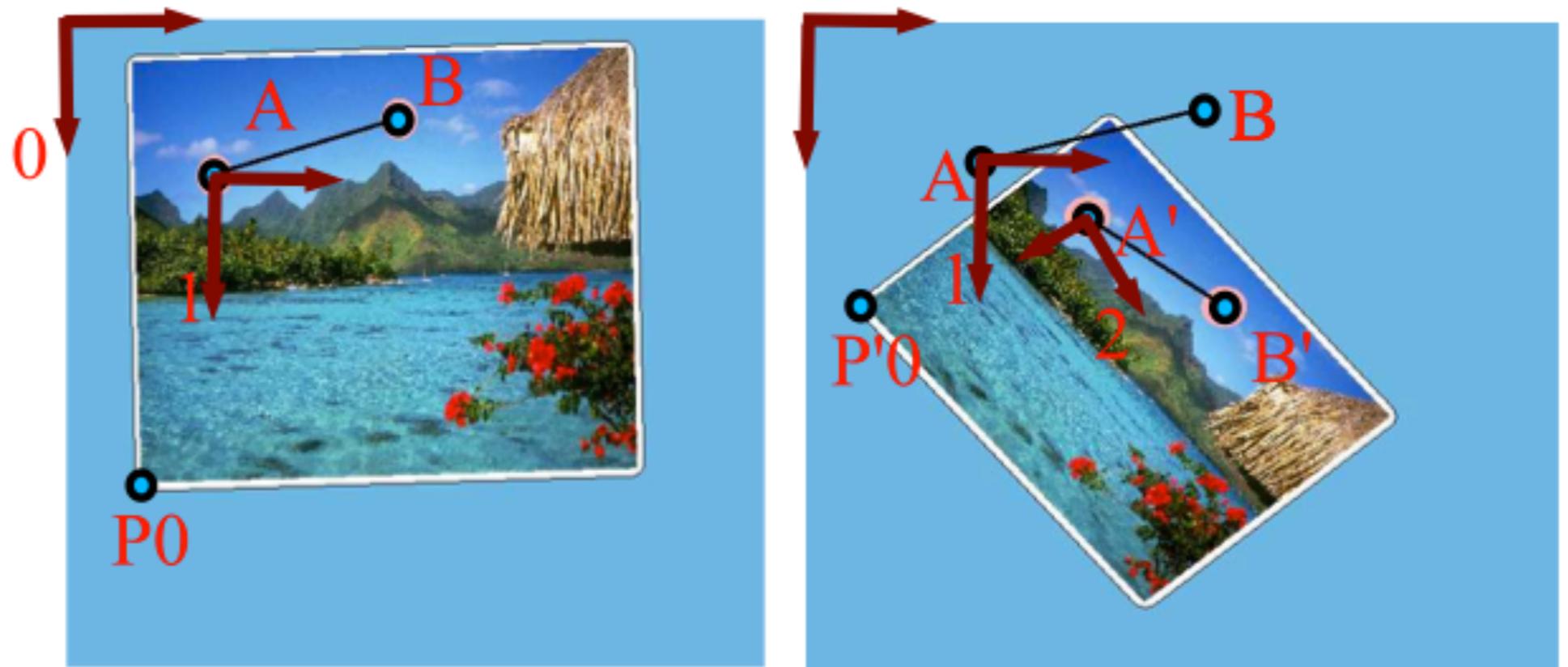
# Superposition de composants

- ▶ L'ordre dans la liste des composants définit l'ordre d'affichage (le premier à l'arrière-plan), ou profondeur d'affichage.
- ▶ Si il y a superposition de composants lors d'une sélection  $\Rightarrow$  le composant sélectionné est celui qui est visible (i.e. le moins profond).
- ▶ Une fois sélectionné, le composant passe à l'avant plan.



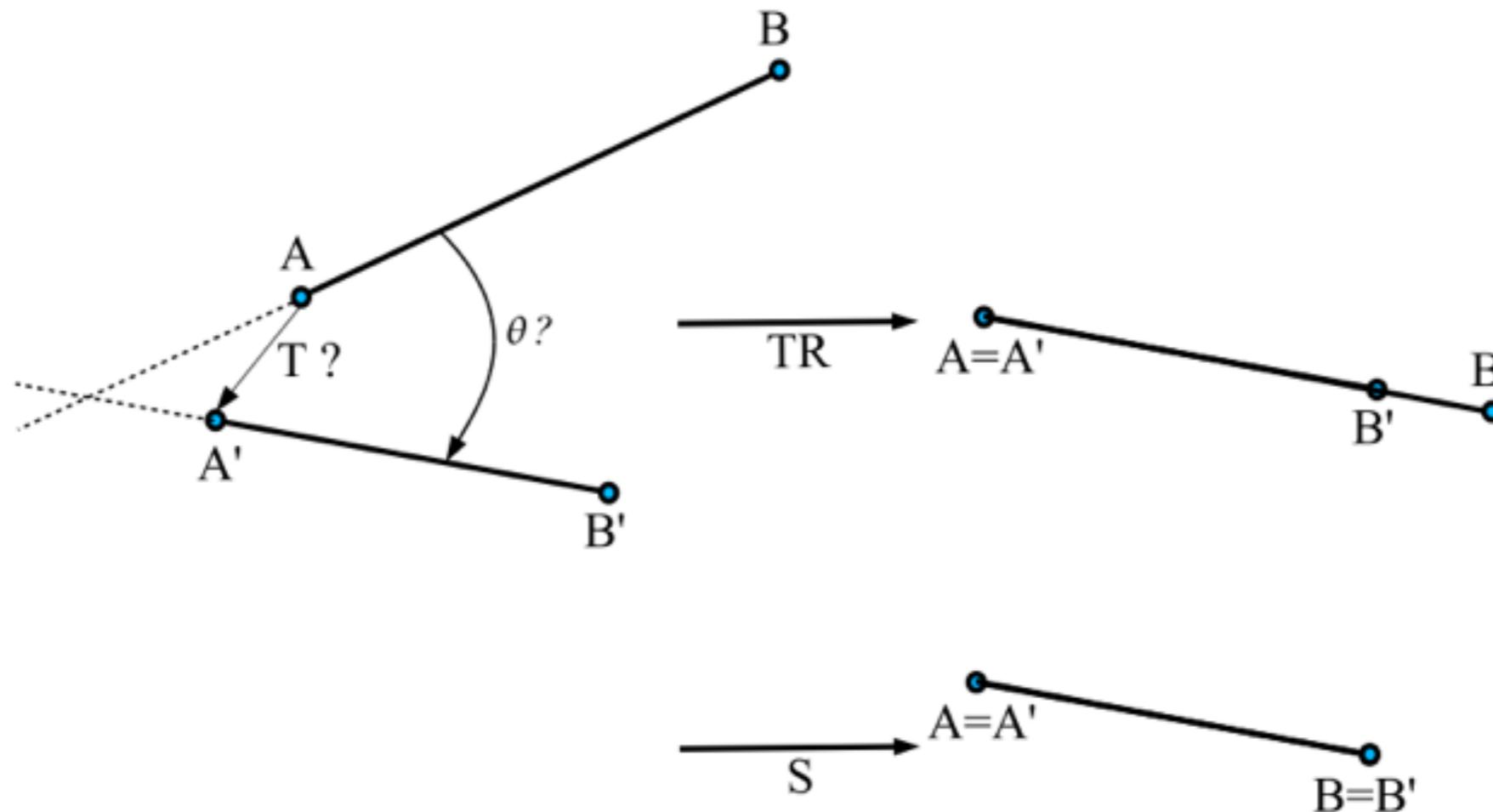
## Mouvement d'un objet avec 2 doigts

- ▶ 2 curseurs sur l'image :  $A$  et  $B$ .
- ▶ Attacher l'image aux curseurs.
- ▶ Mouvement des curseurs :  $A$  déplacé en  $A'$  et  $B$  en  $B'$ .



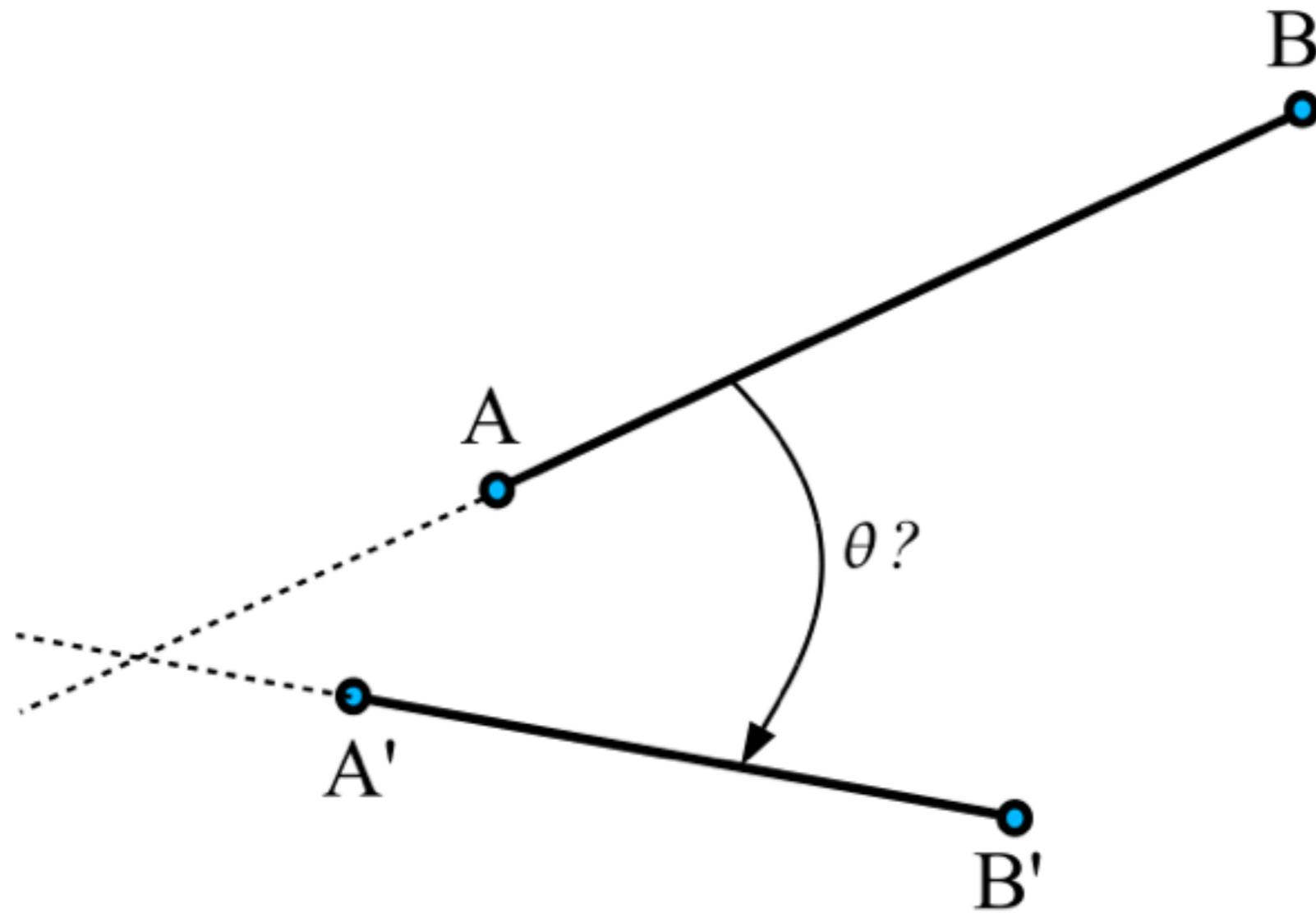
# Transformation du segment AB

- ▶ On "attache"  $AB$  à un repère 1 (l'origine de 1 est  $A$ ) et on exprime le changement de repère  $M_{1 \rightarrow 2}$  pour aller en  $A'B'$  (l'origine de 2 est  $A'$ ) :



- ▶  $T$  = translation de vecteur  $AA'$ .
- ▶ puis  $R$  = rotation d'angle ?
- ▶ puis  $S$  = rapport des longueurs entre  $AB$  et  $A'B'$ .

## Calcul de l'angle de rotation



- On utilise le produit scalaire entre  $AB$  et  $A'B'$ , car  $AB \cdot A'B' = \|AB\| \|A'B'\| \cos\theta$ .

# Produit scalaire

Soient  $u = \begin{pmatrix} u_x \\ u_y \end{pmatrix}$ ,  $v = \begin{pmatrix} v_x \\ v_y \end{pmatrix}$ , le produit scalaire  $u \cdot v$  (appelé dot en anglais) est le nombre donné par :

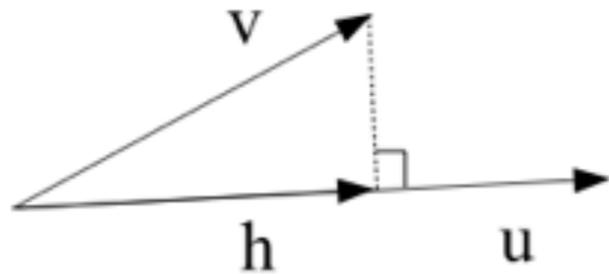
- ▶  $u \cdot v = u_x v_x + u_y v_y$  (Calcul par coordonnées)
- ▶  $u \cdot v = \|u\| \|v\| \cos(u, v)$  (Calcul par cosinus)

Relation avec la norme (la « longueur ») du vecteur  $u$  :

- ▶ Norme (euclidienne) :  $\|u\| = \sqrt{u \cdot u} = \sqrt{u_x u_x + u_y u_y}$
- ▶ Remarque : Normer  $u$  consiste à « rendre » le vecteur  $u$  de norme 1 :  $u' = \frac{u}{\|u\|}$

# Produit scalaire

- ▶ Projection du vecteur  $v$  sur  $u$  :



- $u \cdot v = u \cdot h$
- $\|h\| = \frac{|u \cdot v|}{\|u\|}$
- Si  $u$  est unitaire :  $h = (u \cdot v)u$

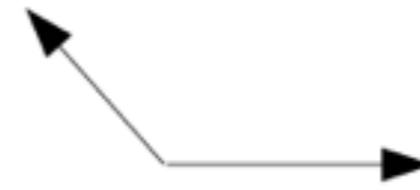
- ▶ Localisation relative des vecteurs  $u$  et  $v$  :



$u \cdot v = 0$  (orthonormal)



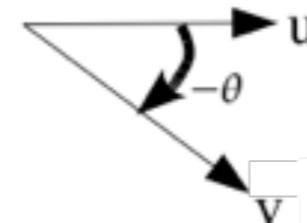
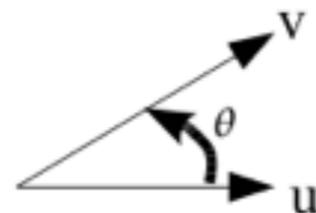
$u \cdot v > 0$  (aigu)



$u \cdot v < 0$  (obtus)

- ▶ Si  $u$  et  $v$  sont de norme 1 :

- $u \cdot v = \cos(u, v)$
- $\arccos(u \cdot v)$  donne un angle dans  $[0, \pi]$ .
- $\Rightarrow$  le produit scalaire ne suffit pas à lui seul :



# Déterminant

► Calcul :

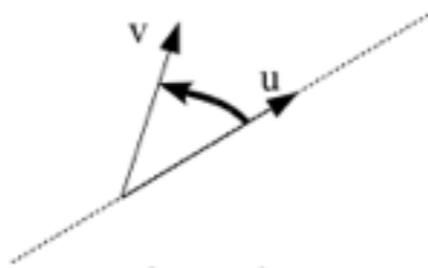
Soient  $u = \begin{pmatrix} u_x \\ u_y \end{pmatrix}$ ,  $v = \begin{pmatrix} v_x \\ v_y \end{pmatrix}$ , le déterminant est donné par le nombre :

$$\det(u, v) = u_x v_y - u_y v_x$$

Remarque : il s'agit de la 3<sup>ème</sup> coordonnée du produit vectoriel entre  $\begin{pmatrix} u_x \\ u_y \\ u_z = 0 \end{pmatrix}$  et

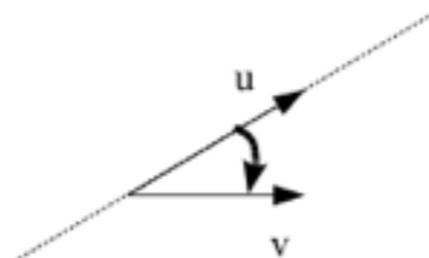
$$\begin{pmatrix} v_x \\ v_y \\ v_z = 0 \end{pmatrix}$$

► Interprétation :



$$\det(u, v) > 0$$

u vers v : dans le sens direct  
appliquer  $\theta$



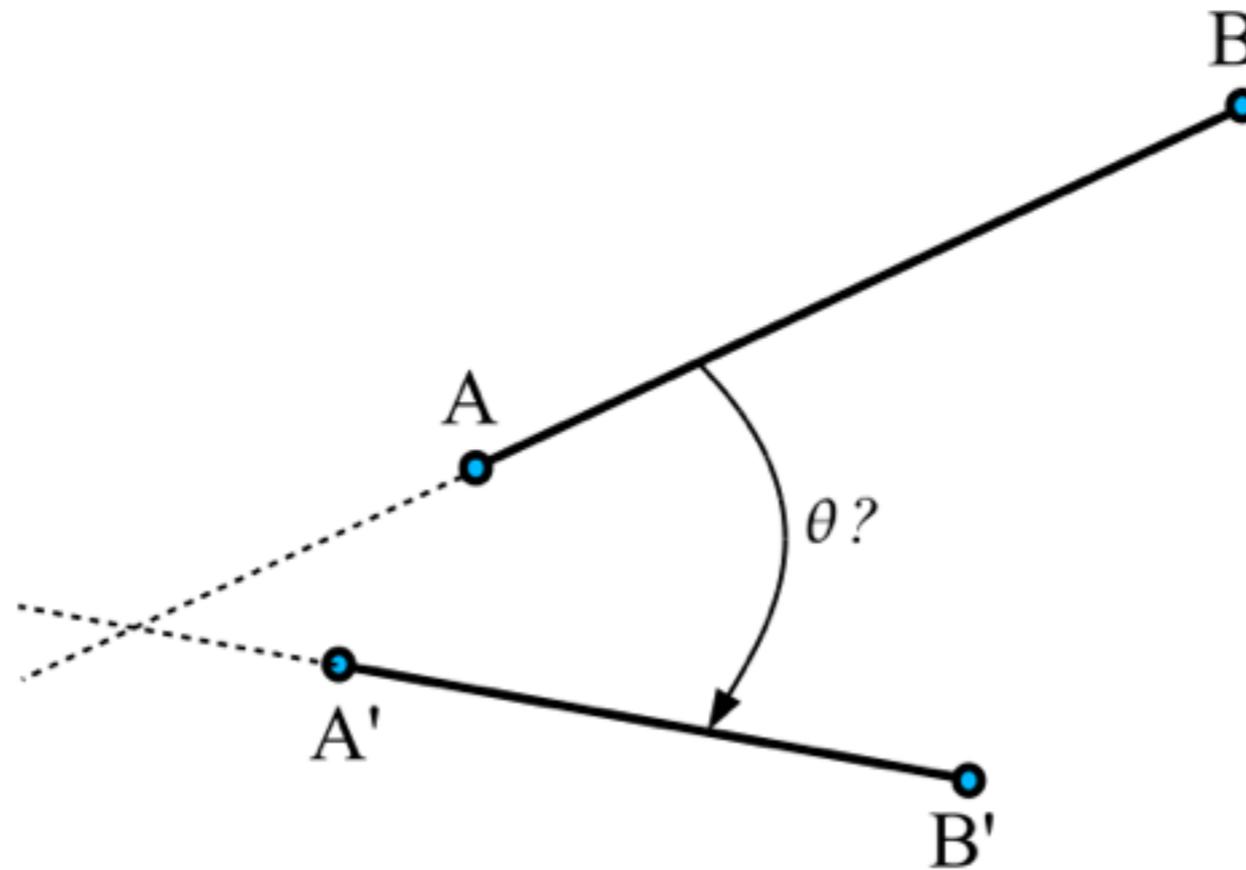
$$\det(u, v) < 0$$

u vers v : dans le sens indirect  
appliquer  $-\theta$



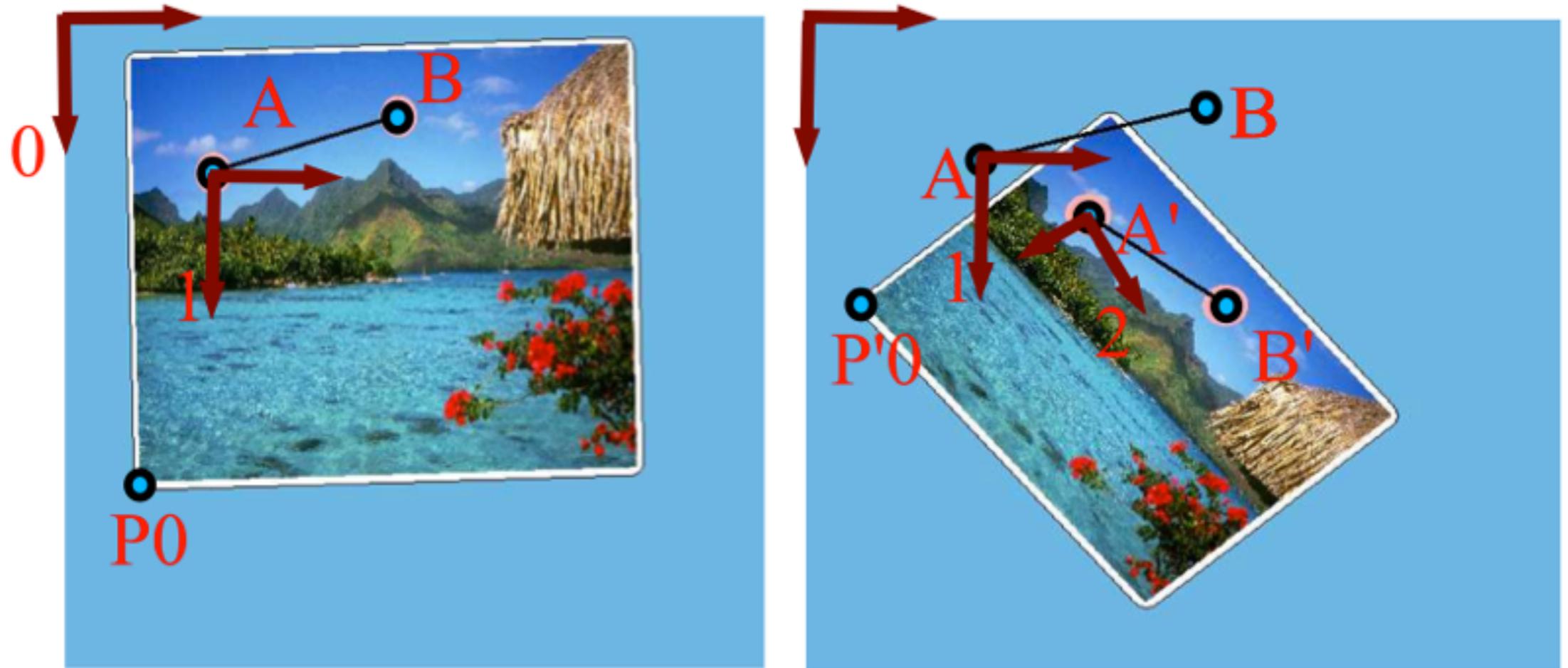
$$\det(u, v) = 0$$

## Résumé du calcul de l'angle de rotation



- ▶  $u = AB, v = A'B'$
- ▶ On norme  $u$  et  $v \Rightarrow u \cdot v = \cos(\theta) \Rightarrow \theta = \arccos(u \cdot v)$
- ▶ Calculer  $\det(u, v)$  pour savoir si  $\theta$  est négatif ou positif (i.e. si négatif, prendre  $-\theta$  comme angle de rotation).

## Résumé du TRS à deux doigts



- ▶ width et height subissent le rapport  $\frac{\|A'B'\|}{\|AB\|}$
- ▶ angle subit l'angle entre  $AB$  et  $A'B'$
- ▶ position subit le mouvement de  $P_0$  à  $P'_0$

## Résumé du TRS à deux doigts

$m_{01}$ : matrice de passage du repère 0 au repère 1

$m_{02}$ : matrice de passage du repère 0 au repère 2

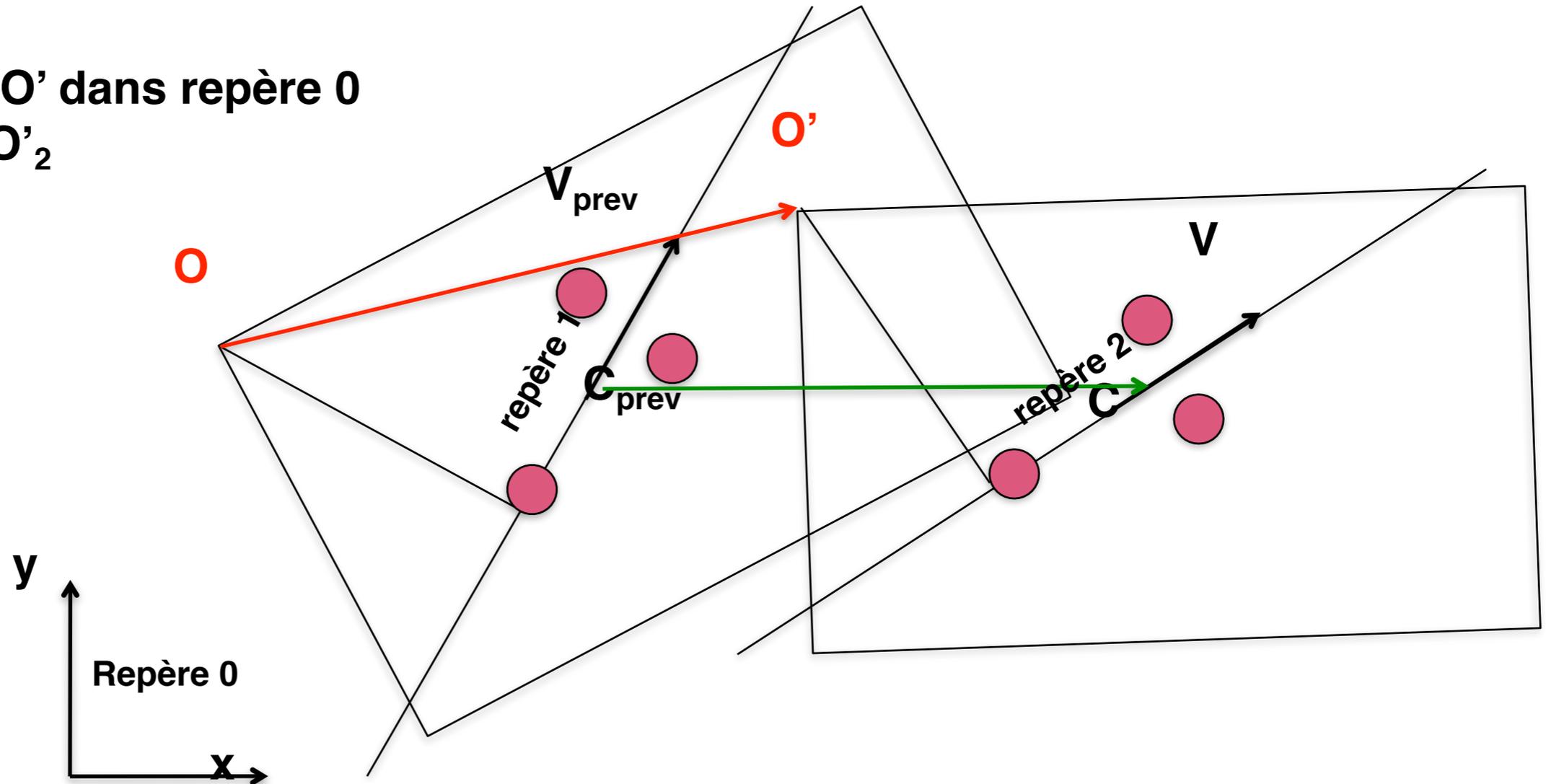
1) Calcul des coordonnées de 0 dans le repère 1:

$$O_1 = m_{01}^{-1} O_0$$

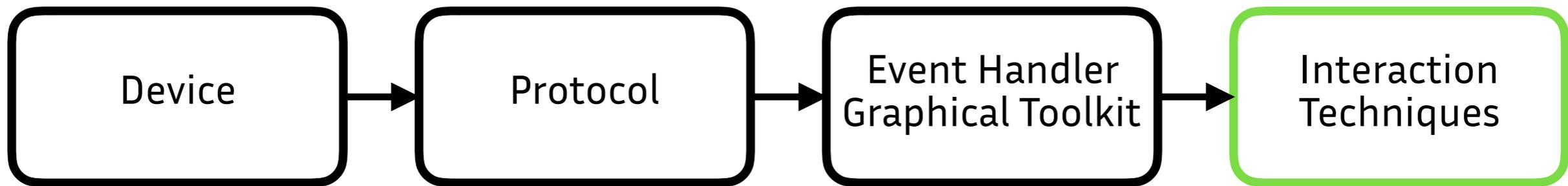
2)  $O'_2 = O_1$  (sans tenir compte du changement d'échelle)

3) Calcul de  $O'$  dans repère 0

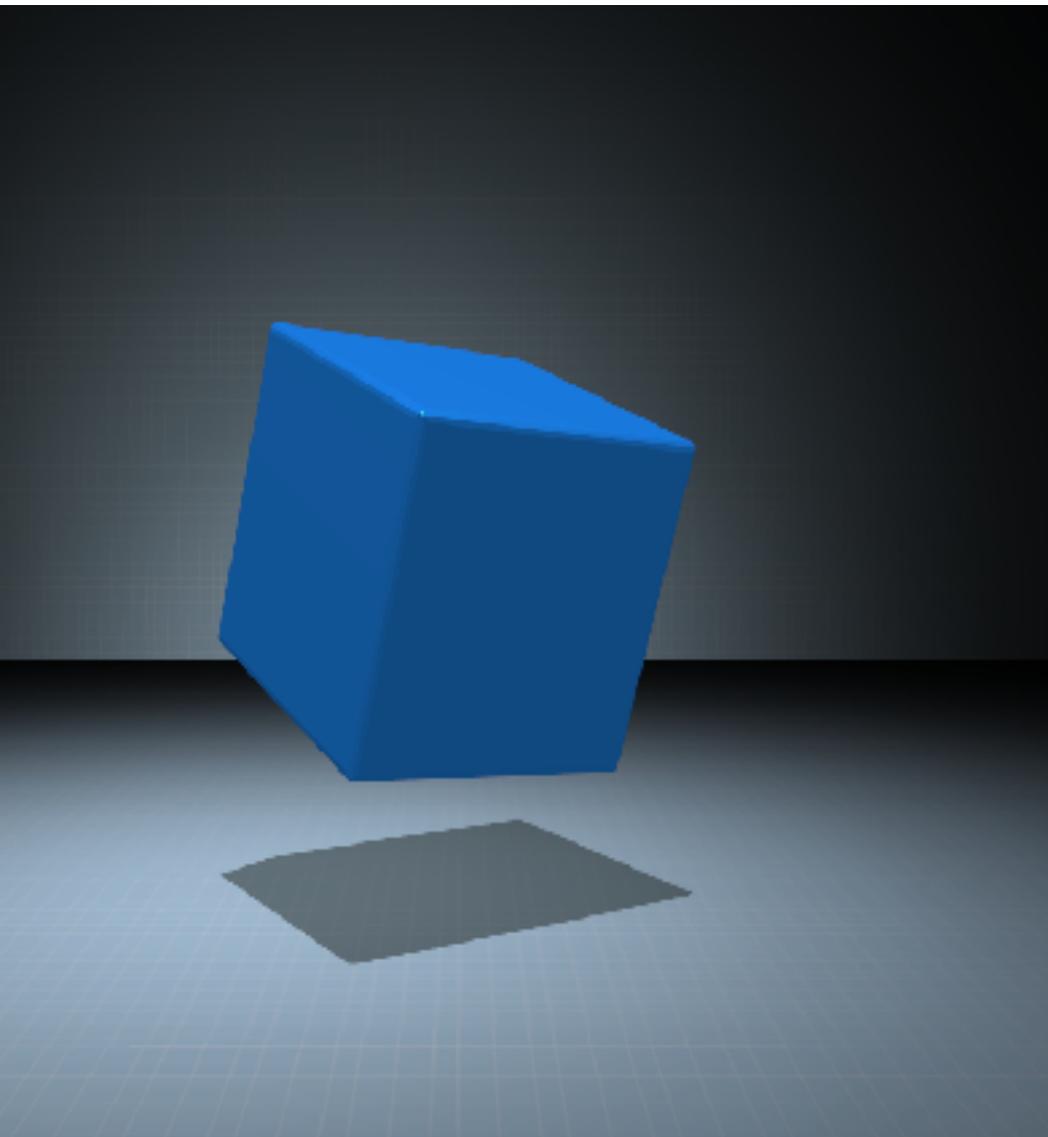
$$O'_0 = m_{02} O'_2$$

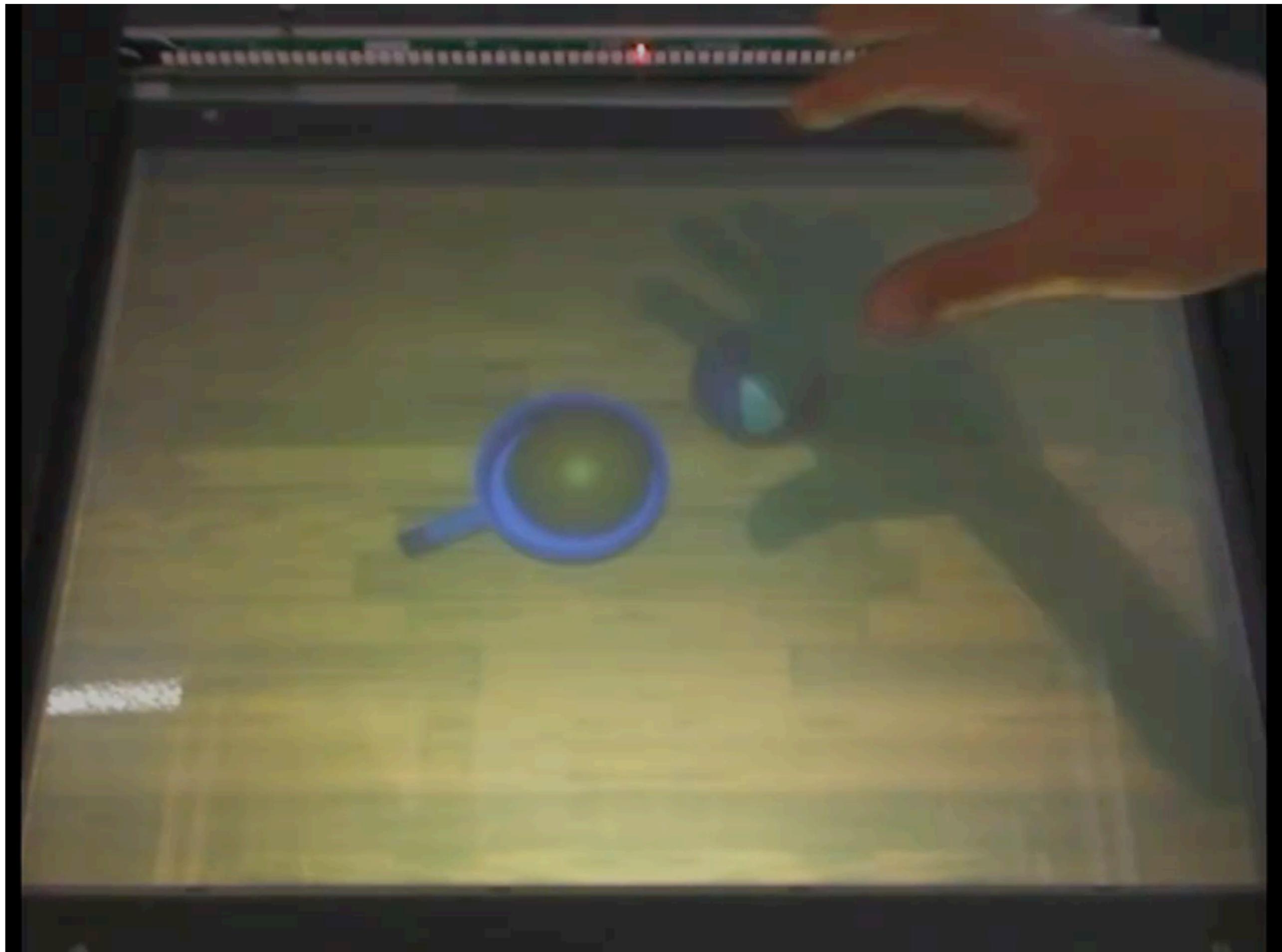


# Multitouch pipeline

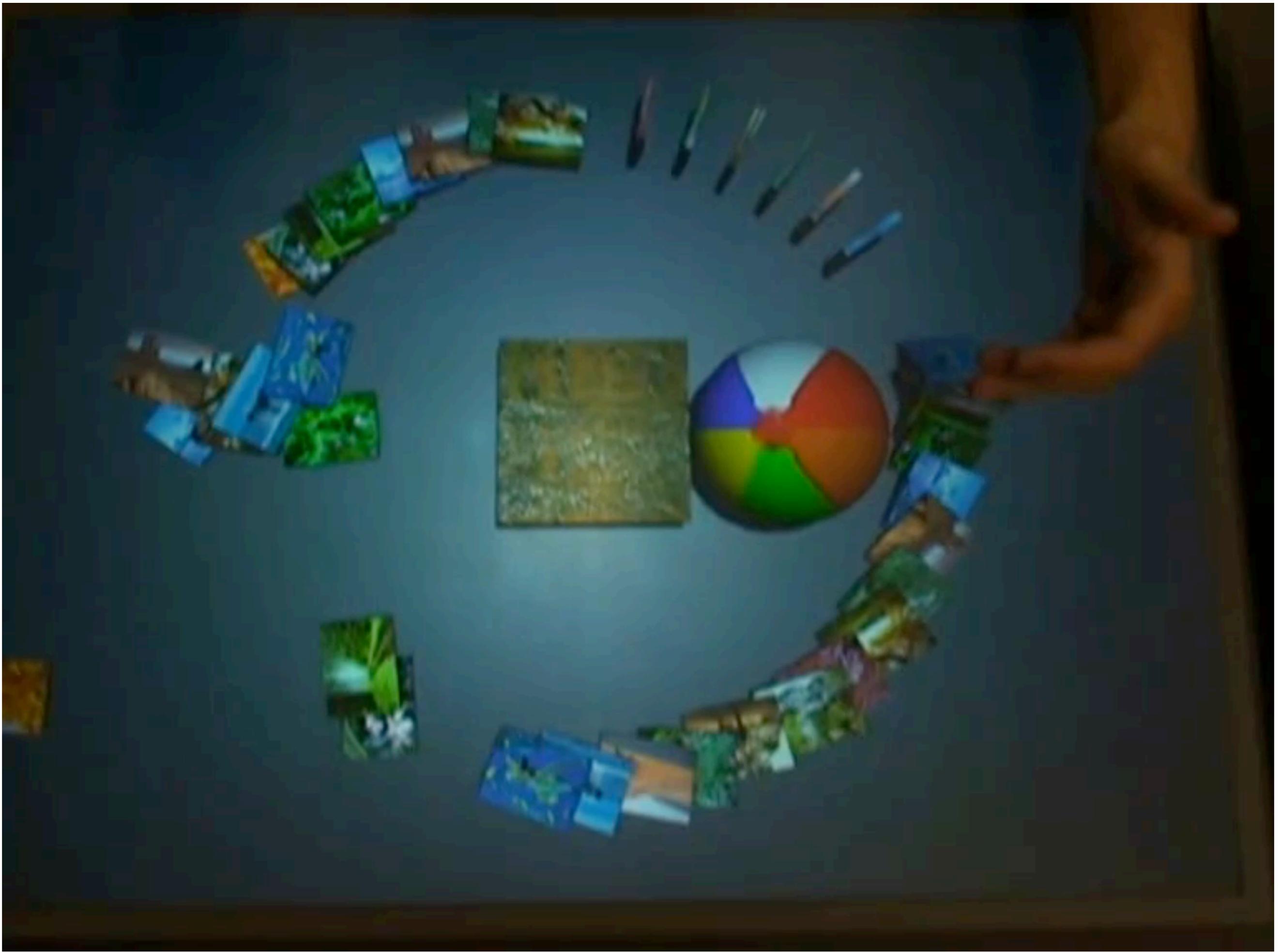


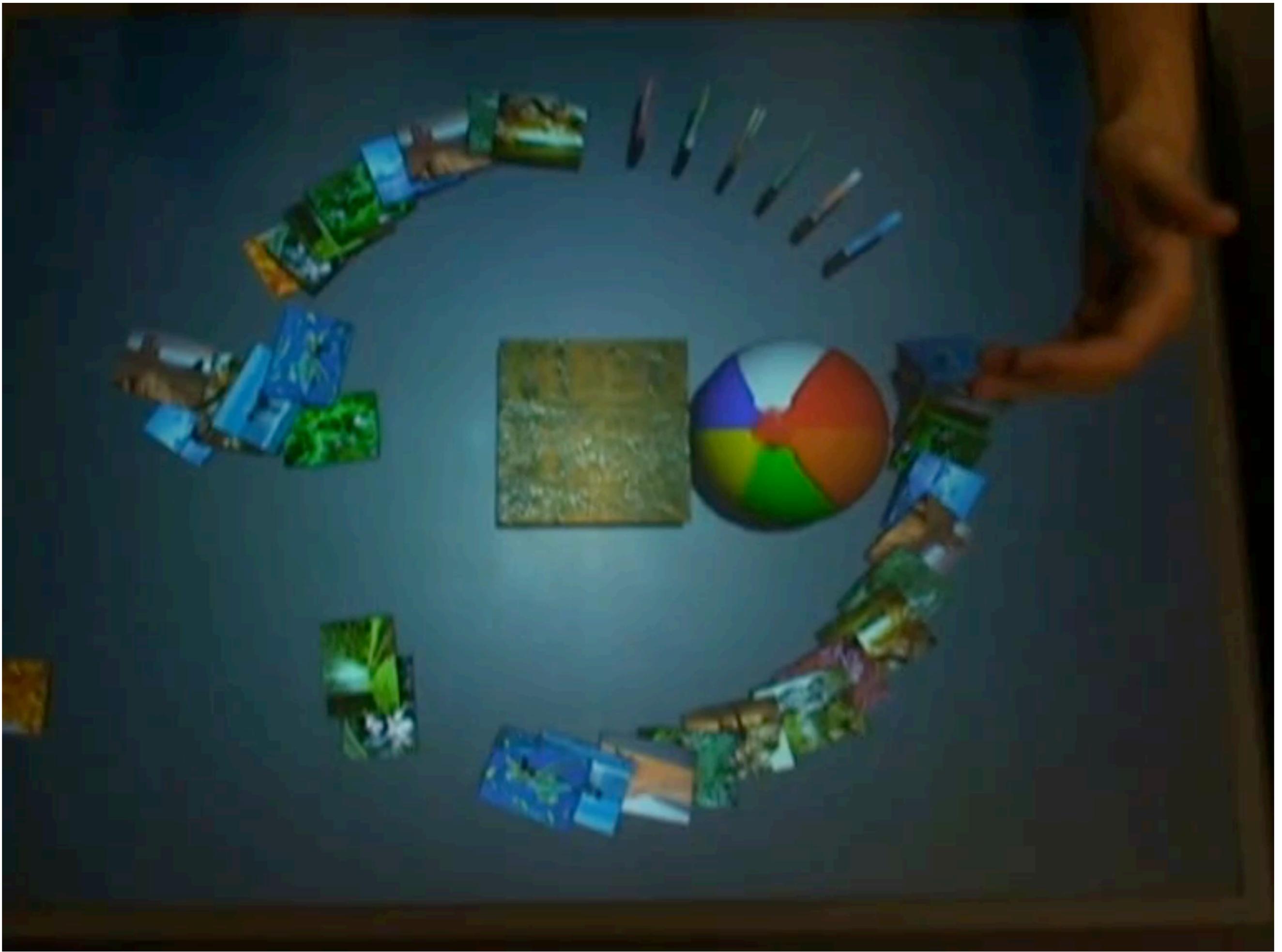
# Manipulation 3D











# Toucheo



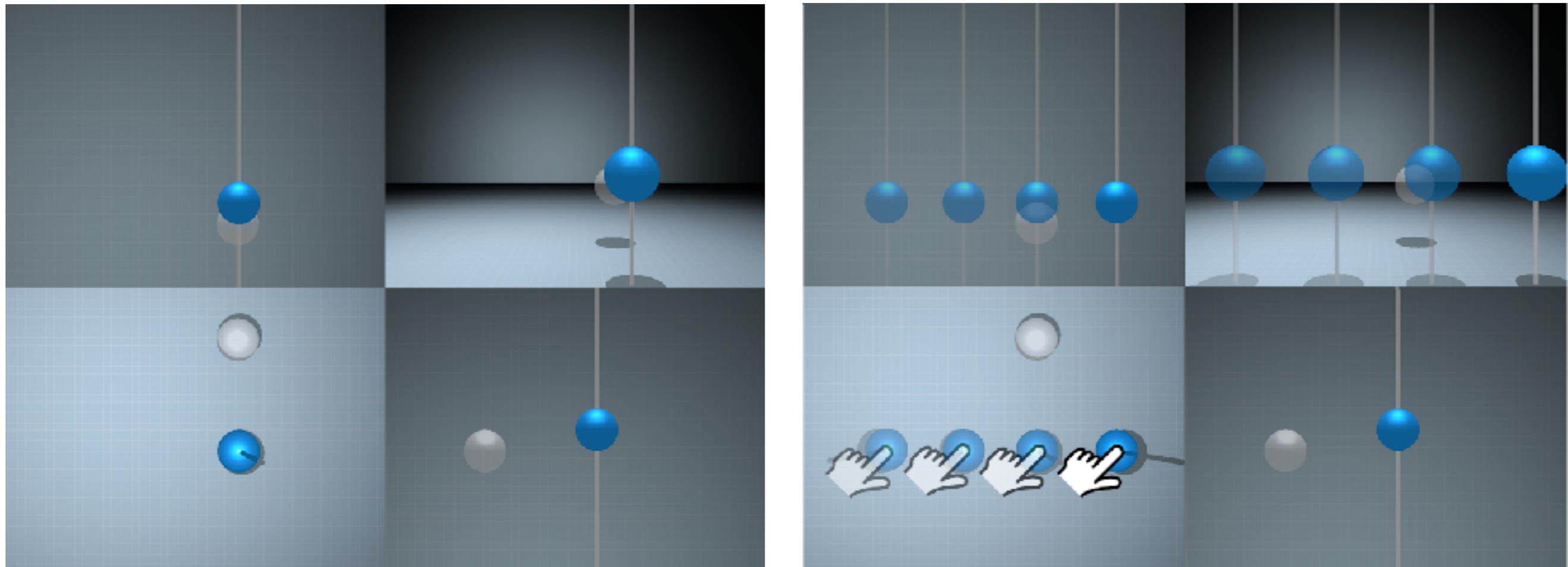
# Toucheo



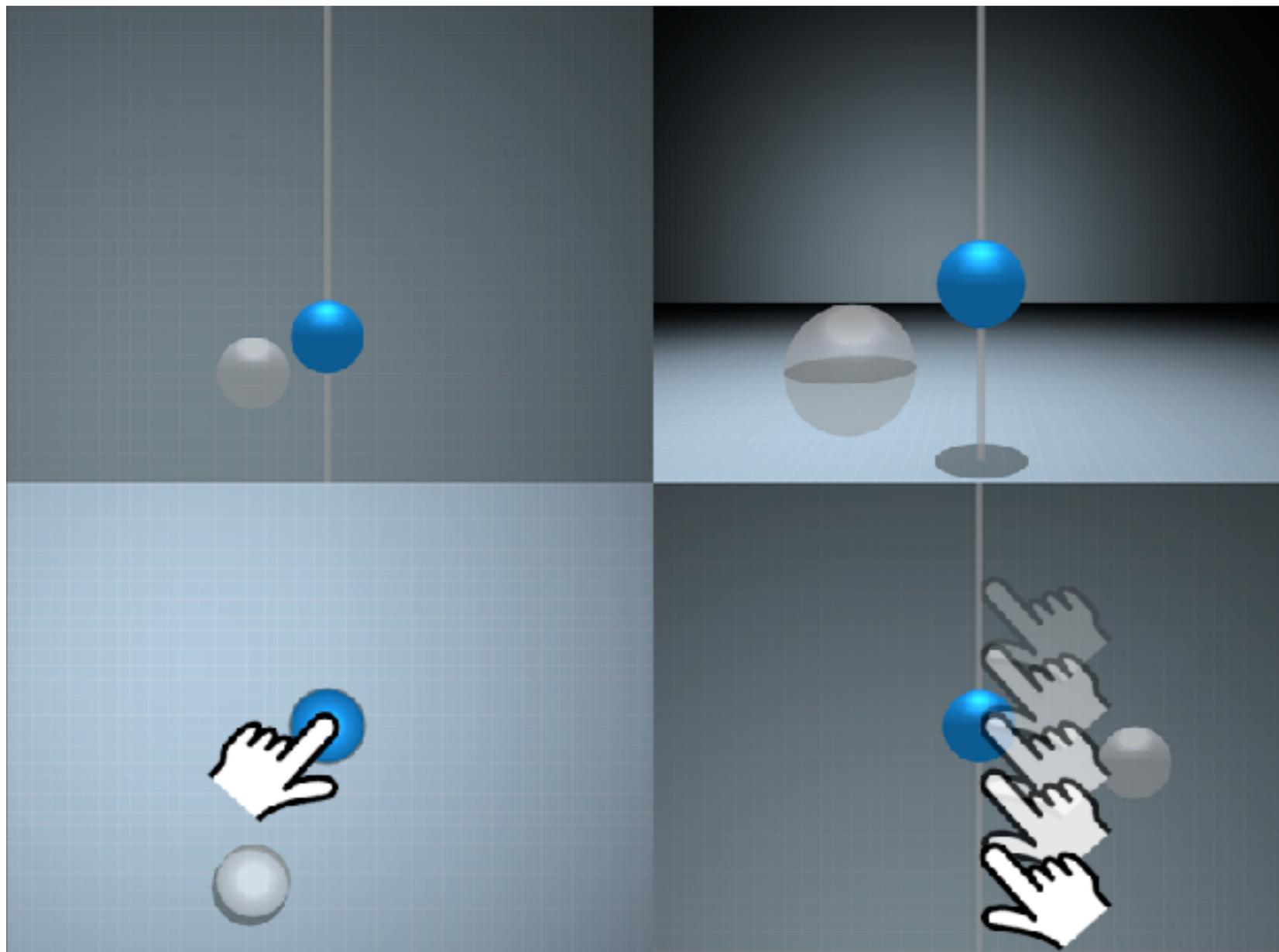
## MT-Viewport

# Amélioration d'une technique traditionnelle

**1 vue = 2 DDL**

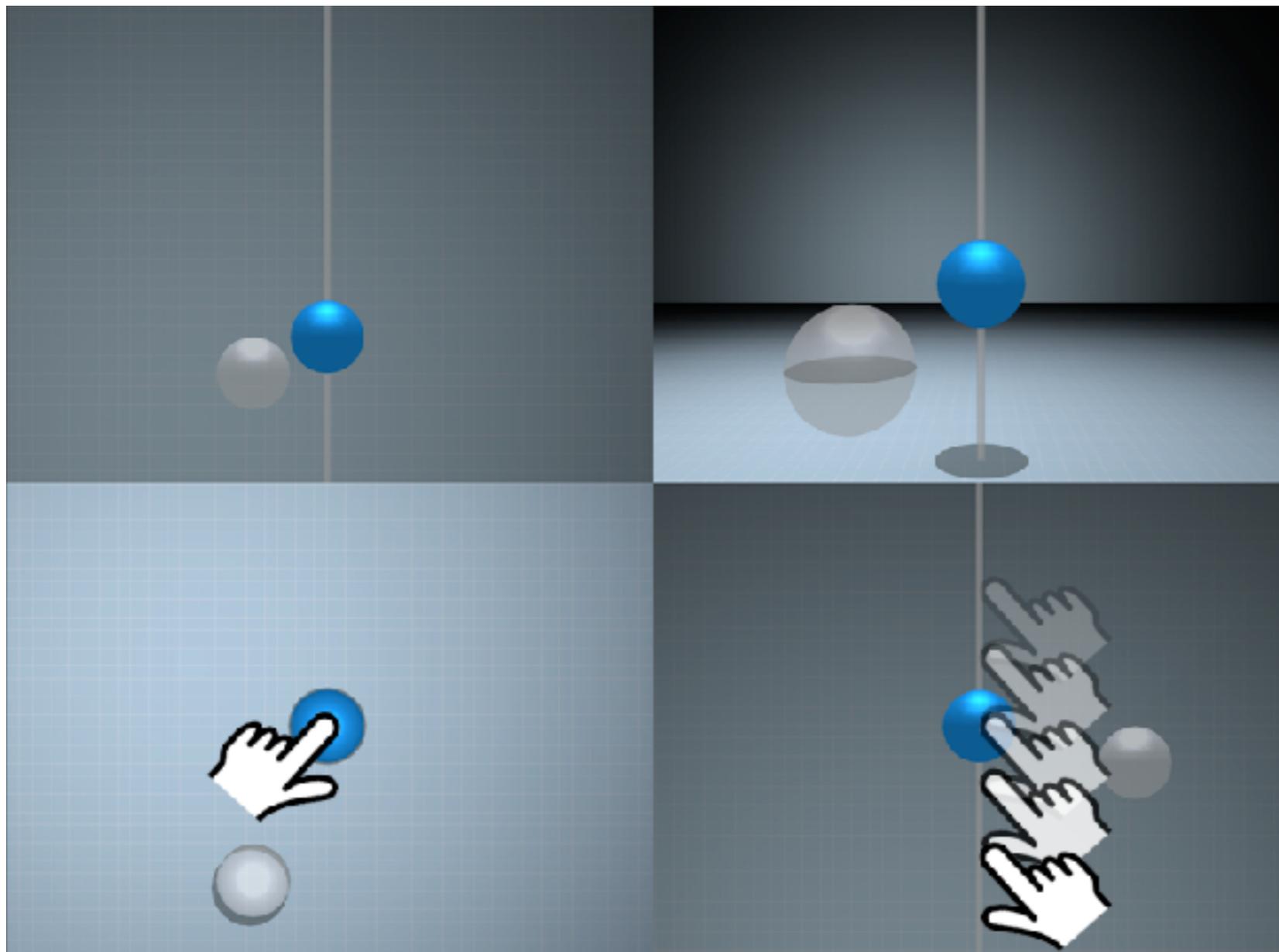


# MT-Viewport

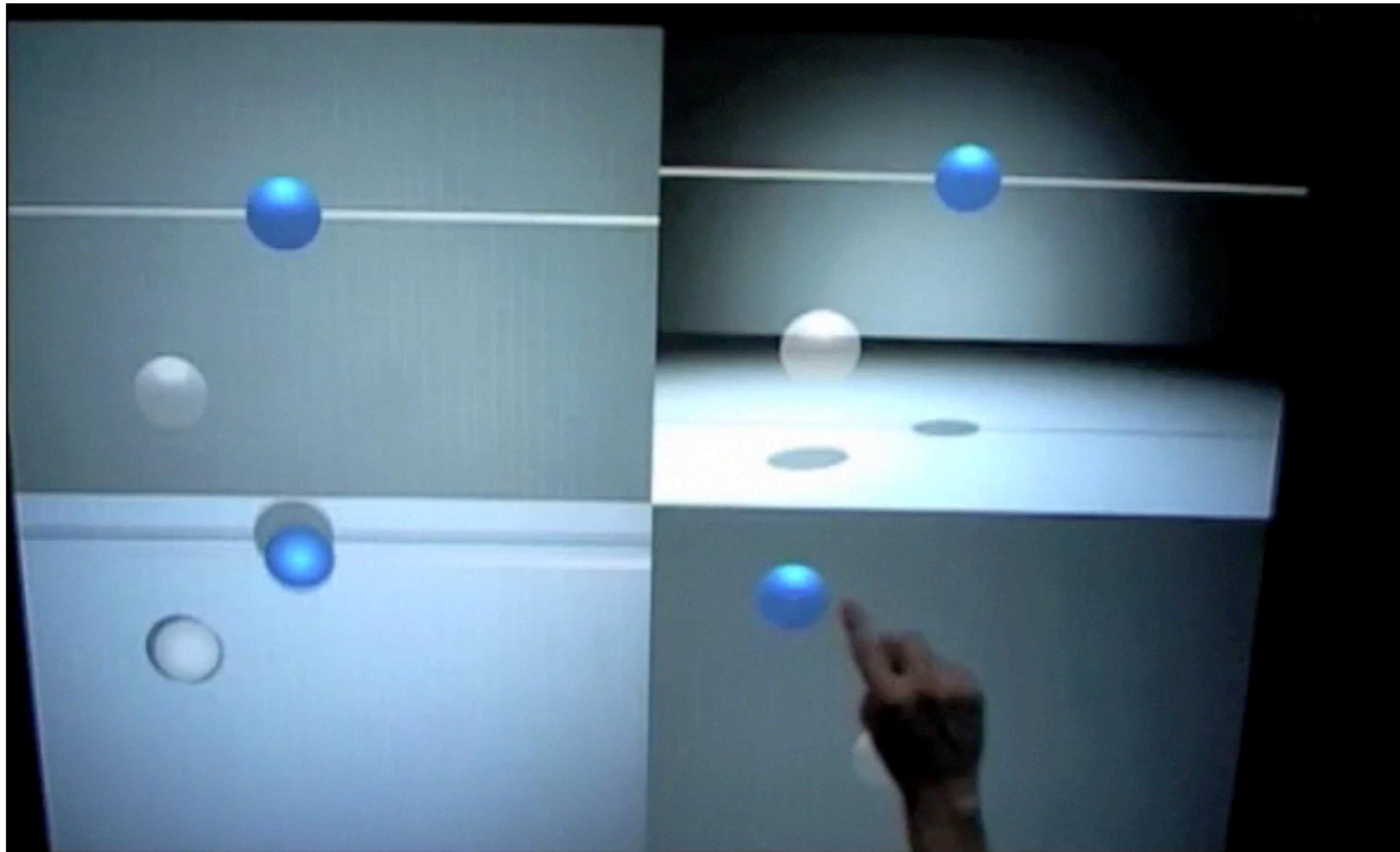


# MT-Viewport

## 3ème DDL dans les autres vues

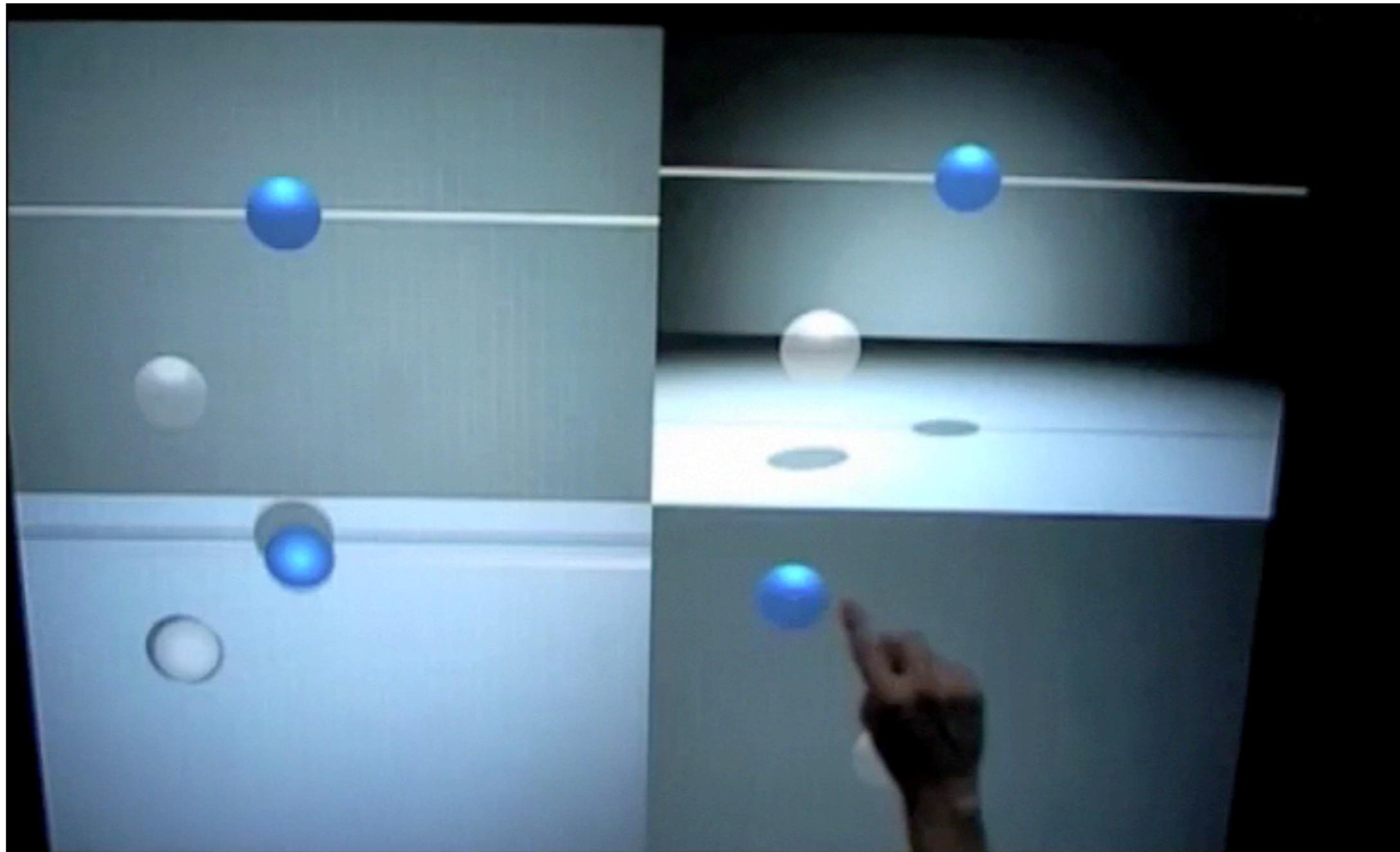


# MT-Viewport



Control of 2 DOF on each viewport  
like the 4-view technique

# MT-Viewport



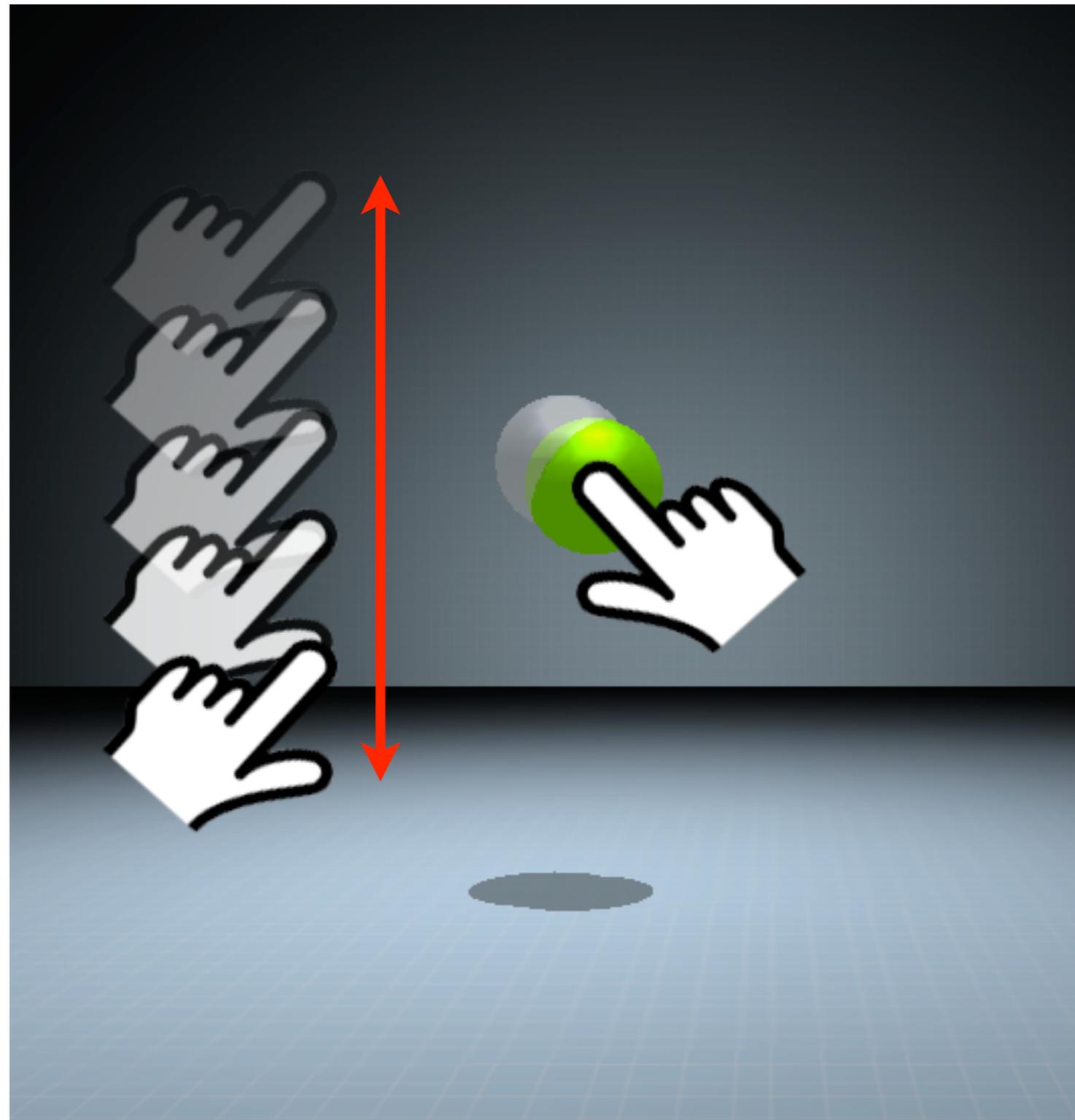
Control of 2 DOF on each viewport  
like the 4-view technique

## Z-technique

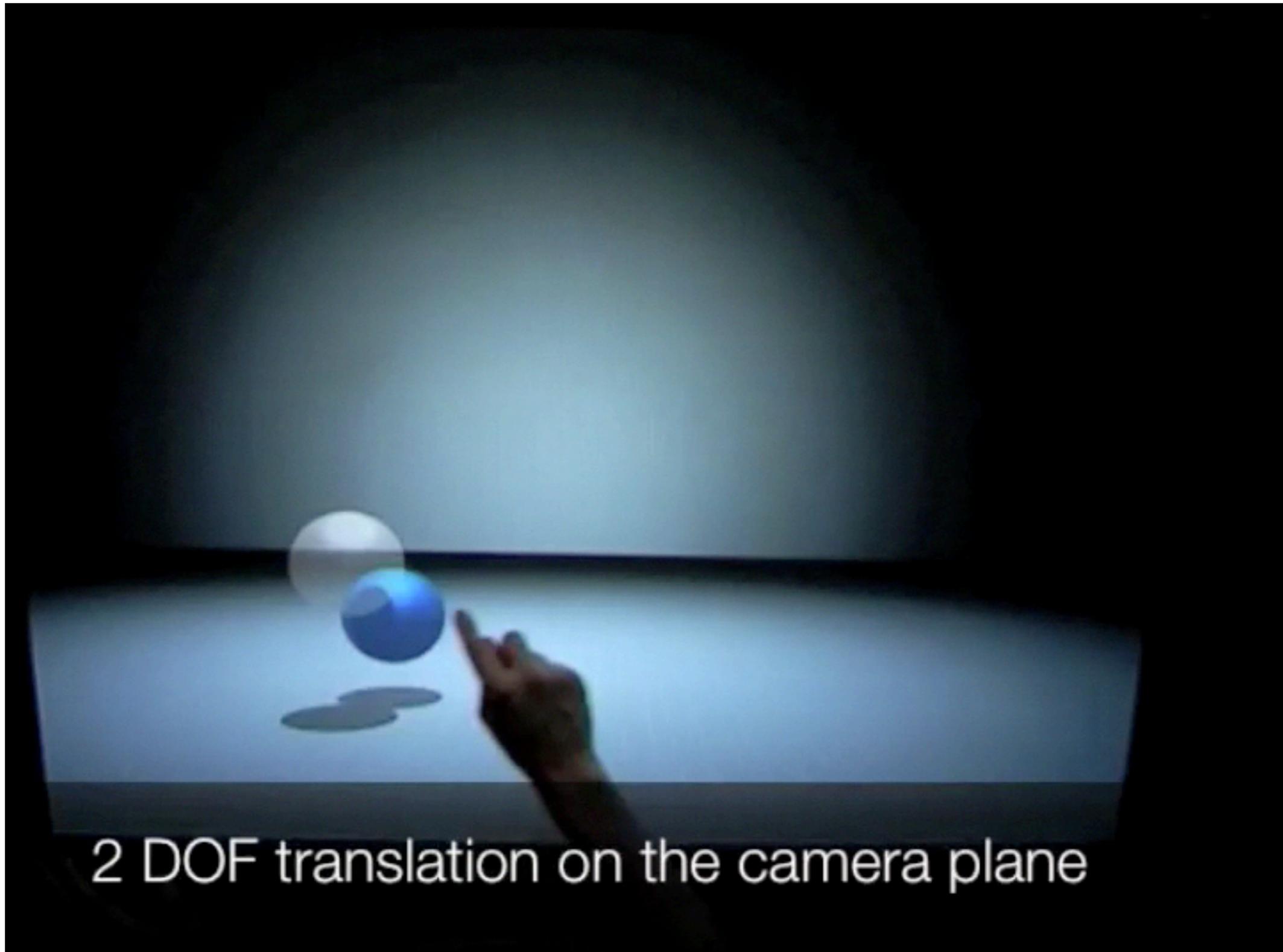
1 doigt : 2 DDL

Doigt indirect :

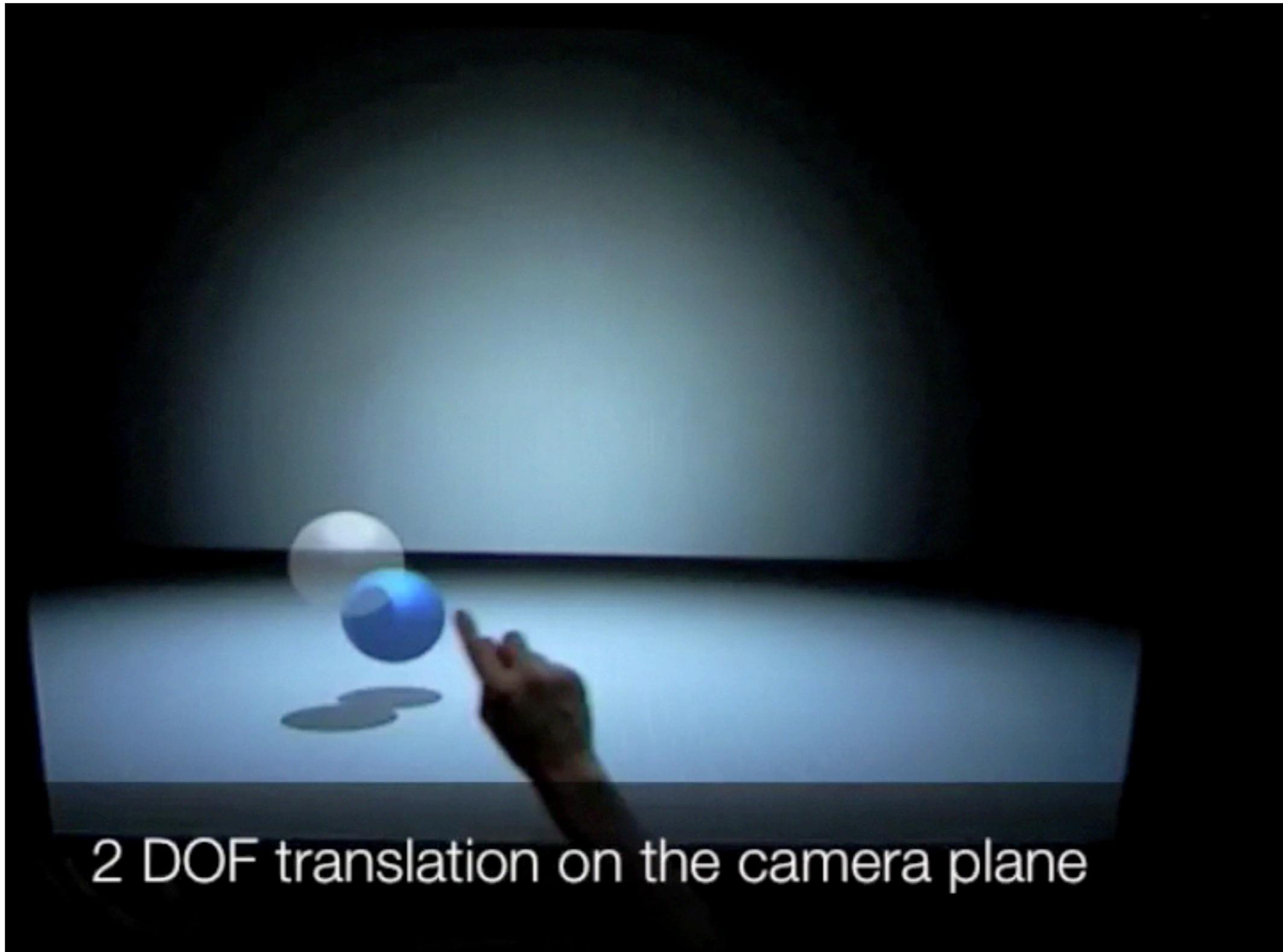
dernier DDL



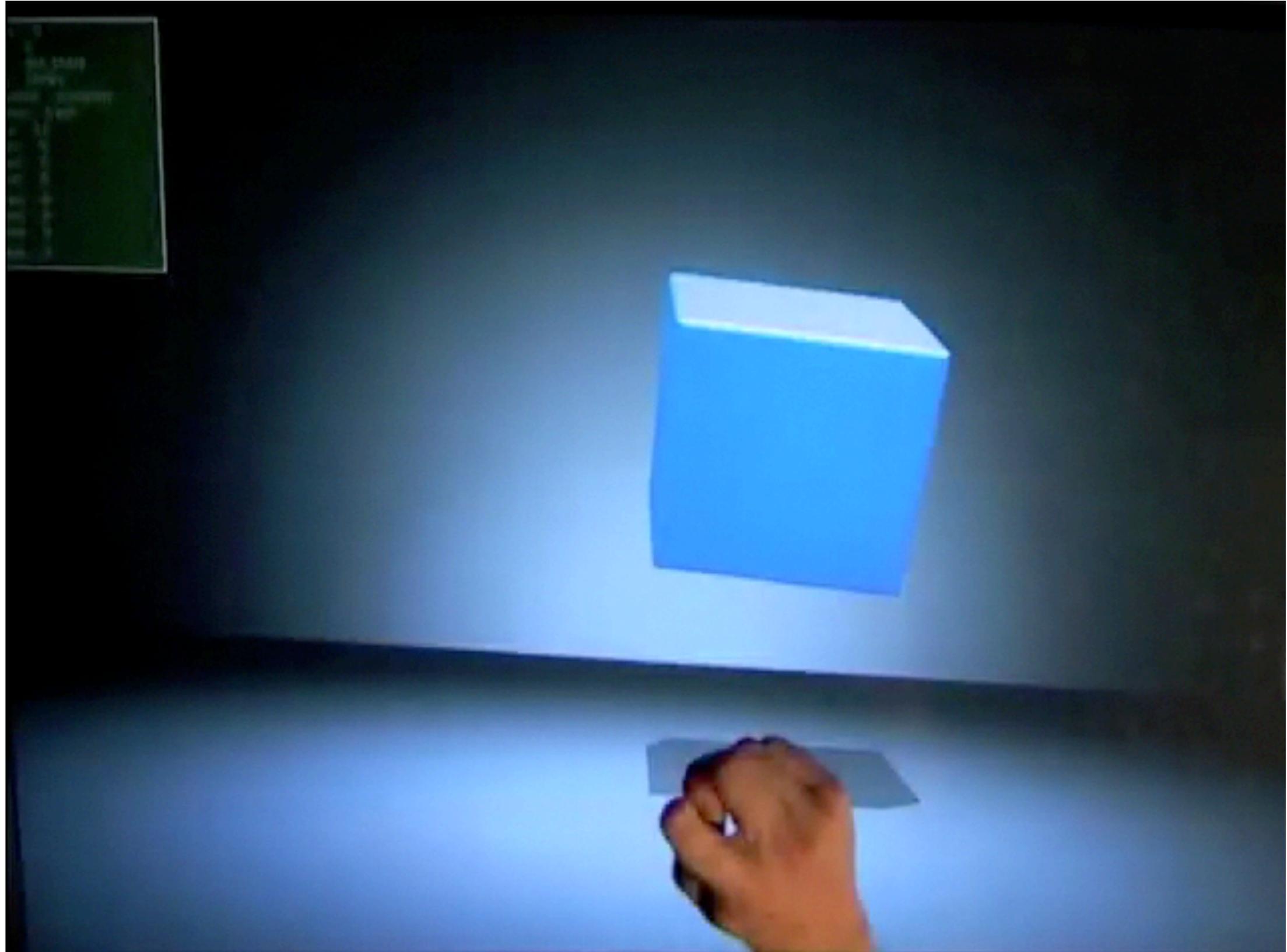
# Z-technique



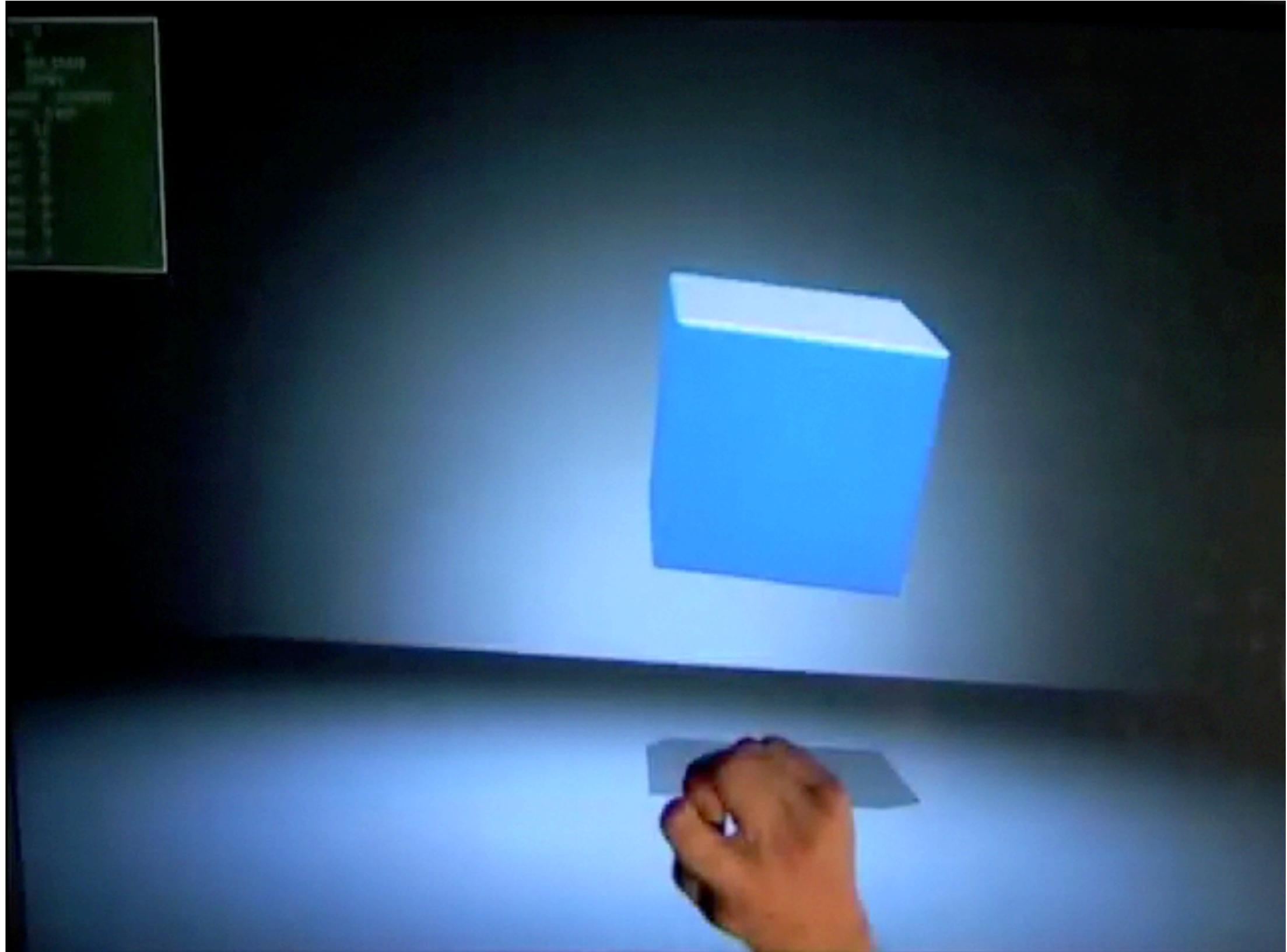
# Z-technique



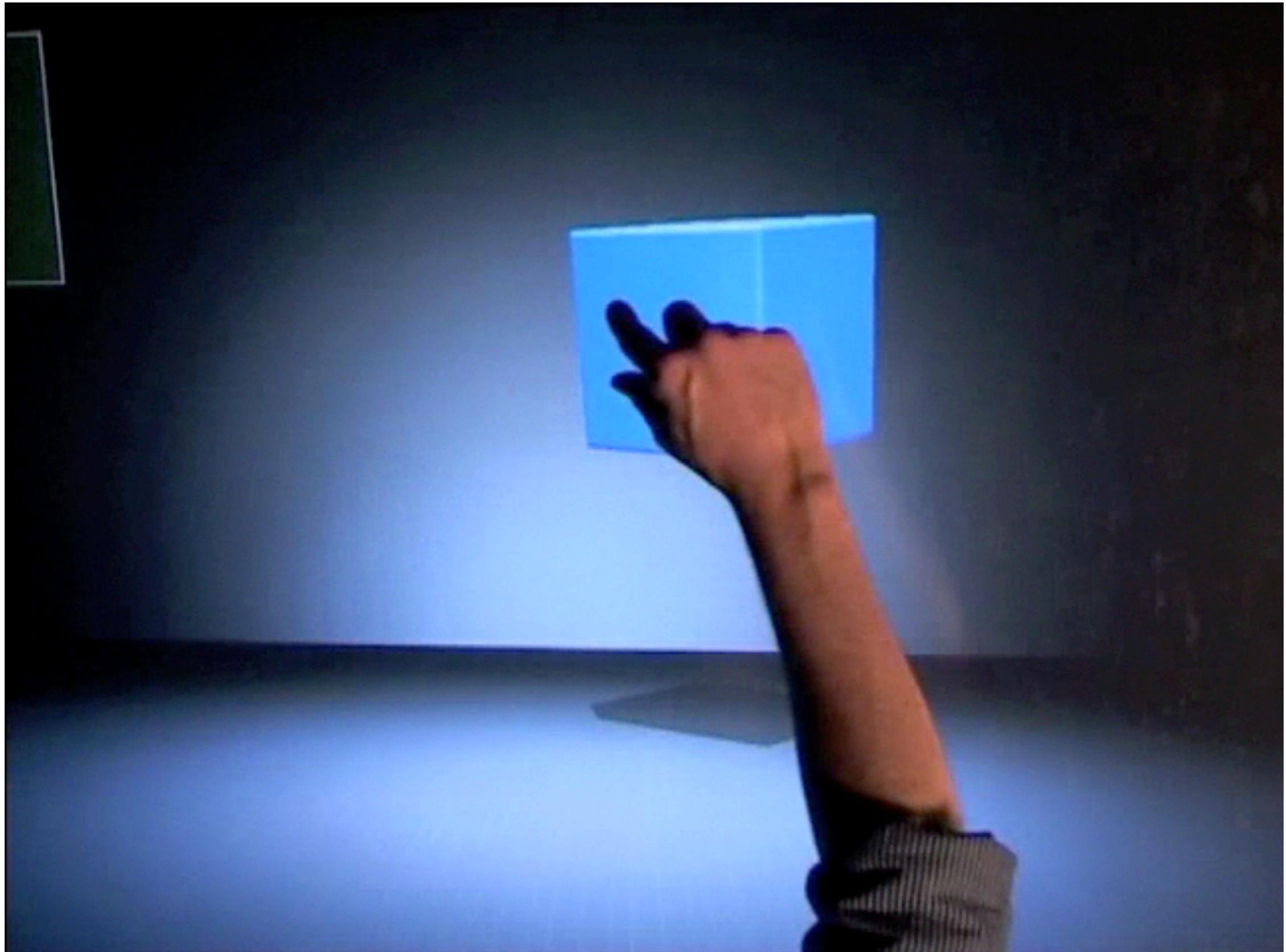
## Sticky Tools [Hancock et al. 2009]



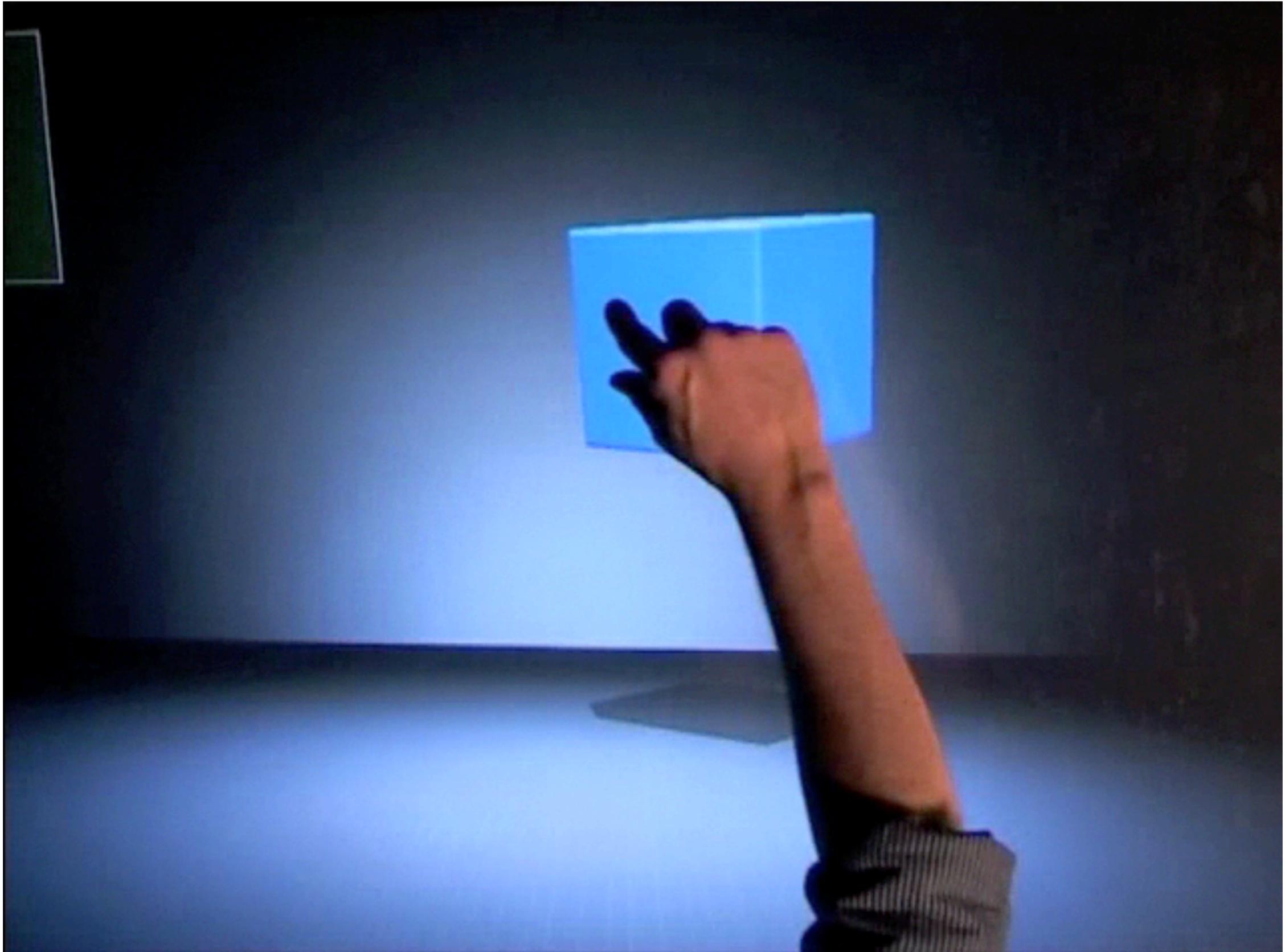
## Sticky Tools [Hancock et al. 2009]



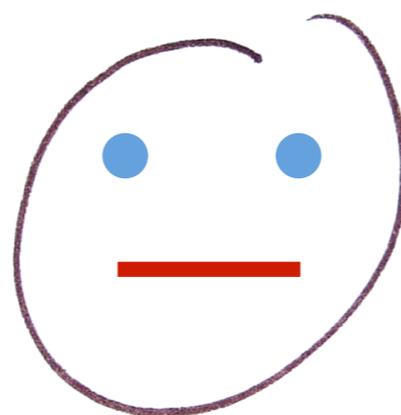
## Screenspace [Reisman et al. 2009]



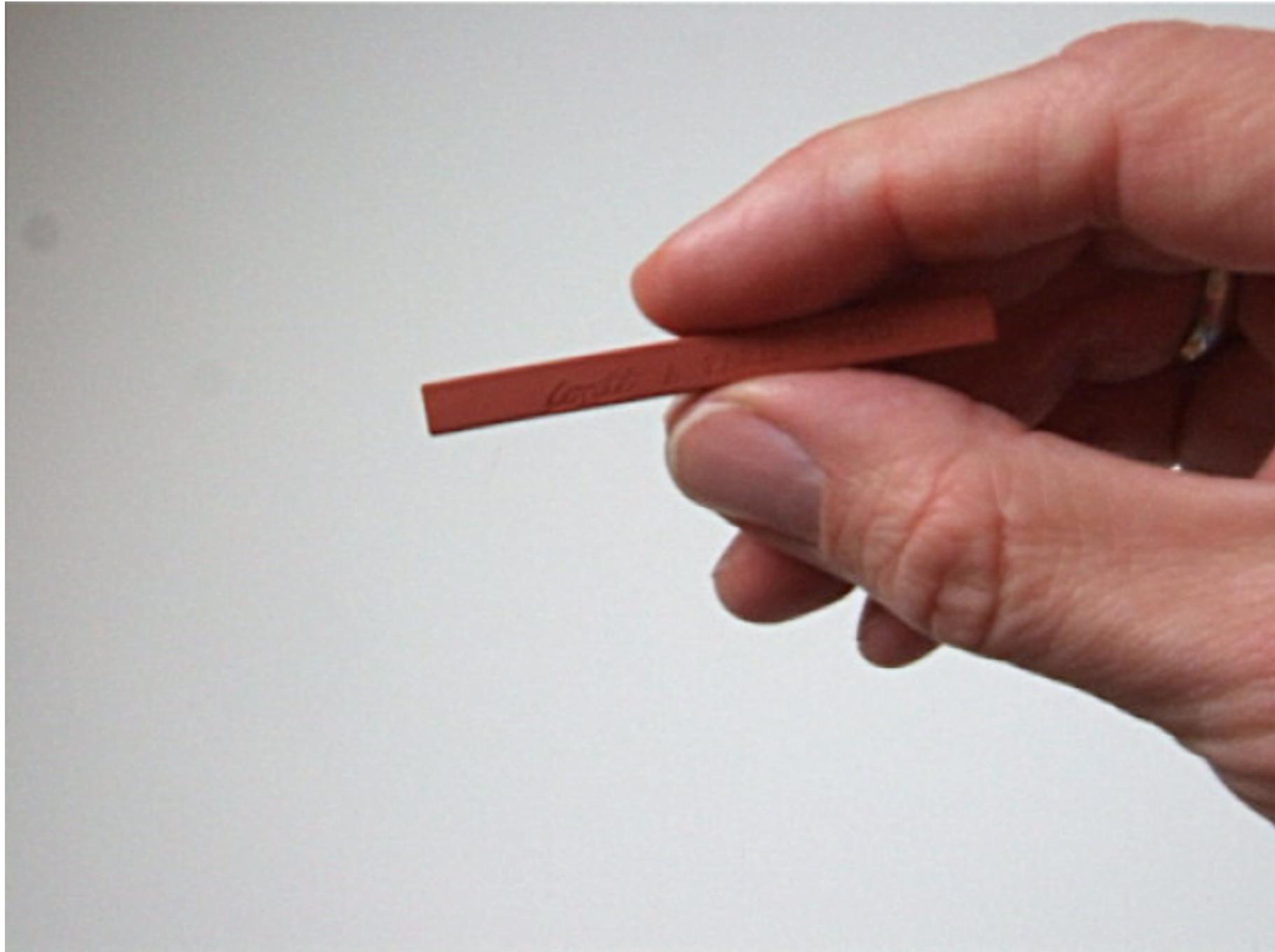
## Screenspace [Reisman et al. 2009]



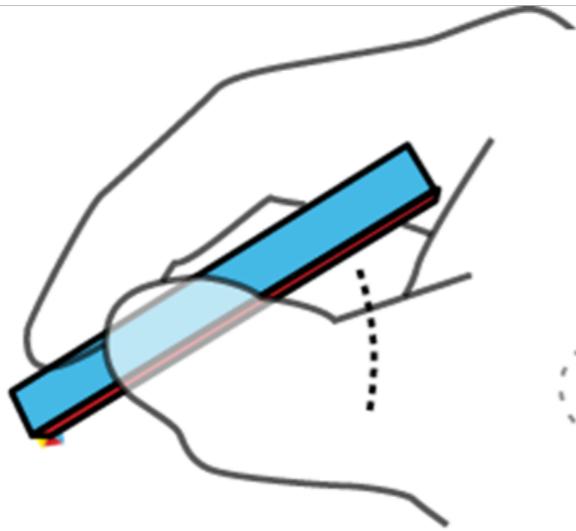
# Conté [Vogel & Casiez 2011]



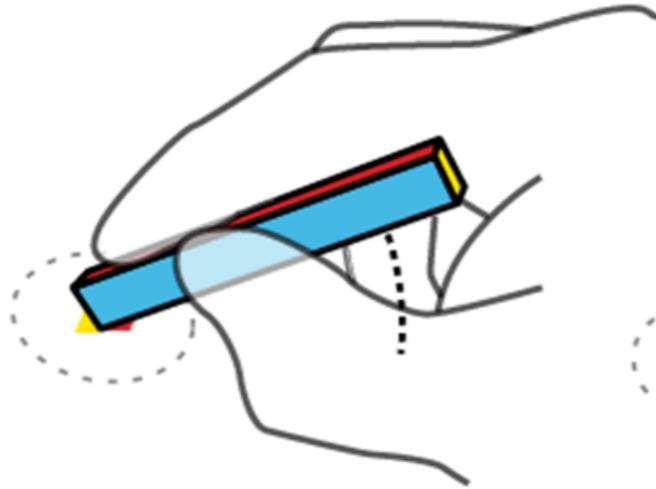
# Conté



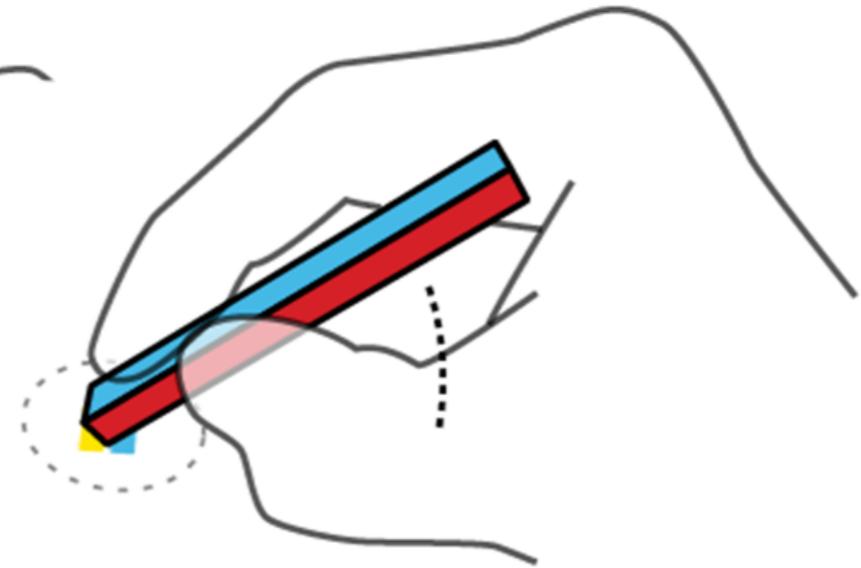
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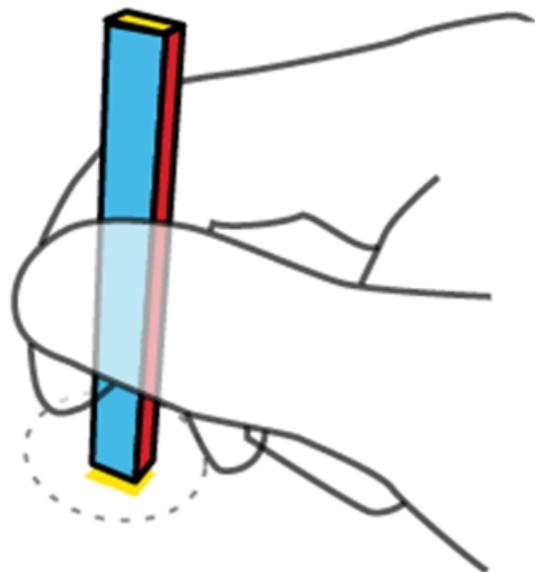
corner



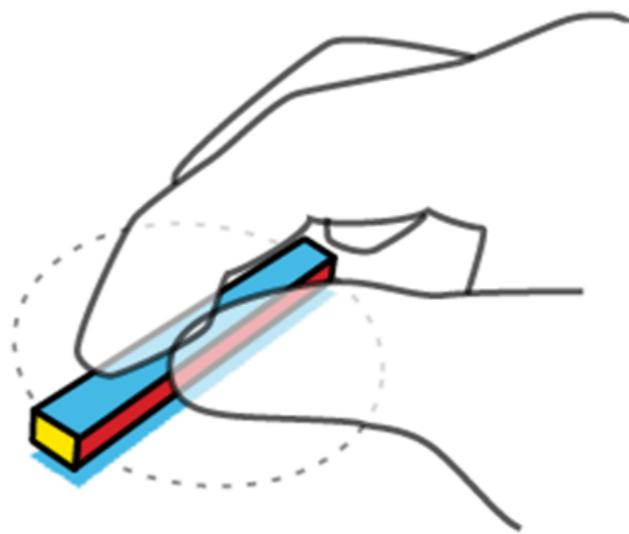
short end edge



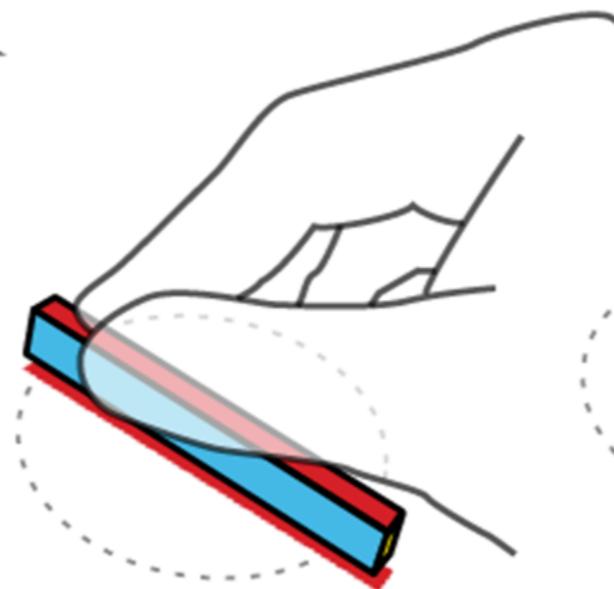
medium end edge



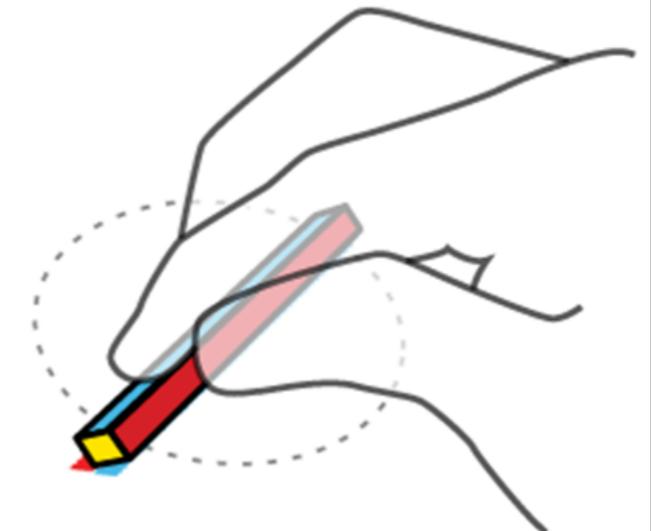
end



thick side

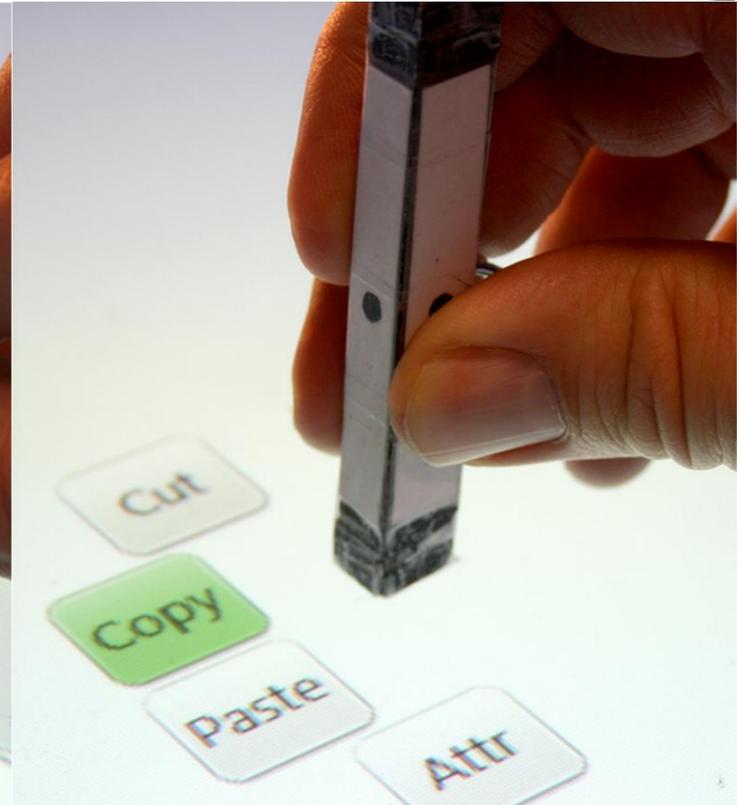
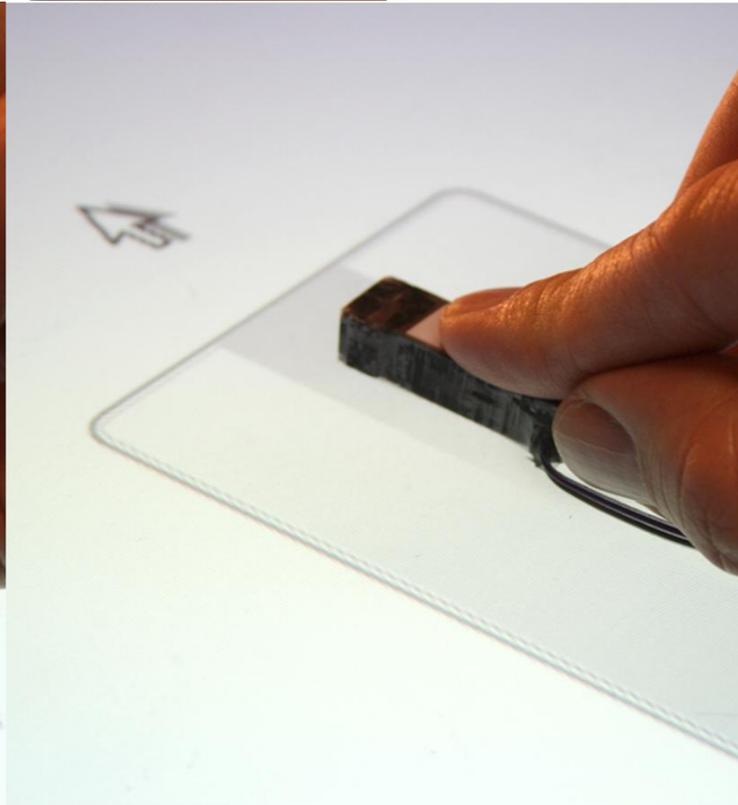
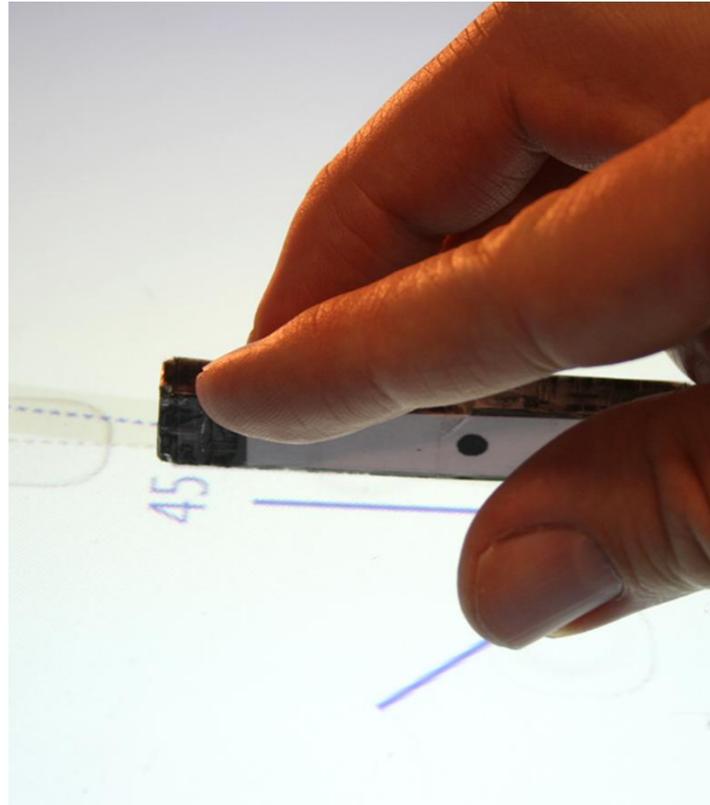
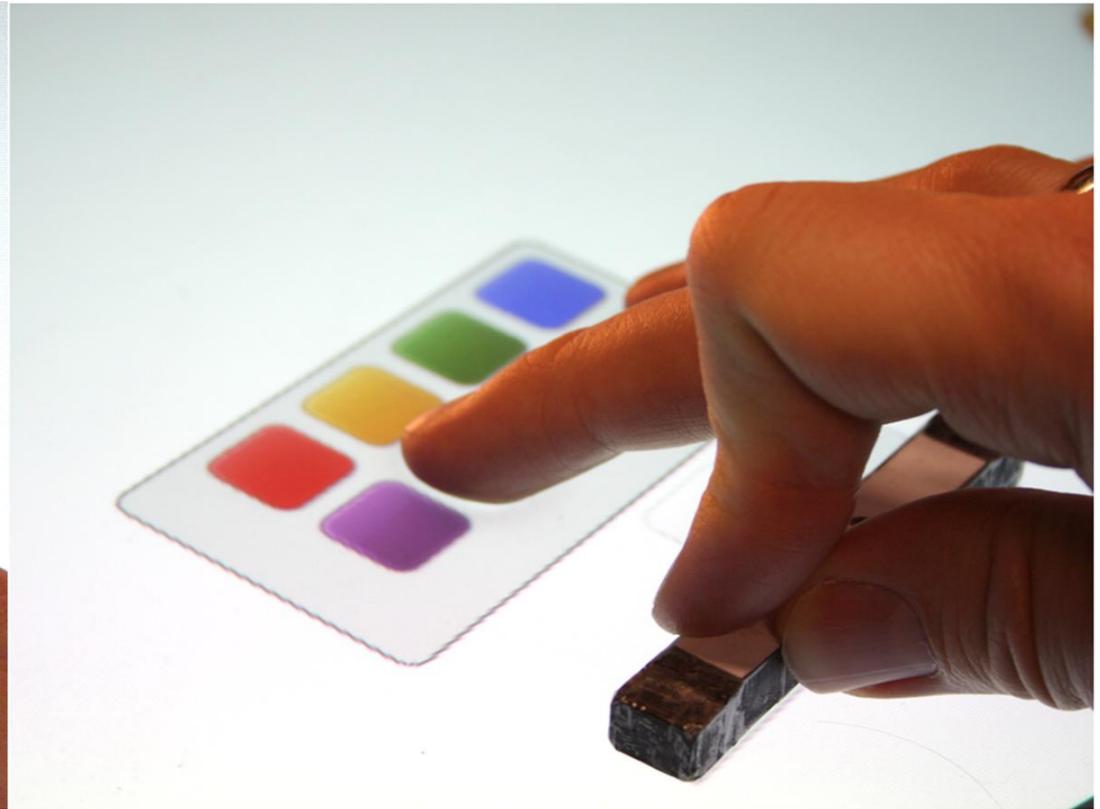
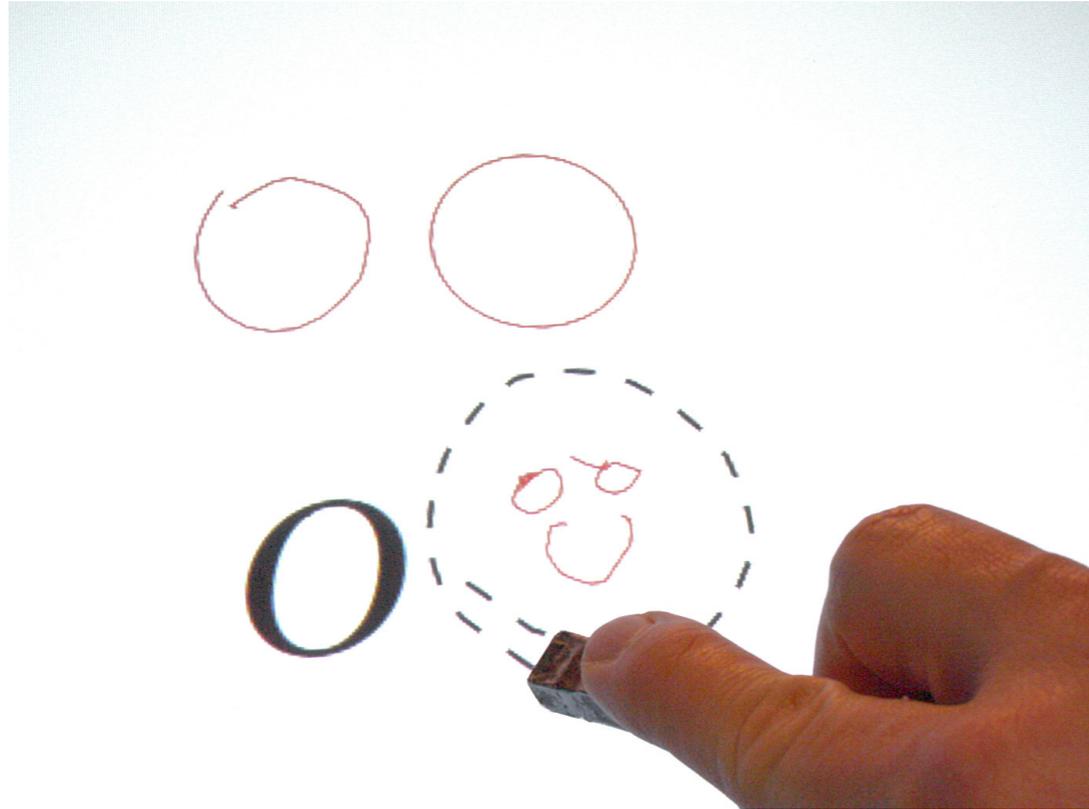


thin side

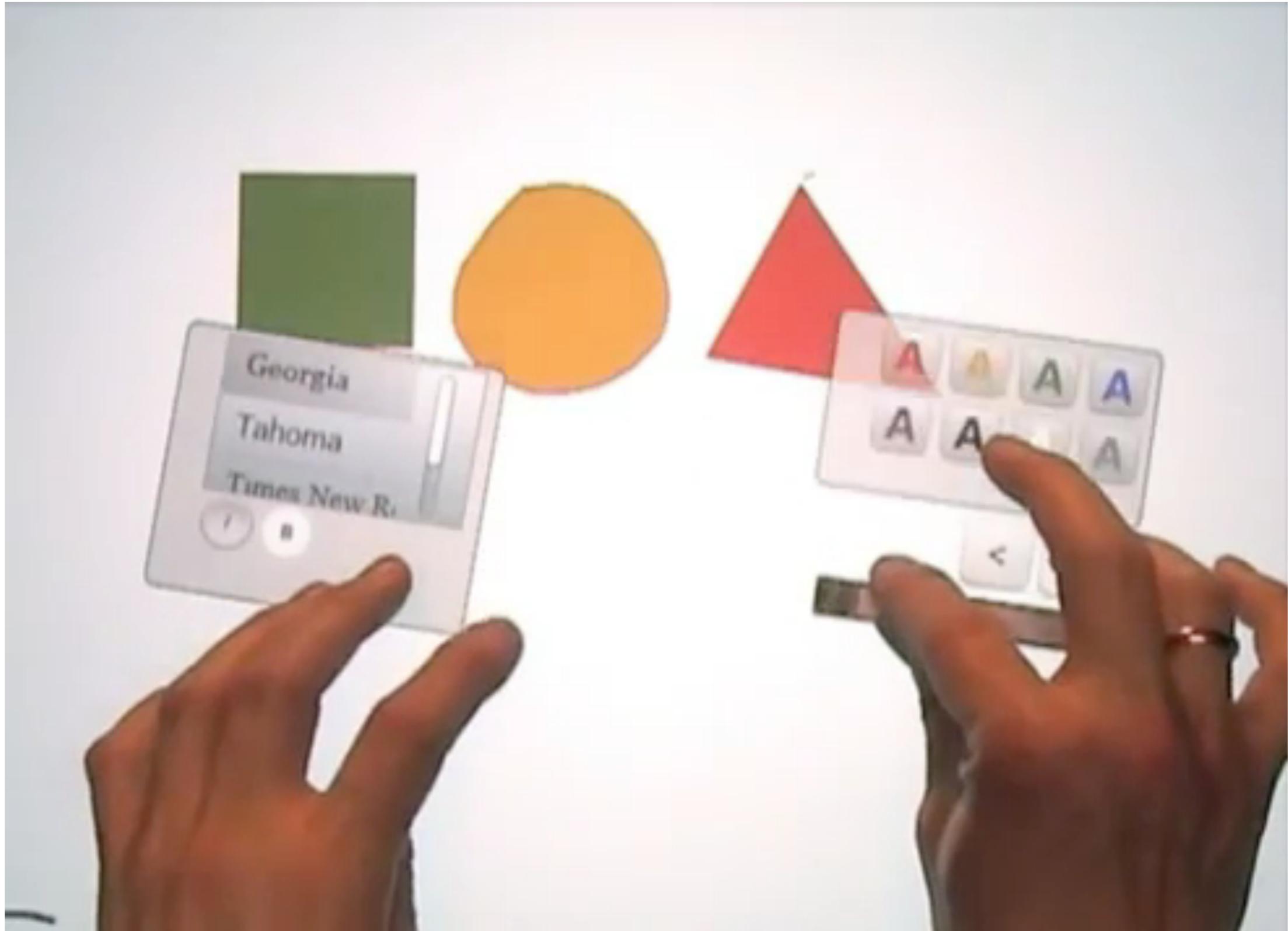


long side edge

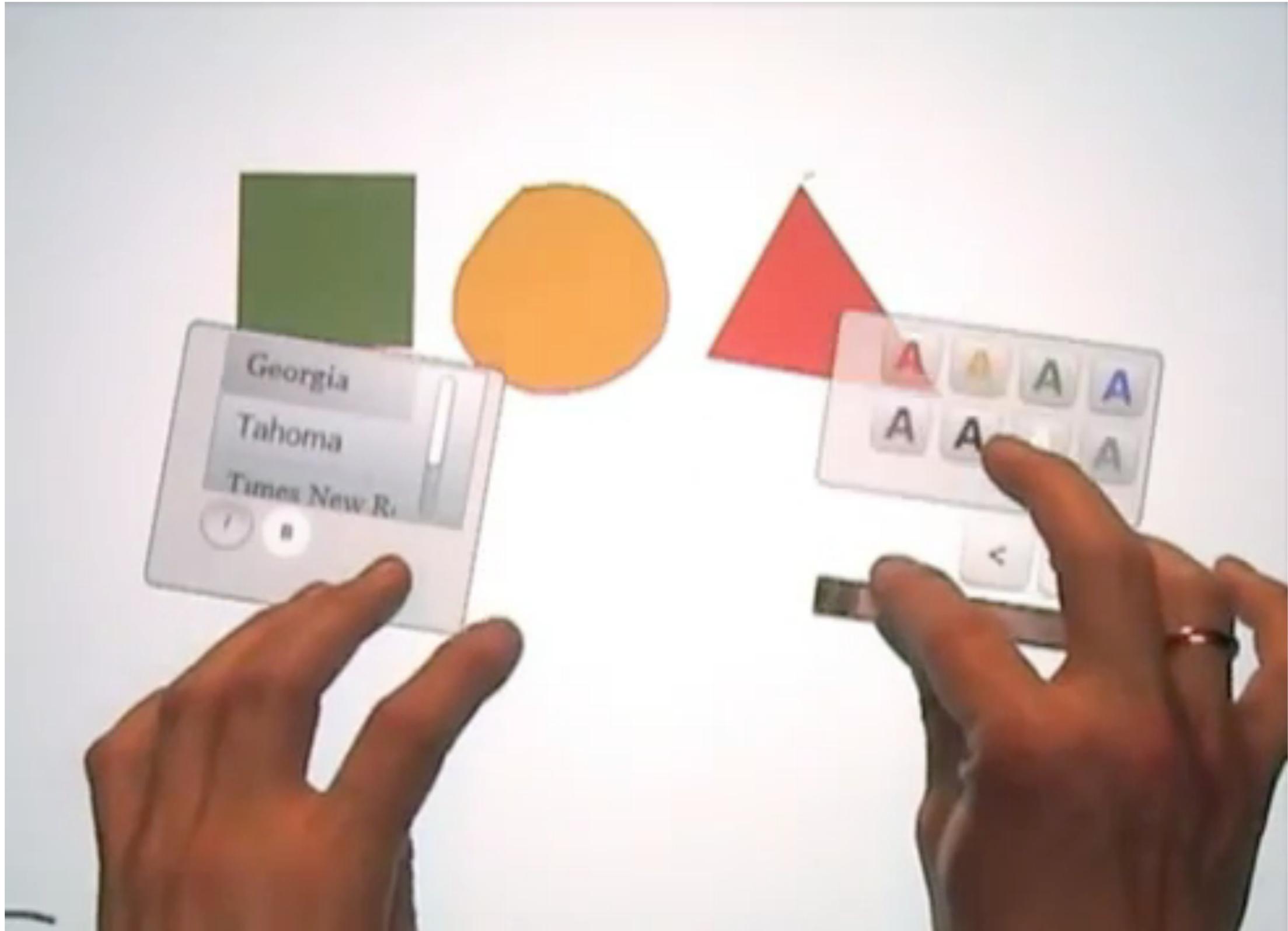
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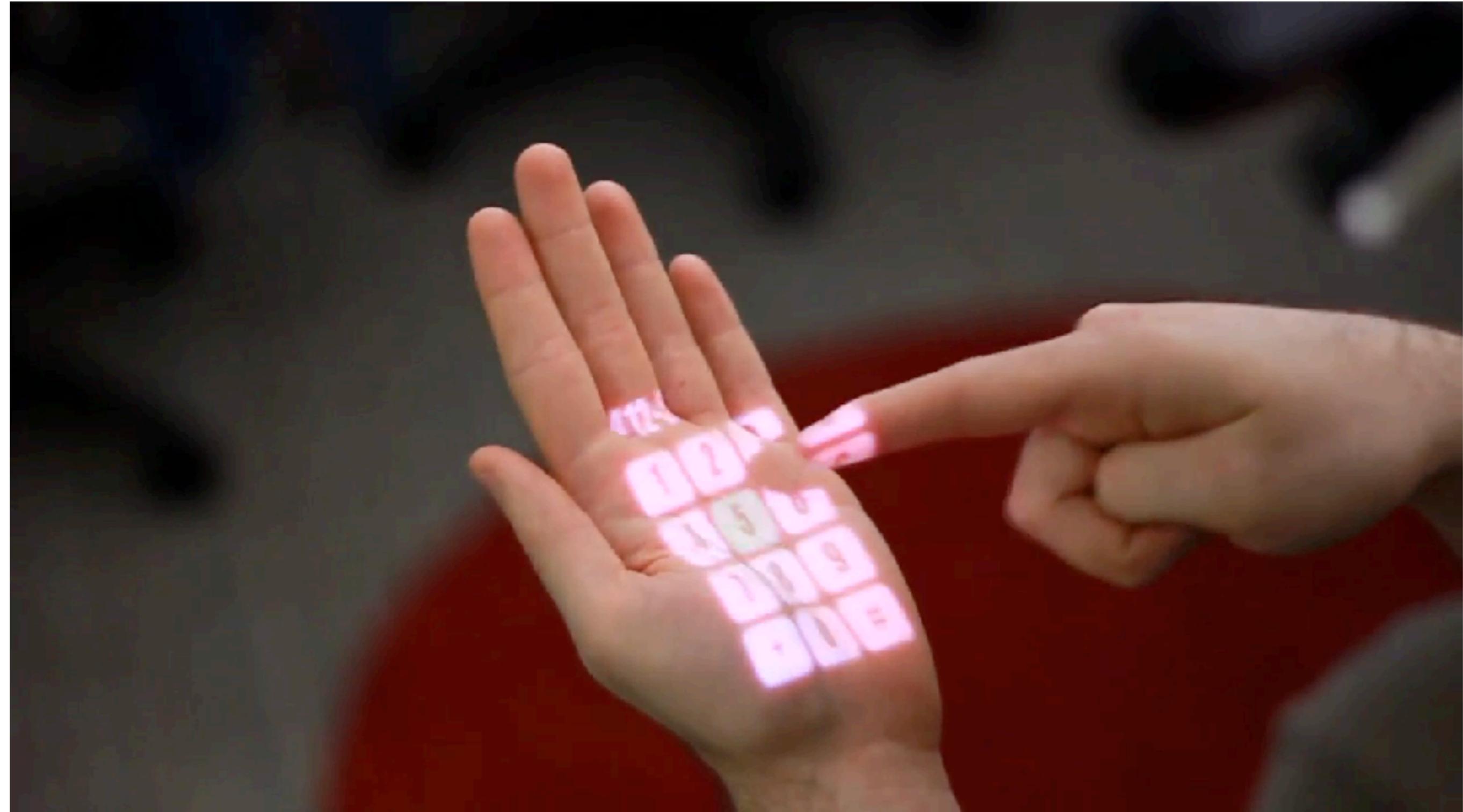


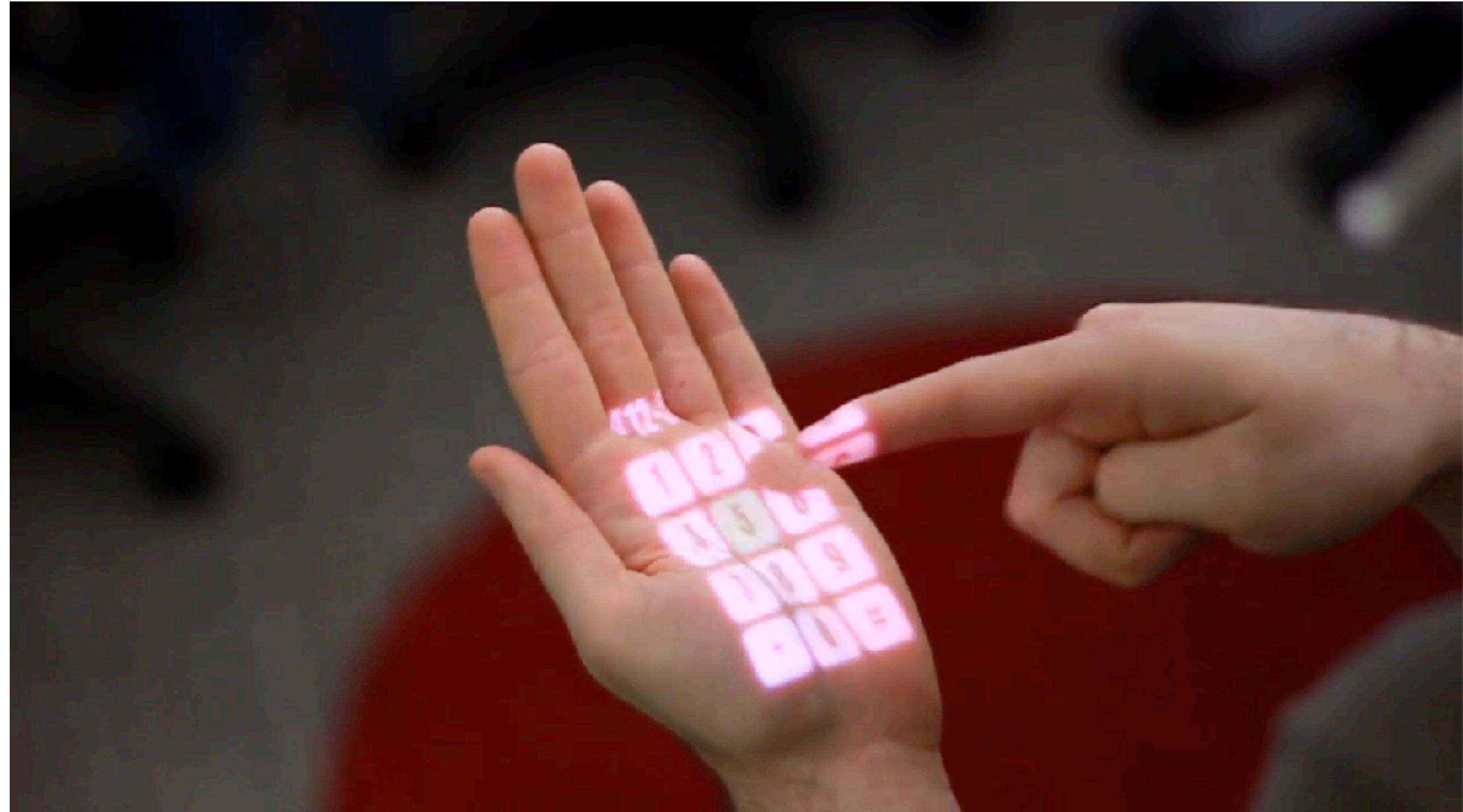
# Conté

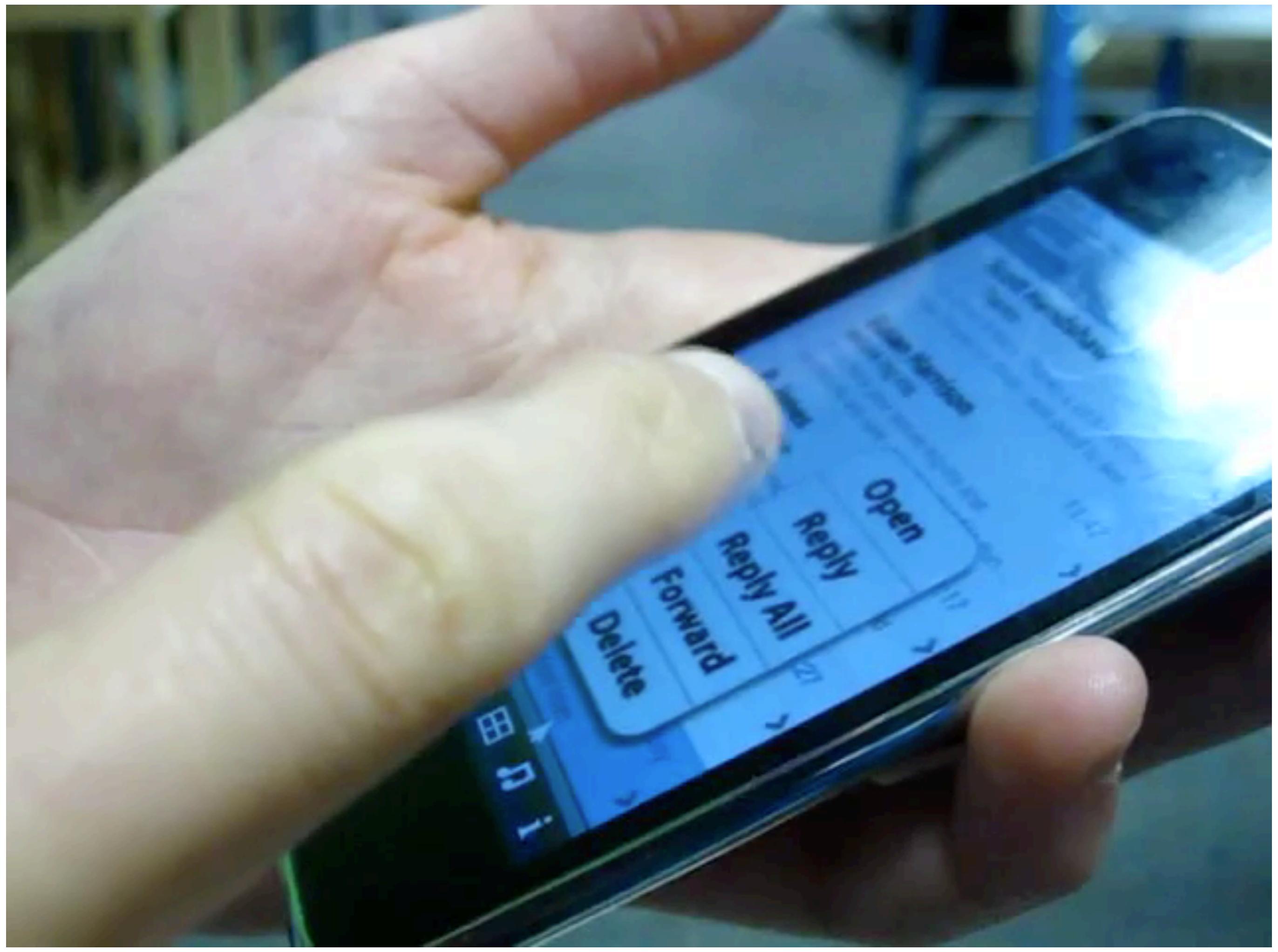


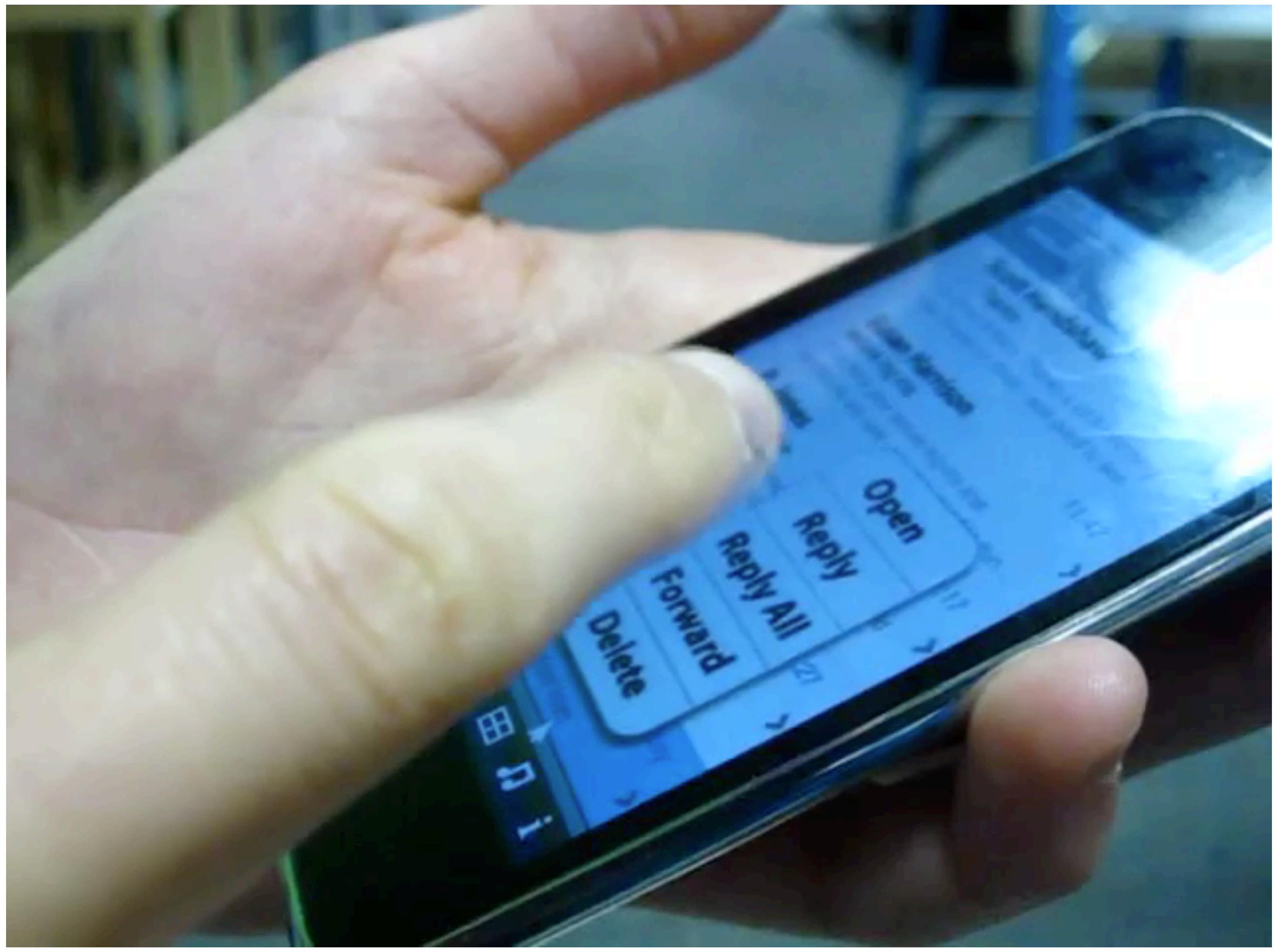
# Conté











## Forces tangentielle

The film plate is used for detecting tangential force

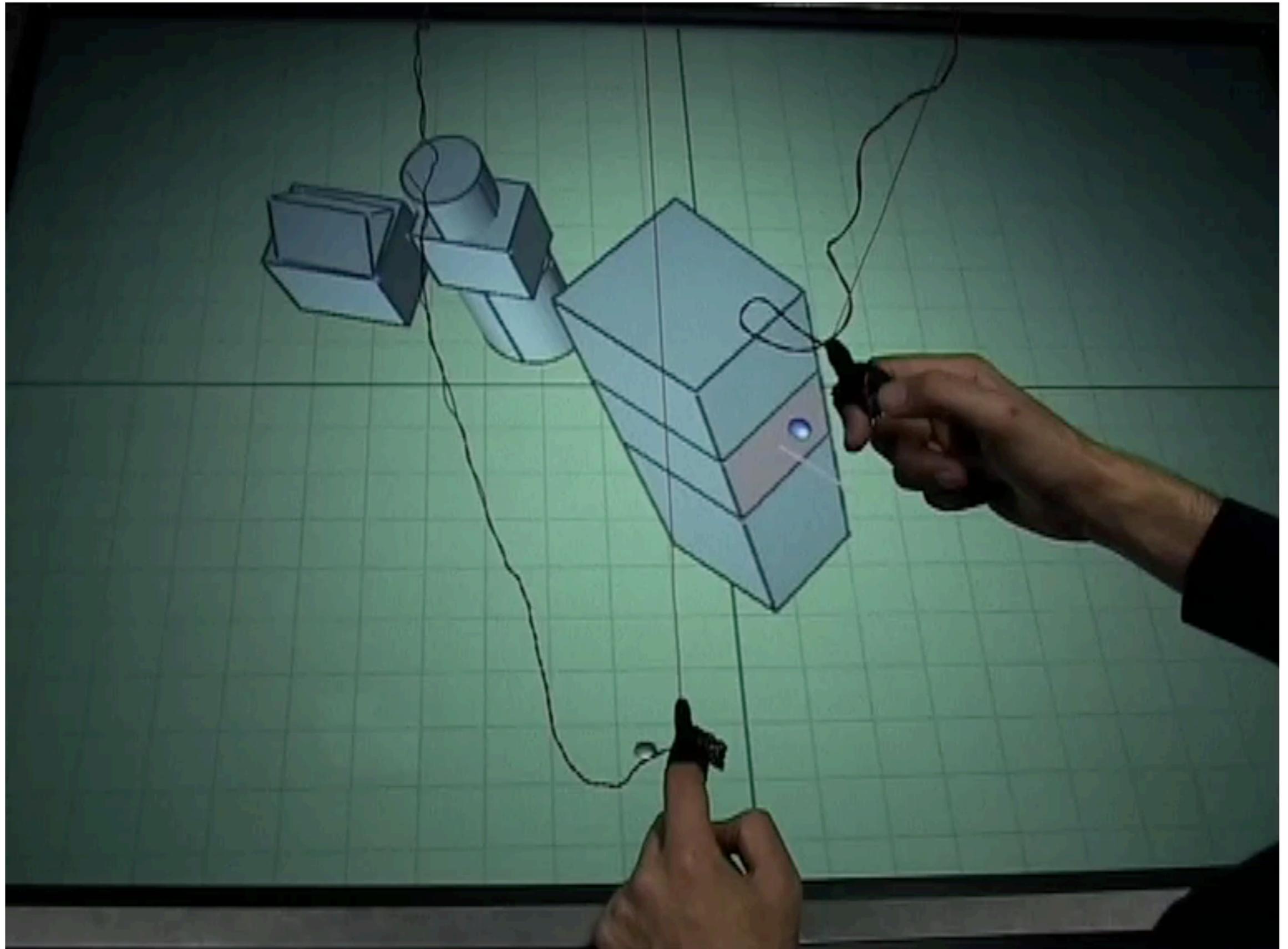


## Forces tangentielle

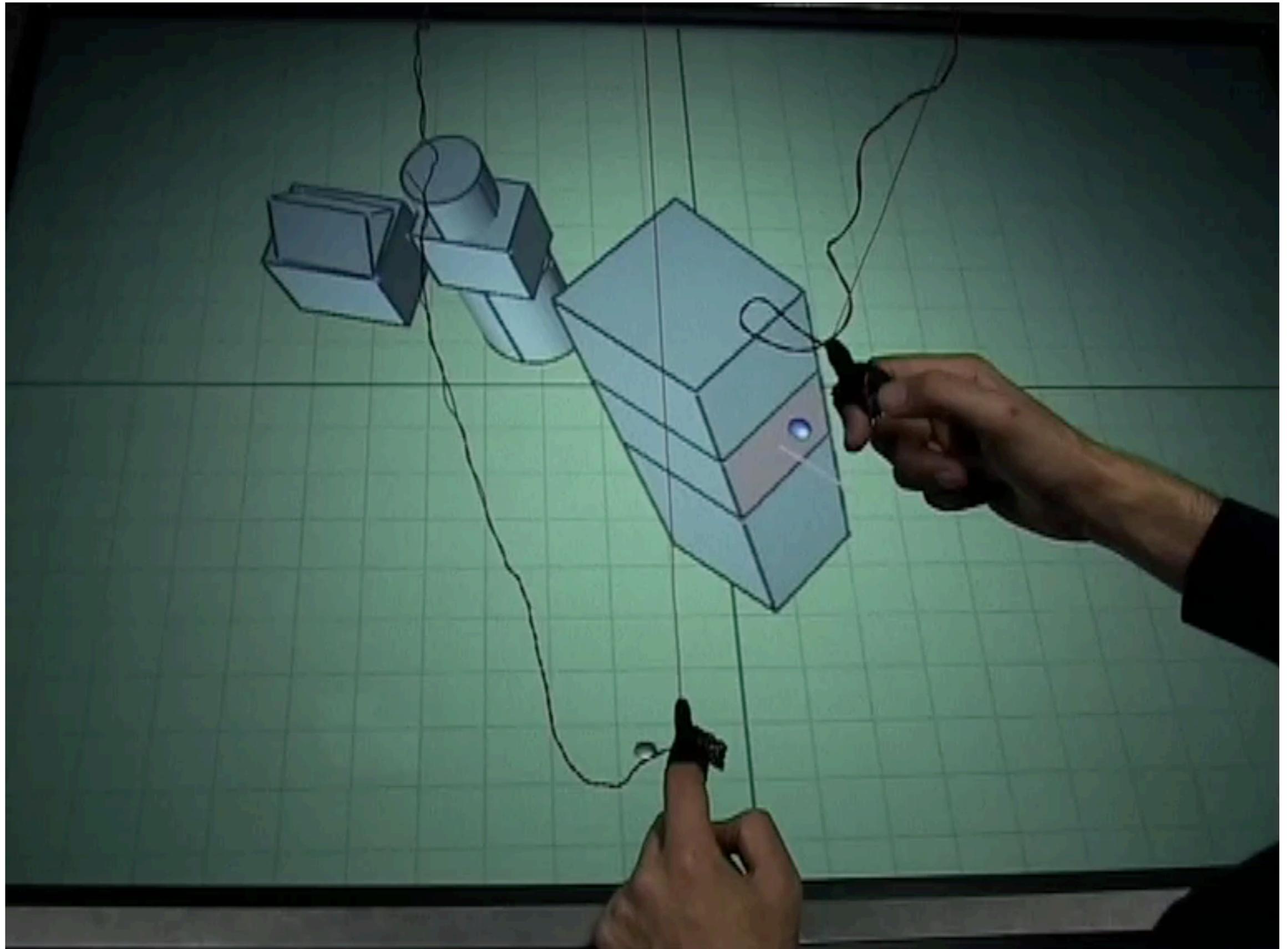
The film plate is used for detecting tangential force



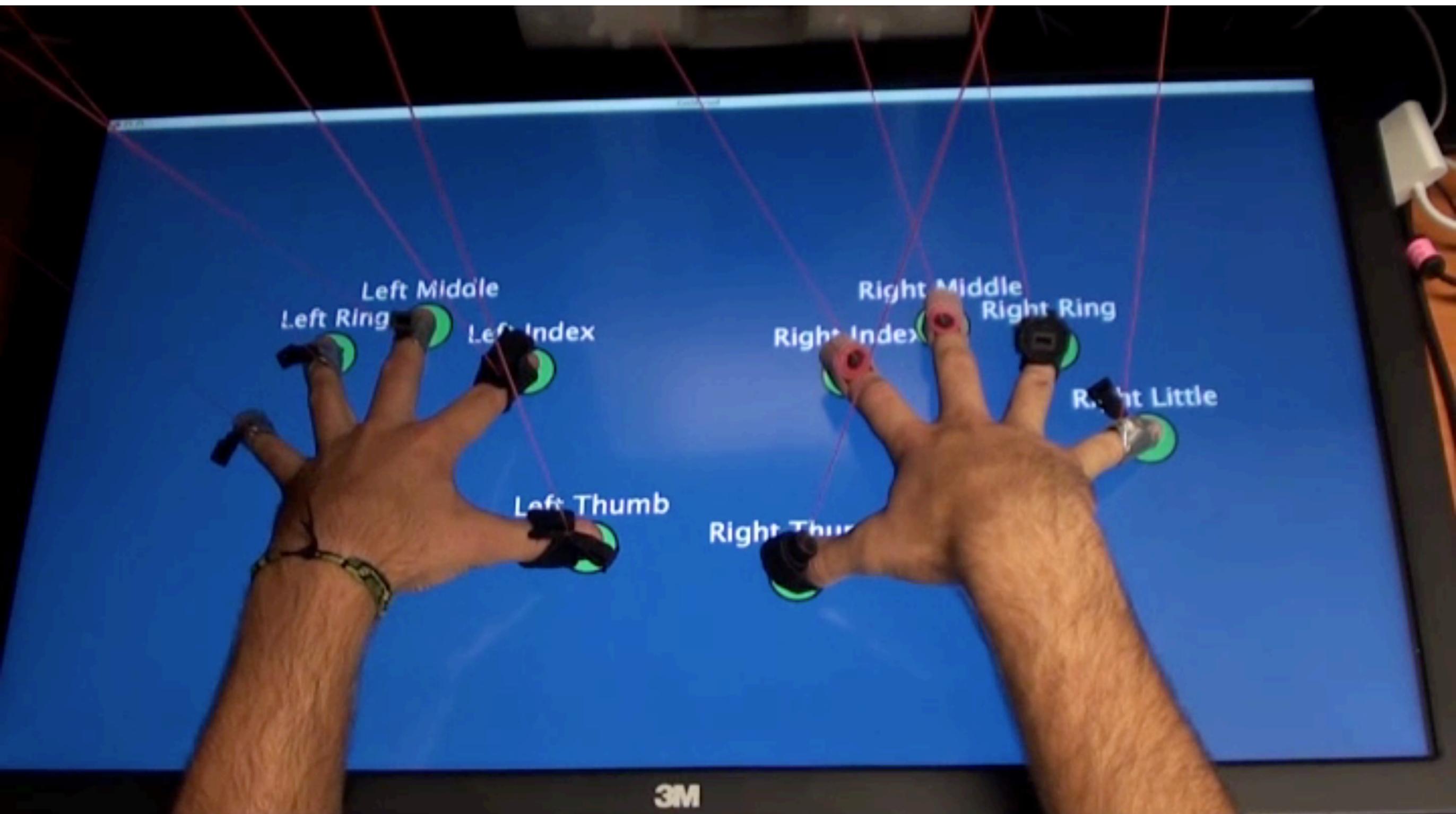
## Mockup Builder [Araujo, Casiez et al. 2012]



## Mockup Builder [Araujo, Casiez et al. 2012]



# HotFingers [Goguey, Casiez et al. 2014]



HotFingers [Goguey, Casiez et al. 2014]

